

arbitrary subfields of the finite field. The results developed in this paper are used to construct additional complete sets of frequency squares, rectangles and hyperrectangles, and orthogonal arrays. Some of the theorems present a relationship between permutation polynomials of a finite field and field permutation functions, an implicit bound on the possible number of functions in an orthogonal field system, and results related to the generation of orthogonal field systems.

- 8.2.21 Remark** For finite rings there are two concepts to distinguish: permutation polynomials (as above) and strong permutation polynomials. The latter are defined via the cardinality of the inverse image. Polynomials are *strong permutation polynomials* (or *strong orthogonal systems*) in n variables if they can be completed to an orthogonal system of n polynomials in n variables.
- 8.2.22 Theorem** [1129] If R is a local ring whose maximal ideal has a minimal number m of generators, then for every $n > m$ there exists a permutation polynomial in n variables that is not a strong permutation polynomial.
- 8.2.23 Corollary** [1129] Every permutation polynomial in any number of variables over a local ring R is strong if and only if R is a finite field.
- 8.2.24 Remark** Wei and Zhang showed [2954] that if $n \leq m$ in the setting of Theorem 8.2.22, then every orthogonal system of k polynomials in n variables can be completed to an orthogonal system of n polynomials (and in particular, every permutation polynomial is strong).

See Also

§9.4	Considers κ -polynomials used for constructions of semifields.
§14.1	Discusses orthogonal latin squares and hypercubes.

[1934]	Section 7.5 discusses permutations and orthogonal systems in several variables.
[2183]	Considers bounds for value sets of polynomial vectors in several variables.
[2321]	Considers an application of permutation polynomials and orthogonal systems to pseudorandom number generation.
[3056]	Considers permutation polynomials over finite commutative rings.

References Cited: [539, 1129, 1932, 1934, 1935, 2027, 2167, 2169, 2222, 2223, 2224, 2321, 2733, 2954, 3056]

8.3 Value sets of polynomials

Gary L. Mullen, The Pennsylvania State University
Michael E. Zieve, University of Michigan

- 8.3.1 Definition** For $f \in \mathbb{F}_q[x]$, the *value set of f* is the set $V_f = \{f(a) | a \in \mathbb{F}_q\}$; the cardinality of V_f is denoted by $\#V_f$.

8.3.2 Remark Every subset of \mathbb{F}_q occurs as V_f for some $f \in \mathbb{F}_q[x]$ of degree at most $q-1$ (by the Lagrange Interpolation Formula); see Theorem 2.1.131.

8.3.1 Large value sets

8.3.3 Remark Any $f \in \mathbb{F}_q[x]$ satisfies $\#V_f \leq q$; equality occurs precisely when f is a permutation polynomial; see Section 8.1.

8.3.4 Theorem Suppose $f \in \mathbb{F}_q[x]$ of degree n is not a permutation polynomial. Then:

1. [2823, 2908, 2979] $\#V_f \leq q - \lceil (q-1)/n \rceil$.
2. [1083, 1363, 1364] If $\#V_f \neq (1-1/n)q$ and $n > 5$ then $\#V_f \leq (1-2/n)q + O_n(\sqrt{q})$.
3. [1363] If $\gcd(n, q) = 1$ then $\#V_f \leq (5/6)q + O_n(\sqrt{q})$.

8.3.5 Example [755] Let $q = r^k$ where r is a prime power and k is a positive integer. Then $f(x) := x^r + x^{r-1}$ satisfies $\#V_f = q - q/r$, and hence achieves equality in (1).

8.3.2 Small value sets

8.3.6 Remark If $f \in \mathbb{F}_q[x]$ has degree n , then $\#V_f \geq \lceil q/n \rceil$ (since each $\alpha \in \mathbb{F}_q$ has at most n preimages under f).

8.3.7 Definition A polynomial $f \in \mathbb{F}_q[x]$ of degree n is a *minimal value set polynomial* if $\#V_f = \lceil q/n \rceil$.

8.3.8 Theorem [546] Let $f \in \mathbb{F}_p[x]$ have degree n , where p is prime. If $n < p$ and $\#V_f = \lceil p/n \rceil \geq 3$, then n divides $p-1$ and $f(x) = a(x+b)^n + c$ with $a, b, c \in \mathbb{F}_p$.

