

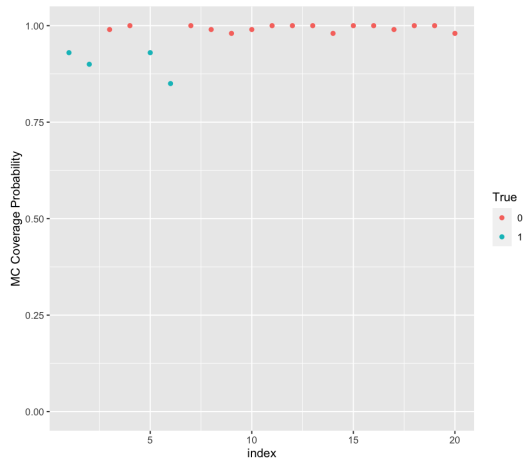
**Supplementary Information for “Bayesian Inference  
for High Dimensional Cox Models with Gaussian and  
Diffused-Gamma Priors: A Case Study of Mortality  
in COVID-19 Patients Admitted to the ICU”**

**Table S1:** Over 100 repetitions with  $n = 100$  and  $p = 100$ , comparisons of MAP estimates obtained by the GD prior approach with the estimates by the MCP, BLASSO, and DLASSO methods. All noise variables with true values of 0 are averaged and grouped as “Noise.”

