

Show all work and include units where appropriate. You have 30 minutes to complete this quiz. (25 pts)

1. Consider the function

$$p(x) = \begin{cases} 0, & \text{if } x < 0 \\ kx^2(1-x), & \text{if } 0 \leq x \leq 1 \\ 0, & \text{if } x > 1 \end{cases}$$

- (a) For what value of  $k$  is  $p(x)$  a probability density function? (3 pts)

- (b) Using that value of  $k$ , find the probability that  $x$  is greater than 0.5.(2 pts)

- (c) Find the mean.(3 pts)

- (d) Find the median.(3 pts)

2. Use the formulas for the sums of geometric series on the following. (3 pts each)

(a)  $1 - \frac{1}{2} + \frac{1}{4} - \frac{1}{8} + \cdots$

(b)  $\sum_{n=5}^{15} \left(\frac{2}{3}\right)^n$

3. Suppose that you make monthly deposits into a savings account of \$250, with the first deposit occurring today. Every month, your account pays 4% interest. Let  $B_n$  represent the balance in your account immediately after the  $n$ th deposit.

(a) Find  $B_1$ ,  $B_2$ , and  $B_3$ . (3 pts)

(b) Find a closed form, explicit formula (that is, no summation signs or  $+\cdots+$ ) for  $B_n$ . (5 pts)