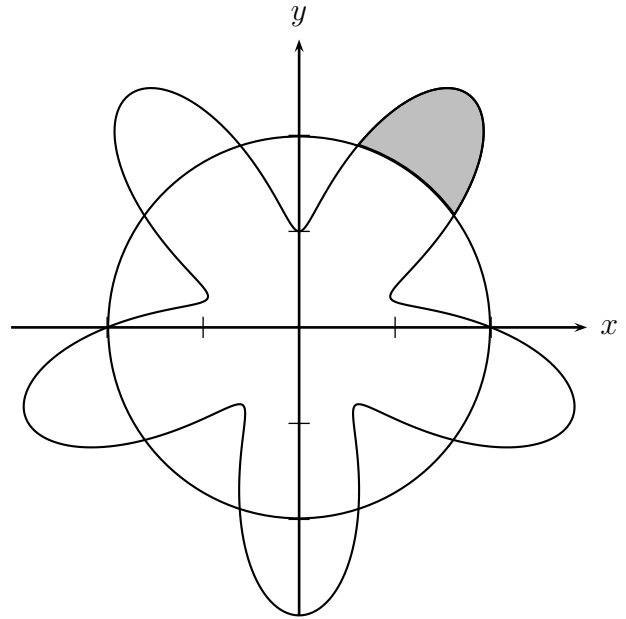


Worksheet Until We Meet Again

1. (Adapted from a Fall, 2010 Math 116 Exam) In the picture to the right, the graphs of $r = 2$ and $r = 2 - \sin(5\theta)$ are shown.

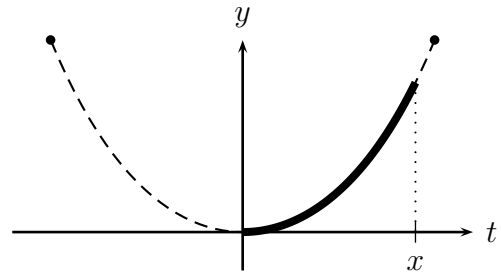


- Write a definite integral that computes the shaded area.
- Compute the area exactly.
- Write an integral for the length of the boundary of the shaded area.
- Get an approximate answer for that length, using your calculator.

2. We've made some progress finding the shape of a hanging chain. If the shape is given by $F(x)$, then by considering forces and arc length we've shown that

$$T_0 F'(x) = \delta g \int_0^x \sqrt{1 + F'(t)^2} dt$$

where T_0 is the tension at the bottom of the chain, δ is the mass density of the chain, and g is acceleration due to gravity (all constants). Where to go from here? We'd like to find a formula for $F(x)$.



- That thing on the right is begging for you take its derivative. ("Take my derivative!" it cries.) So take the derivative of both sides with respect to x .
- Hmmm. No F s, only F' s. And lots of constants. Let $y = F'(x)$, and put all the constants together into one constant. That should make it look better.
- What is y when x is 0? Now you have an initial value to go with your differential equation.
- Separate the variables and solve the differential equation.