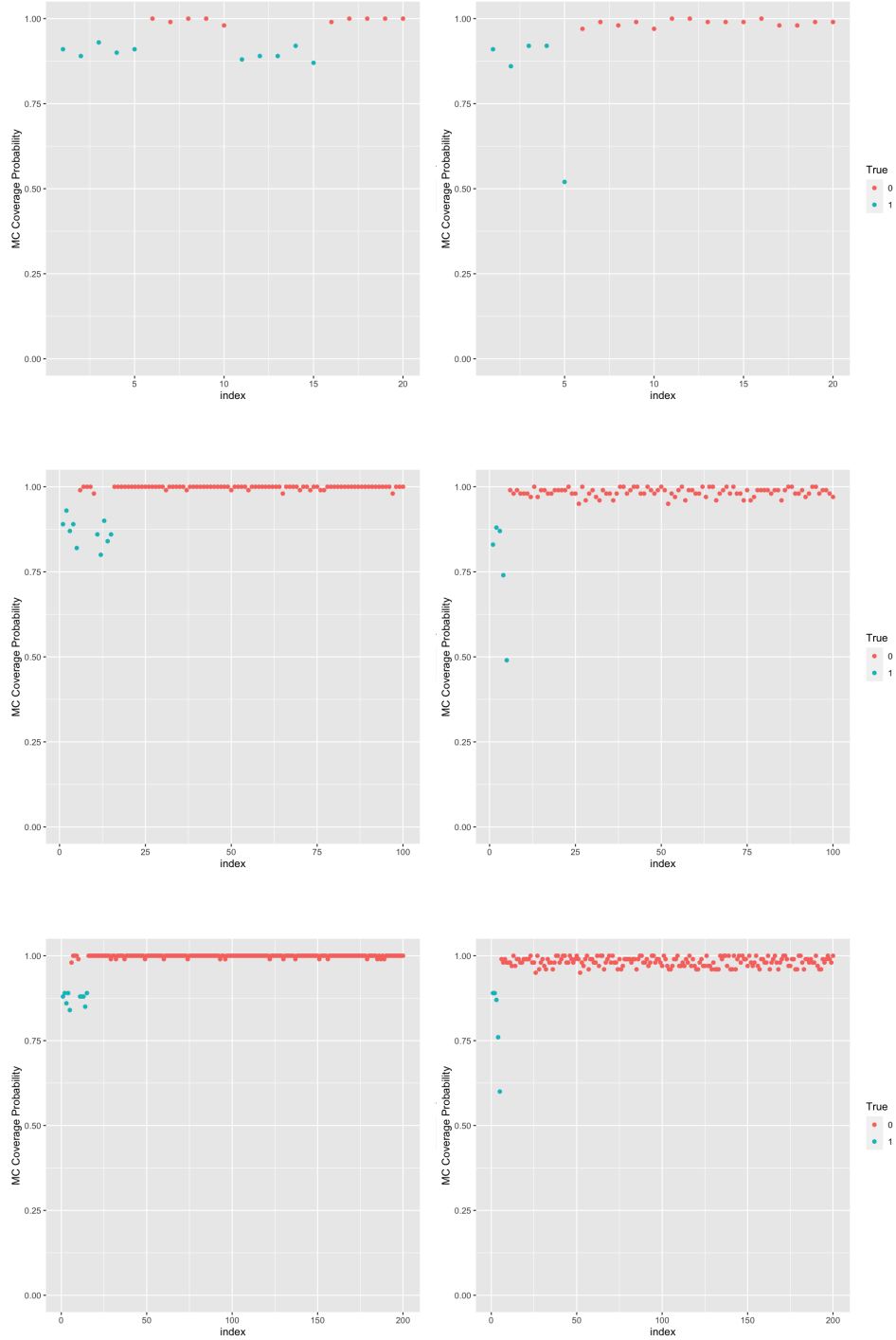
|            | COEF         | TRUE      | MCP         |            | BLASSO      |            | GD          |            |      |
|------------|--------------|-----------|-------------|------------|-------------|------------|-------------|------------|------|
|            |              |           | MEAN(SE)    | MSE        | MEAN(SE)    | MSE        | MEAN(SE)    | MSE        |      |
| Scenario 1 | $\beta_1$    | 1         | 1.06(0.21)  | 0.05       | 1.02(0.21)  | 0.04       | 0.99(0.16)  | 0.03       |      |
|            | $\beta_2$    | 1         | 1.06(0.19)  | 0.04       | 1.02(0.2)   | 0.04       | 0.99(0.16)  | 0.03       |      |
|            | $\beta_5$    | 1         | 1.04(0.2)   | 0.04       | 1(0.21)     | 0.04       | 0.97(0.17)  | 0.03       |      |
|            | $\beta_6$    | 1         | 1.06(0.22)  | 0.05       | 1.02(0.22)  | 0.05       | 1(0.18)     | 0.03       |      |
|            | Noise        | 0         | 0(0)        | 0.00       | 0(0)        | 0.00       | 0(0)        | 0.00       |      |
|            |              |           |             |            |             |            |             |            |      |
| Scenario 2 | $\beta_1$    | 1         | 0.85(0.62)  | 0.41       | 0.61(0.21)  | 0.20       | 0.92(0.25)  | 0.07       |      |
|            | $\beta_2$    | 1         | 0.94(0.57)  | 0.33       | 0.7(0.21)   | 0.13       | 0.98(0.24)  | 0.06       |      |
|            | $\beta_3$    | 1         | 0.84(0.65)  | 0.44       | 0.67(0.23)  | 0.16       | 0.93(0.26)  | 0.07       |      |
|            | $\beta_4$    | 1         | 1(0.57)     | 0.32       | 0.69(0.21)  | 0.14       | 0.99(0.25)  | 0.06       |      |
|            | $\beta_5$    | 1         | 0.77(0.56)  | 0.37       | 0.6(0.22)   | 0.20       | 0.91(0.24)  | 0.07       |      |
|            | $\beta_{11}$ | 1         | 0.83(0.56)  | 0.34       | 0.61(0.2)   | 0.19       | 0.95(0.23)  | 0.05       |      |
|            | $\beta_{12}$ | 1         | 0.91(0.6)   | 0.36       | 0.66(0.24)  | 0.17       | 0.93(0.3)   | 0.09       |      |
|            | $\beta_{13}$ | 1         | 0.86(0.59)  | 0.36       | 0.68(0.22)  | 0.15       | 0.95(0.23)  | 0.05       |      |
|            | $\beta_{14}$ | 1         | 0.94(0.6)   | 0.36       | 0.67(0.24)  | 0.17       | 0.96(0.27)  | 0.07       |      |
|            | $\beta_{15}$ | 1         | 0.82(0.55)  | 0.33       | 0.61(0.19)  | 0.19       | 0.93(0.21)  | 0.05       |      |
|            | Noise        | 0         | 0(0)        | 0.00       | 0(0)        | 0.00       | 0(0)        | 0.00       |      |
|            |              |           |             |            |             |            |             |            |      |
|            | Scenario 3   | $\beta_1$ | 1           | 0.62(0.52) | 0.41        | 0.74(0.32) | 0.17        | 1(0.26)    | 0.07 |
|            |              | $\beta_2$ | 1           | 0.63(0.55) | 0.44        | 0.71(0.32) | 0.19        | 0.94(0.29) | 0.08 |
|            |              | $\beta_3$ | 1           | 0.64(0.5)  | 0.38        | 0.73(0.29) | 0.16        | 0.96(0.28) | 0.08 |
| $\beta_4$  |              | -2.121    | -1.05(1.17) | 2.51       | -1.29(0.76) | 1.27       | -1.87(0.47) | 0.28       |      |
| $\beta_5$  |              | 0.333     | 0.12(0.17)  | 0.07       | 0.18(0.13)  | 0.04       | 0.2(0.21)   | 0.06       |      |
| Noise      |              | 0         | 0(0.01)     | 0.00       | 0(0.01)     | 0.00       | 0(0.01)     | 0.00       |      |