8.3.9 Theorem [2100] Let $f \in \mathbb{F}_q[x]$ be monic of degree n , where $\gcd(n, q) = 1$ and $n \leq \sqrt{q}$. If $\#V_f = \lceil q/n \rceil$, then n divides $q-1$ and $f(x) = (x+b)^n + c$ with $b, c \in \mathbb{F}_q$.

8.3.10 Problem Determine all minimal value set polynomials over \mathbb{F}_{p^k} . This is done for $k \leq 2$ in [2100].

8.3.11 Remark Minimal value set polynomials whose values form a subfield are characterized in [350]. A connection between minimal value set polynomials and Frobenius non-classical curves is given in [349].

8.3.12 Theorem [623, 1308] If $f(x) \in \mathbb{F}_q[x]$ is monic of degree $n > 15$, where $n^4 < q$ and $\#V_f < 2q/n$, then $f(x)$ has one of the forms:

1. $(x+a)^n + b$, where $n \mid (q-1)$;
2. $((x+a)^{n/2} + b)^2 + c$, where $n \mid (q^2-1)$;
3. $((x+a)^2 + b)^{n/2} + c$, where $n \mid (q^2-1)$.

8.3.13 Theorem [288] Let $f \in \mathbb{F}_p[x]$ have degree less than $\frac{3}{4}(p-1)$, where p is prime. If $\#f(\mathbb{F}_p^*) = 2$ then f is a polynomial in $x^{(p-1)/d}$ for some $d \in \{2, 3\}$.

8.3.14 Remark This result indicates that some phenomena become apparent only when one considers $\#f(\mathbb{F}_p^*)$ rather than $\#V_f$.

8.3.3 General polynomials

8.3.15 Theorem [284, 2978] Fix n , and let $e_n := \sum_{j=1}^n (-1)^{j-1}/j!$. There is a constant a_n such that, for each q , there are $q^n + O_n(q^{n-1})$ monic polynomials $f \in \mathbb{F}_q[x]$ of degree n satisfying $|\#V_f - e_n q| \leq a_n \sqrt{q}$.

8.3.16 Remark The previous result says that if q is large compared to n then most polynomials over \mathbb{F}_q of degree n take approximately $e_n q$ values. Note that $e_n \rightarrow 1 - 1/e$ as $n \rightarrow \infty$.

8.3.17 Theorem [662] For fixed n , there is a finite set T_n of rational numbers such that: for any q , and any $f \in \mathbb{F}_q[x]$ of degree n , there is an element $c_f \in T_n$ such that $\#V_f = c_f q + O_n(\sqrt{q})$.

8.3.18 Remark The set T_n may be chosen to be $\{a/n! : (n-1)! \leq a \leq n!\}$.

8.3.19 Remark For fixed n , if q is large and $f \in \mathbb{F}_q[x]$ has degree n , then $\#V_f/q$ lies in a tiny interval around a member of a finite set; crucially, this finite set depends only on n , and not on q .

8.3.20 Theorem [662] Let $f \in \mathbb{F}_q[x]$ have degree n , and write $f = g(x^{p^j})$ where $j \geq 0$ and $g \in \mathbb{F}_q[x] \setminus \mathbb{F}_q[x^p]$; here p is the characteristic of \mathbb{F}_q . Let t be transcendental over \mathbb{F}_q , and let A and G be the Galois groups of $g(x) - t$ over $\mathbb{F}_q(t)$ and $\overline{\mathbb{F}_q}(t)$, respectively, where $\overline{\mathbb{F}_q}$ denotes an algebraic closure of \mathbb{F}_q . Then G is a normal subgroup of A , and A/G is cyclic. The quantity c_f in Theorem 8.3.17 may be taken to be the proportion of elements in a generating coset of A/G which fix at least one of the roots of $g(x) - t$.

