Douglass Houghton Workshop, Section 2, Tue 03/17/20 Worksheet Magnificent

1. Let

- S = The fraction of people who are susceptible to infection,
- I = The fraction of people currently infected, and
- R = The fraction of people who have been removed.

Suppose also that the probability that the disease is transmitted during a single interaction between an infected and susceptible person is .01 (1%).

- (a) Suppose Bob is a susceptible person, and on a given day he interacts with n other people, chosen randomly. About how many infected people did he interact with?
- (b) What's the probability Bob was NOT infected the first time he met an infected person AND not infected the second time he met an infected person? Assume the interactions are independent.
- (c) What's the probability that Bob wasn't infected by any of his interactions?
- (d) What's the last answer if the probability of transmission is p instead of .01?
- 2. So the probability that Bob becomes infected is

$$1 - (1 - p)^{nl}$$

where p is 1% or less, and nI is on the order of 10 or 20.

(a) Find the first two nonzero terms of the Taylor series about x = 0 for

$$f(x) = (1-x)^k$$

where k is some constant.

- (b) Use that to approximate the probability that Bob becomes infected.
- 3. So we can model the disease's spread by saying that the three types of people change accoring to these equations:

$$S(t+1) = S(t) - npI(t)S(t)$$
$$I(t+1) = I(t) + npI(t)S(t) - vI(t)$$
$$R(t+1) = R(t) + vI(t)$$

n is the number of contacts per person,

where p is the probability of one contact between an S and an I resulting in infection, and v is the removal rate.

Use the Google sheet for your group to model the disease using those equations. n, p, and v are defined to refer to the numbers in the upper-right corner of the sheet. So you can use those letters in your equations. Once you get it to work, try changing the value of n to see what happens.