**Table S2:** Over 100 repetitions with  $n = 100$  and  $p = 200$ , comparisons of MAP estimates obtained by the GD prior approach with the estimates by the MCP, BLASSO, and DLASSO methods. All noise variables with true values of 0 are averaged and grouped as “Noise.”

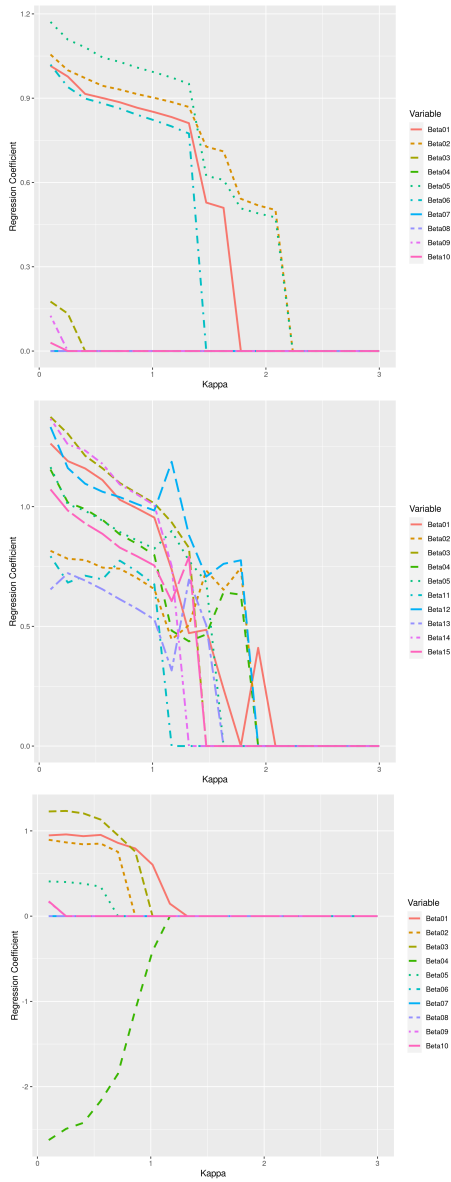
|            | COEF         | TRUE      | MCP         |            | BLASSO     |            | GD          |            |      |
|------------|--------------|-----------|-------------|------------|------------|------------|-------------|------------|------|
|            |              |           | MEAN(SE)    | MSE        | MEAN(SE)   | MSE        | MEAN(SE)    | MSE        |      |
| Scenario 1 | $\beta_1$    | 1         | 1.02(0.18)  | 0.03       | 1.01(0.2)  | 0.04       | 0.99(0.14)  | 0.02       |      |
|            | $\beta_2$    | 1         | 1(0.2)      | 0.04       | 1(0.18)    | 0.03       | 1(0.16)     | 0.03       |      |
|            | $\beta_5$    | 1         | 1.01(0.2)   | 0.04       | 1.02(0.2)  | 0.04       | 1.01(0.16)  | 0.03       |      |
|            | $\beta_6$    | 1         | 1.01(0.2)   | 0.04       | 1(0.21)    | 0.04       | 1.01(0.16)  | 0.03       |      |
|            | Noise        | 0         | 0(0)        | 0.00       | 0(0)       | 0.00       | 0(0)        | 0.00       |      |
|            |              |           |             |            |            |            |             |            |      |
| Scenario 2 | $\beta_1$    | 1         | 0.49(0.54)  | 0.55       | 0.53(0.21) | 0.26       | 0.9(0.21)   | 0.05       |      |
|            | $\beta_2$    | 1         | 0.71(0.57)  | 0.41       | 0.65(0.24) | 0.18       | 0.93(0.23)  | 0.06       |      |
|            | $\beta_3$    | 1         | 0.56(0.57)  | 0.51       | 0.62(0.24) | 0.20       | 0.92(0.23)  | 0.06       |      |
|            | $\beta_4$    | 1         | 0.68(0.59)  | 0.44       | 0.59(0.23) | 0.22       | 0.91(0.24)  | 0.06       |      |
|            | $\beta_5$    | 1         | 0.48(0.52)  | 0.54       | 0.56(0.24) | 0.25       | 0.9(0.3)    | 0.10       |      |
|            | $\beta_{11}$ | 1         | 0.52(0.58)  | 0.57       | 0.54(0.25) | 0.27       | 0.92(0.23)  | 0.06       |      |
|            | $\beta_{12}$ | 1         | 0.66(0.59)  | 0.46       | 0.63(0.22) | 0.19       | 0.92(0.25)  | 0.07       |      |
|            | $\beta_{13}$ | 1         | 0.63(0.61)  | 0.50       | 0.64(0.23) | 0.18       | 0.94(0.25)  | 0.07       |      |
|            | $\beta_{14}$ | 1         | 0.63(0.59)  | 0.48       | 0.58(0.26) | 0.24       | 0.91(0.27)  | 0.08       |      |
|            | $\beta_{15}$ | 1         | 0.53(0.51)  | 0.48       | 0.57(0.18) | 0.22       | 0.92(0.19)  | 0.04       |      |
|            | Noise        | 0         | 0(0)        | 0.00       | 0(0)       | 0.00       | 0(0)        | 0.00       |      |
|            |              |           |             |            |            |            |             |            |      |
|            | Scenario 3   | $\beta_1$ | 1           | 0.38(0.48) | 0.62       | 0.64(0.35) | 0.26        | 1.03(0.25) | 0.06 |
|            |              | $\beta_2$ | 1           | 0.3(0.45)  | 0.70       | 0.59(0.36) | 0.30        | 0.95(0.34) | 0.12 |
|            |              | $\beta_3$ | 1           | 0.36(0.47) | 0.63       | 0.62(0.35) | 0.26        | 0.95(0.34) | 0.12 |
| $\beta_4$  |              | -2.121    | -0.39(0.92) | 3.83       | -1.16(0.9) | 1.71       | -1.87(0.57) | 0.39       |      |
| $\beta_5$  |              | 0.333     | 0.07(0.13)  | 0.09       | 0.14(0.12) | 0.05       | 0.25(0.25)  | 0.07       |      |
| Noise      |              | 0         | 0(0)        | 0.00       | 0(0)       | 0.00       | 0(0)        | 0.00       |      |