8.3.21 Example Let $f \in \mathbb{F}_q[x]$ have degree n .

1. If $n = 2$ then $\#V_f \in \{q/2, (q+1)/2, q\}$.
2. If $n = 3$ then $\#V_f \in \{q/3, (q+2)/3, (2q-1)/3, 2q/3, (2q+1)/3, q\}$.
3. [2038] If $n = 4$ and q is an odd prime then $\#V_f$ is either $(q+3)/4, (q+1)/2, (3q+4+i)/8$ with $\pm i \in \{1, 3, 5\}$, or $5q/8 + O(\sqrt{q})$.

8.3.4 Lower bounds

8.3.22 Theorem [2916] If $\mu_q(f)$ is the smallest positive integer i so that $\sum_{a \in \mathbb{F}_q} (f(a))^i \neq 0$, then $\#V_f \geq \mu_q(f) + 1$.

8.3.23 Remark Assume that for a polynomial f the degree n of f satisfies $n < q - 1$. Write $(f(x))^i = \sum_{j=0}^{q-1} a_{ij} \text{ mod } (x^q - x)$. Let A_f be the matrix $A_f = (a_{ij}^{q-1})$, for $1 \leq i, j \leq q-1$ so that the (i, j) -th entry of A_f is 1 if the coefficient of x^j in $(f(x))^i \text{ mod } (x^q - x)$ is nonzero. If f is not the zero polynomial, then A_f has at least one nonzero column. If the j -th column of A_f consists entirely of 0's or entirely of 1s, set $l_j = 0$. Otherwise, for a nonzero j -th column of A_f , arrange the entries in a circle and define l_j to be the maximum number of consecutive zeros appearing in this circular arrangement. Let L_f be the maximum of the values of l_j , where the maximum is taken over all of the $q-1$ columns of the matrix A_f .

8.3.24 Theorem [769] With notation as above, $|V_f| \geq L_f + 2$.

8.3.25 Remark [625] If f is a polynomial over \mathbb{F}_q and A'_f is the matrix from Remark 8.3.23 without the $(q-1)$ -st powers, i.e., the matrix $A'_f = (a_{ij})$, then $\#V_f = 1 + \text{rank}(A'_f)$.

8.3.26 Corollary Since $|V_f| \geq l_{q-1} + 2$, we have the result of Theorem 2.1 of [2916].

8.3.27 Remark The Hermite/Dickson criterion from Section 8.1 is essentially equivalent to the first $q-2$ consecutive elements of the last column of the matrix A_f being 0, with the last

element being 1. Thus f is a permutation polynomial if and only if $L_f = q - 2$.

8.3.28 Remark See [2823] for further inequalities.

8.3.5 Examples

8.3.29 Theorem $\#V_{x^n} = 1 + (q - 1)/(n, q - 1)$.

8.3.30 Definition The *Dickson polynomial* of degree n and parameter $a \in \mathbb{F}_q$ is defined by

$$D_n(x, a) = \sum_{i=0}^{\lfloor n/2 \rfloor} \frac{n}{n-i} \binom{n-i}{i} (-a)^i x^{n-2i}.$$

8.3.31 Remark See Section 9.6 for a discussion of Dickson polynomials over \mathbb{F}_q .

8.3.32 Theorem [623] Suppose q is odd with $2^r \parallel (q^2 - 1)$. Then for each $n \geq 1$, and each $a \in \mathbb{F}_q^*$,

$$\#V_{D_n(x,a)} = \frac{q-1}{2(n, q-1)} + \frac{q+1}{2(n, q+1)} + \alpha,$$

where $\alpha = 1$ if $2^{r-1} \parallel n$; $\alpha = 1/2$ if $2^t \parallel n$ and $1 \leq t \leq r-2$; $\alpha = 0$ otherwise. Here η denotes the quadratic character defined by $\eta(0) = 0$, $\eta(a) = 1$ if a is a square in \mathbb{F}_q and $\eta(a) = -1$ if a is a nonsquare in \mathbb{F}_q .

