

# Homework Set 5

MATH 201 — WINTER 2015

*Due Tuesday, February 17*

## **Section 3.2**

Problems 30, 34, 40.

## **Section 3.3**

Problems 20, 22, 28.

## **Section 4.1**

Problems 2, 6, 10, 14, 18.

## **Section 4.2**

Problems 6, 10, 24, 28, 30.

**PROBLEM 5.1.** Let  $A$  be an  $n \times n$  matrix. Suppose that  $\text{Nul}(A) = \{\mathbf{0}\}$ . Does it follow that  $\text{Col}(A) = \mathbb{R}^n$ ? Justify your answer.

**PROBLEM 5.2.** Let  $A$  be a  $3 \times 2$  matrix. Suppose that  $\text{Nul}(A) = \{\mathbf{0}\}$ . Does it follow that  $\text{Col}(A) = \mathbb{R}^3$ ? Justify your answer.

**PROBLEM 5.3.** Let  $A$  be an  $m \times n$  matrix and  $B$  be an  $n \times p$  matrix. Prove that  $\text{Col}(AB)$  is a subspace of  $\text{Col}(A)$ .

**PROBLEM 5.4.** Let  $A, B$  be  $n \times n$  matrices. Is  $\text{Col}(AB)$  a subspace of  $\text{Col}(B)$ ? Justify your answer.