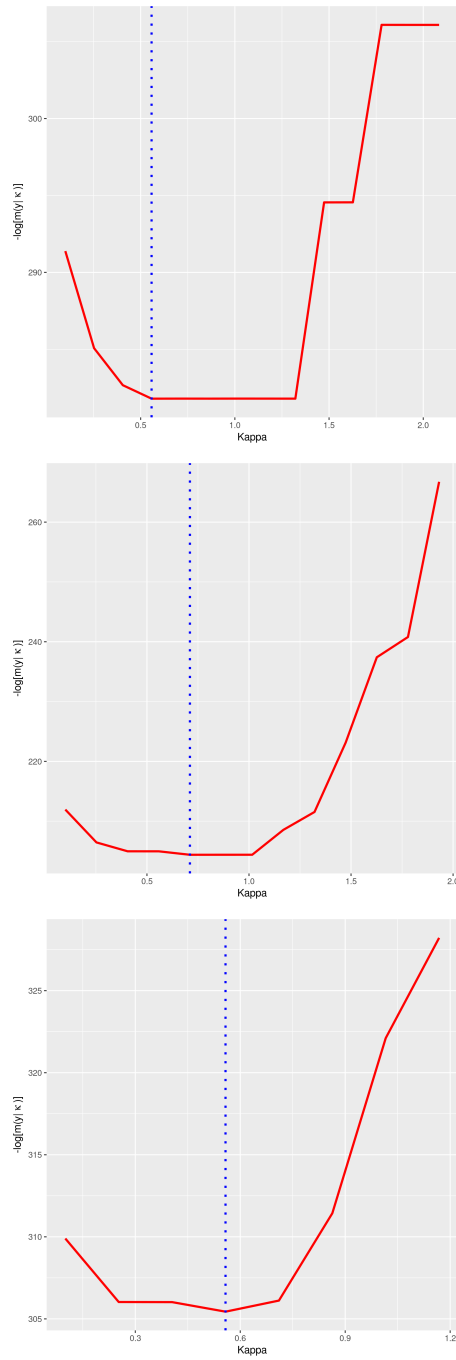
**Fig. S1:** MC coverage plot for Scenario 1 for  $n = 100$  and  $p = 20$ . The legend “True” is 1 if the variable is nonzero and 0 if the variable is zero.