8.3.33 Remark If $(n_1, q^2 - 1) = (n_2, q^2 - 1)$, then $\#V_{D_{n_1}(x,a)} = \#V_{D_{n_2}(x,a)}$.

8.3.34 Theorem [623] Suppose q is even. Then for each $n \geq 1$, and each $a \in \mathbb{F}_q^*$,

$$\#V_{D_n(x,a)} = \frac{q-1}{2(n, q-1)} + \frac{q+1}{2(n, q+1)}$$

8.3.35 Remark For further examples, see for instance [752, 753].

8.3.6 Further value set papers

8.3.36 Remark There are many other papers describing results concerning value sets of polynomials over finite fields; however for lack of space, we are unable to precisely state them. Pages 379-381 of [1934] provide a wealth of descriptions of older papers dealing with value sets; pages 388-389 of [1934] provide summaries of value set results for polynomials in several variables. The paper [2823] presents the state of knowledge about value sets as of 1995.

8.3.37 Remark Since the publication of [1934], in [767] are given formulas for the number of polynomials of degree $q - 1$ with a value set of cardinality k . Paper [768] describes value sets of diagonal equations over finite fields by giving a new proof of the Cauchy-Davenport theorem. See [752] and [753] for a discussion of polynomials over \mathbb{F}_{2^n} which take on each nonzero value only a small number of times (at most six).

8.3.38 Remark Paper [1219] shows that if f is not a permutation polynomial over \mathbb{F}_q and $q \geq n^4$, then $\#V_f < q - q/(2n)$, while [755] shows that by using the polynomial $(x + 1)x^{q-1}$, Wan's bound is sharp for every extension of the base field. The paper [57] discusses results concerning the size of the intersection of the value sets of two nonconstant polynomials and [1454] discusses lower bounds for the size of the value set for the polynomial $(x^m + b)^n$ improving the bound given in [1307]. Paper [2743] discusses cardinalities of value sets for

diagonal kinds of polynomials in several variables where the preimage points come from subsets of the field rather than the entire field.

See Also

§8.1	Discusses permutation polynomials in one variable.
§8.2	Discusses permutation polynomials in several variables.
§8.4	Considers exceptional polynomials.
[624]	Considers polynomials whose value sets lie in a subfield.
[729]	Studies value sets as they relate to Dembowski-Ostrom and planar polynomials.

References Cited: [57, 284, 288, 349, 350, 546, 623, 624, 625, 662, 729, 752, 753, 755, 767, 768, 769, 1083, 1219, 1307, 1308, 1363, 1364, 1454, 1934, 2038, 2100, 2743, 2823, 2908, 2916, 2978, 2979]

8.4 Exceptional polynomials

Michael E. Zieve, University of Michigan

8.4.1 Fundamental properties

8.4.1 Definition An *exceptional polynomial* over \mathbb{F}_q is a polynomial $f \in \mathbb{F}_q[x]$ which is a permutation polynomial on \mathbb{F}_{q^m} for infinitely many m .

8.4.2 Remark If $f \in \mathbb{F}_q[x]$ is exceptional over \mathbb{F}_{q^k} for some k , then f is exceptional over \mathbb{F}_q .

8.4.3 Definition A polynomial $F(x, y) \in \mathbb{F}_q[x, y]$ is *absolutely irreducible* if it is irreducible in $\overline{\mathbb{F}_q}[x, y]$, where $\overline{\mathbb{F}_q}$ is an algebraic closure of \mathbb{F}_q .

8.4.4 Theorem [662] A polynomial $f \in \mathbb{F}_q[x]$ is exceptional over \mathbb{F}_q if and only if every absolutely irreducible factor of $f(x) - f(y)$ in $\mathbb{F}_q[x, y]$ is a constant times $x - y$.

8.4.5 Corollary If $f \in \mathbb{F}_q[x]$ is exceptional, then there are integers $1 < e_1 < e_2 < \dots < e_k$ such that: f is exceptional over \mathbb{F}_{q^n} if and only if n is not divisible by any e_i .

8.4.6 Corollary If $f \in \mathbb{F}_q[x]$ is exceptional, then there is an integer $M > 1$ such that f permutes each field \mathbb{F}_{q^m} for which m is coprime to M .

8.4.7 Corollary For $g, h \in \mathbb{F}_q[x]$, the composition $g \circ h$ is exceptional if and only if both g and h are exceptional.

8.4.8 Definition A polynomial $f \in \mathbb{F}_q[x]$ is *indecomposable* if it cannot be written as the composition $f = g \circ h$ of two nonlinear polynomials $g, h \in \mathbb{F}_q[x]$.

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