PROBLEM SET 3 (DUE ON THURSDAY, OCT 1)

(All Exercises are references to the November 18, 2017 version of *Foundations of Algebraic Geometry* by R. Vakil.)

- **Problem 1.** Exercise 3.6.K (sometimes functions are determined by their values on closed points)
- **Problem 2.** Use the existence of the structure sheaf $\mathcal{O}_{\operatorname{Spec} A}$ to show that if $\operatorname{Spec} A$ is disconnected, then A is isomorphic to a product of two nonzero rings.
- **Problem 3.** Let $X = \operatorname{Spec} k[x,y,z]/(xz,yz)$ and let $U \subset X$ be the complement of the closed point [(x,y,z)]. Compute the ring $\mathcal{O}_X(U)$ along with the restriction map $\operatorname{res}_{X,U}: \mathcal{O}_X(X) \to \mathcal{O}_X(U)$. Is $\operatorname{res}_{X,U}$ isomorphic to some localization map $A \to S^{-1}A$?
- **Problem 4.** Exercise 4.3.A (classifying isomorphisms of affine schemes)