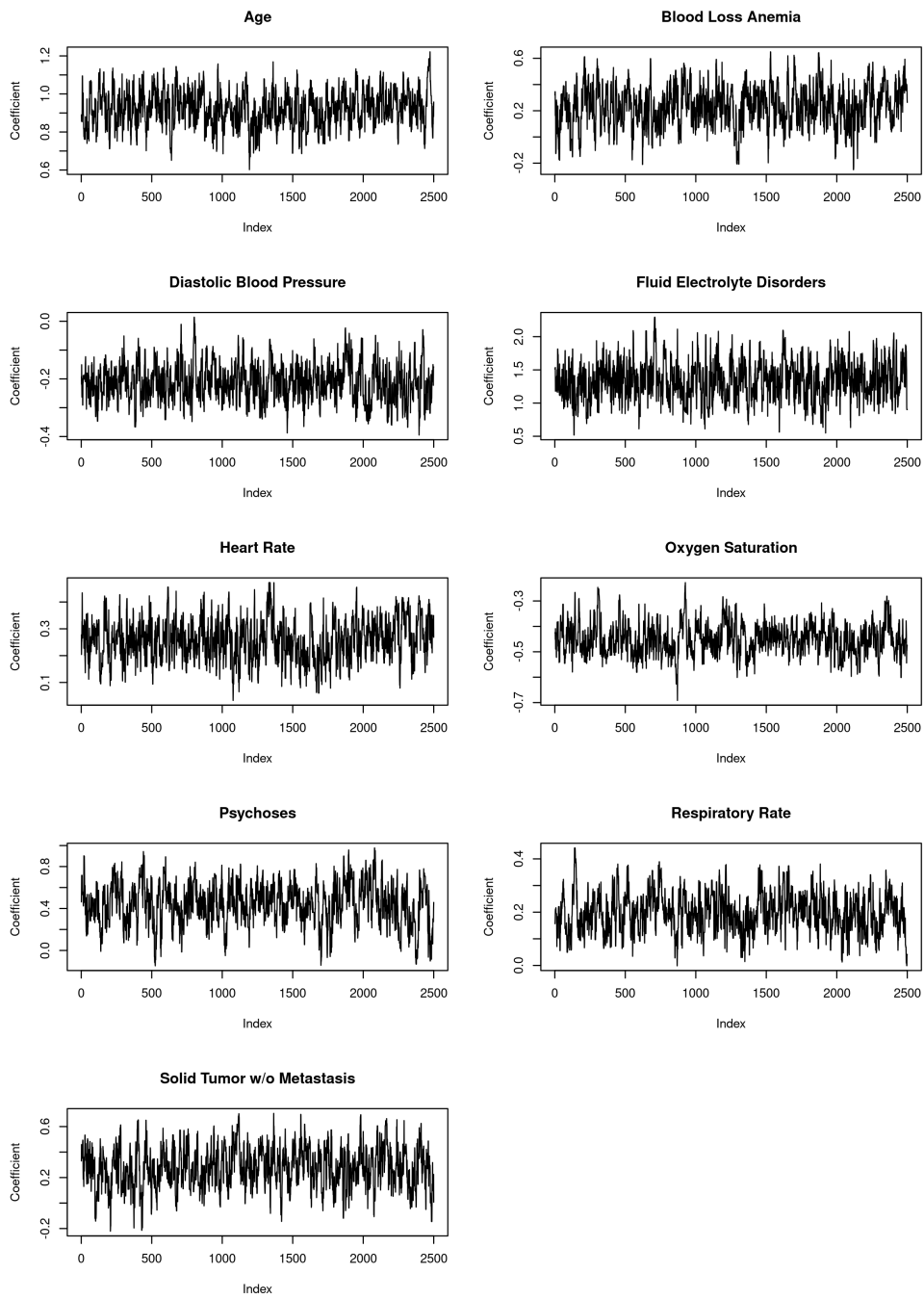
**Fig. S2:** MC coverage plot for Scenario 2 (left column) and Scenario 3 (right column) for  $n = 100$  and  $p = 20, 100, 200$ . The legend True represents 1 if the variable is nonzero or 0 if the variable is zero.



**Fig. S3:** Solution path for the tuning parameter in Scenarios 1 (top), 2 (middle), and 3 (bottom) for  $n = 100$  and  $p = 20$ . The path for the first 10 regression coefficients in Scenarios 1 and 3, and the 10 regression coefficients with true values of 1 are displayed in Scenario 2.

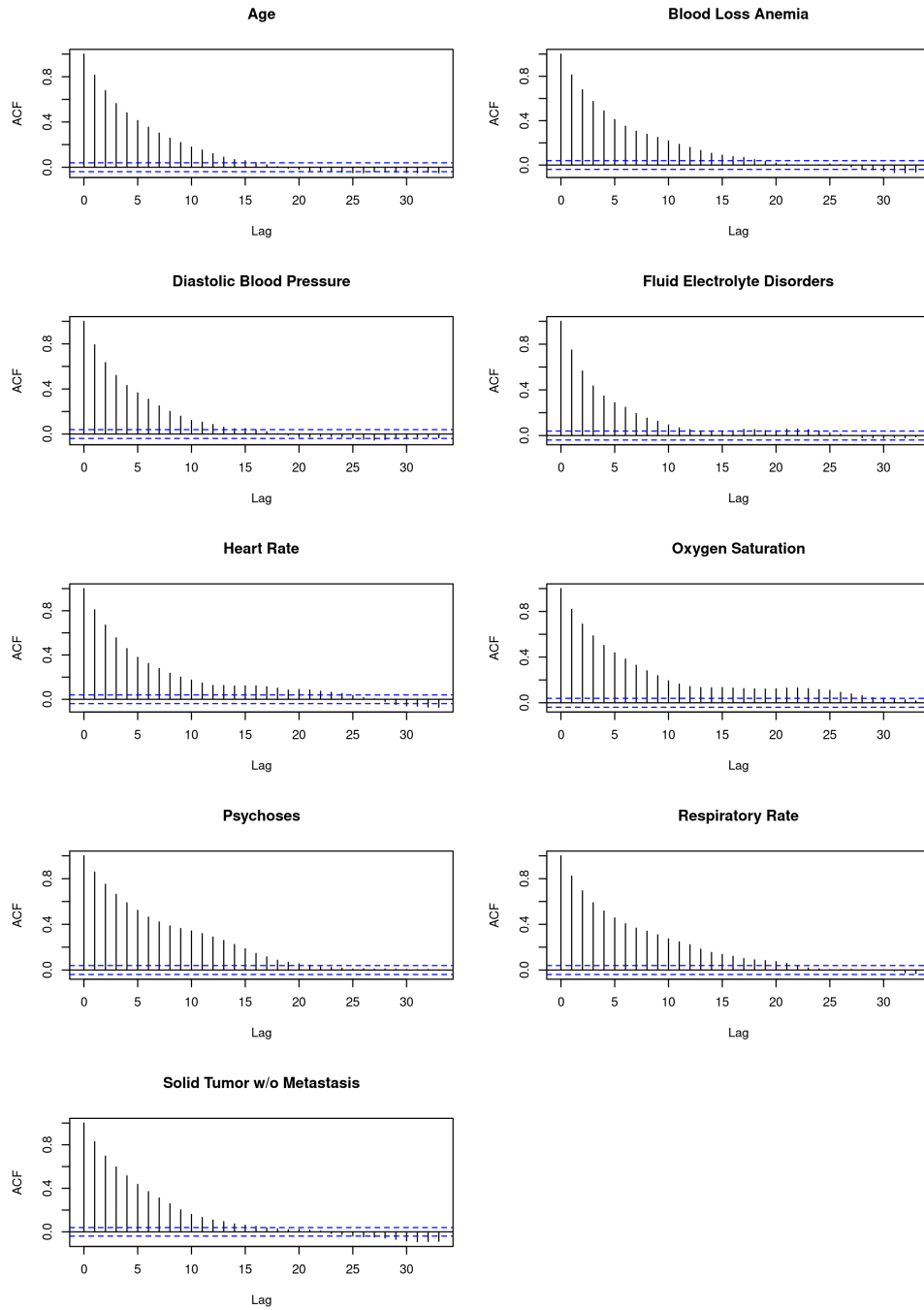


**Fig. S4:** Marginal likelihood estimates for selecting tuning parameter  $\kappa$  selection in Scenarios 1 (top), 2 (middle), and 3 (bottom), with  $n = 100$  and  $p = 20$ . The chosen  $\kappa$  is indicated by the blue dotted vertical line corresponding to the maximum marginal likelihood.



**Fig. S5:** MCMC trace plots for the selected variables in COVID-19 data.





**Fig. S6:** MCMC autocorrelation plots of the selected variables in COVID-19 data.