Dark energy survey year 3 results: Cosmology with peaks using an emulator approach


Affiliations are listed at the end of the paper

Accepted 2022 January 10. Received 2022 January 10; in original form 2021 October 21

ABSTRACT

We constrain the matter density $\Omega_m$ and the amplitude of density fluctuations $\sigma_8$ within the $\Lambda$CDM cosmological model with shear peak statistics and angular convergence power spectra using mass maps constructed from the first three years of data of the Dark Energy Survey (DES Y3). We use tomographic shear peak statistics, including cross-peaks; peak counts calculated on maps created by taking a harmonic space product of the convergence of two tomographic redshift bins. Our analysis follows a forward-modelling scheme to create a likelihood of these statistics using $N$-body simulations, using a Gaussian process emulator. We take into account the uncertainty from the remaining, largely unconstrained $\Lambda$CDM parameters ($\Omega_b$, $n_s$, and $h$). We include the following lensing systematics: multiplicative shear bias, photometric redshift uncertainty, and galaxy intrinsic alignment. Stringent scale cuts are applied to avoid biases from unmodelled baryonic physics. We find that the additional non-Gaussian information leads to a tightening of the constraints on the structure growth parameter yielding $S_8 \equiv \sigma_8 \sqrt{\Omega_m/0.3} = 0.797^{+0.015}_{-0.013}$ (68 per cent confidence limits), with a precision of 1.8 per cent, an improvement of 38 per cent compared to the angular power spectra only case. The results obtained with the angular power spectra and peak counts are found to be in agreement with each other and no significant difference in $S_8$ is recorded. We find a mild tension of 1.5$\sigma$ between our study and the results from Planck 2018, with our analysis yielding a lower $S_8$. Furthermore, we observe that the combination of angular power spectra and tomographic peak counts breaks the degeneracy between galaxy intrinsic alignment $A_{\text{IA}}$ and $S_8$, improving cosmological constraints. We run a suite of tests concluding that our results are robust and consistent with the results from other studies using DES Y3 data.

Key words: cosmology: observations.
1 INTRODUCTION

The large scale structure (LSS) of the Universe is a powerful probe for testing cosmological models (see Albrecht et al. 2006; Kilbinger 2015, for reviews). Recent measurements from observational programs that map the LSS such as the Dark Energy Survey1 (DES), Kilo-Degree Survey2 (KiDS), and Hyper-Suprime Cam3 (HSC) have delivered cosmological constraints on the matter density $\Omega_m$ and amplitude of density fluctuations $\sigma_8$ with better than 5 per cent precision.4 This has revealed evidence of moderate tensions between the LSS measurements and measurements using the cosmic microwave background (CMB) for these parameters (Leauthaud et al. 2017; Lemos et al. 2020; Di Valentino et al. 2021); these tensions may indicate that the Lambda Cold Dark Matter (ΛCDM) model is unable to explain these observations jointly, or that our understanding of systematic effects is insufficient. Multiple modelling choices and analysis variants have been explored (Frolova et al. 2018b; Joudaki et al. 2020) in an attempt to understand this discrepancy.

The evolution of the cosmic web substructures of the LSS, consisting of haloes, filaments, sheets, and voids (Bond, Kolb & Pogosyan 1996; Forero-Romero et al. 2009; Dietrich et al. 2012; Libeskind et al. 2018), carries information about the underlying cosmological parameters. Weak gravitational lensing is one of the probes able to map the distribution of these structures directly (see Kilbinger 2015, for review). Not only does it enable us to map their spatial distribution, it also allows us to study their temporal evolution through tomography. Weak lensing mass maps are created using small shape distortions in the images of background galaxies caused by the gravitational lensing due to the foreground LSS (see Bernstein & Jarvis 2002a; Bartelmann & Schneider 2001, for reviews). The information contained in these maps is typically extracted using 2-point statistics such as the real space correlation function, the angular power spectrum, or the wavelet-like COSEBIs (complete orthogonal sets of E/B-integrals) (Asgari et al. 2021). However, 2- point statistics do not capture all the information available in the highly non-Gaussian mass maps (Springel, Frenk & White 2006; Yang et al. 2011). Multiple approaches have been proposed to extract this information: the peak count function, which counts local maxima of the mass maps and thus probes their highly non-linear parts (Jain & Van Waerbeke 2000; Dietrich & Hartlap 2010; Kacprzak et al. 2016, hereafter K16; Martinet et al. 2018; Shan et al. 2018; Harnois-Dérais et al. 2021; Jeffrey, Alsing & Lanusse 2021a), 3-point statistics, which analyse the configurations of triangles at various scales (Takada & Jain 2003; Semboloni et al. 2011; Fu et al. 2014), the higher order moments of convergence maps (Van Waerbeke et al. 2013; Patton et al. 2017; Gatti et al. 2020), the Minkowski functionals, which analyse the topology of the maps (Shirasaki & Yoshida 2014; Petri et al. 2015; Parron et al. 2020), and machine learning approaches, which aim to detect features automatically (Gupta et al. 2018; Fluri et al. 2019; Jeffrey et al. 2021a). Some of these statistics and their combinations increase the precision of the cosmological parameter measurement, as well as responding differently to systematic effects such as galaxy intrinsic alignments (see Zürcher et al. 2021, hereafter Z21, for example).

These approaches increase the cosmological constraining power, but face a major difficulty in their application: the prediction from theory is more challenging than that of 2-point statistics. A possible solution is to use numerical simulations to provide predictions for the statistics. These simulations are computationally expensive, especially for high dimensional parameter spaces that include cosmological, astrophysical, and systematics parameters. Major progress has been made in recent years in creating a fully simulation-based likelihood for cosmic shear measurements, with emerging emulators (Lawrence et al. 2017; Knabenhs et al. 2020; Angulo et al. 2021) and simulation grids (DeRose et al. 2019; Villasenca-Navarro et al. 2021). Map-level implementations of intrinsic alignments (Joachimi et al. 2013) and baryonic effects (Schneider et al. 2020) have recently been used in cosmic shear measurements (Fluri et al. 2018a). This enables a reliable measurement of the structure growth parameter $S_8 \equiv \sigma_8\sqrt{\Omega_m/0.3}$ (the quantity to which weak lensing measurements are the most sensitive) at large and intermediate scales (Weiss et al. 2019). These approaches can shed more light on the tension in this parameter between CMB and LSS measurements by providing cosmological information complementary to the 2-point statistics.

In this work, we infer cosmological parameter constraints using peak counts and the angular power spectra of the tomographic weak lensing mass maps from the first three years of data from the Dark Energy Survey (DES Y3) (Sevilla-Noarbe et al. 2021). The DES Y3 mass maps were first presented in Jeffrey et al. (2021b). We follow a forward-modelling scheme by building an emulator of the peak counts at different cosmologies. The emulator is trained on a suite of PKDGRAV3 N-Body simulations (Potter, Stadel & Teyssier 2017) that we created, dubbed DARKGRIDV1. We measure the cosmological parameters $\sigma_8$ and $\Omega_m$ in the ΛCDM model, as well as the galaxy intrinsic alignment amplitude $A_{IA}$. We do not infer the values of the remaining ΛCDM parameters (baryon density $\Omega_b$, scalar spectral index $n_s$, and dimensionless Hubble parameter $h$) as they are mostly unconstrained by weak lensing measurements, but we take into account their contribution to the measurement uncertainty. Further, we incorporate the effects of photometric redshift uncertainty, shear calibration biases, and the redshift dependence of galaxy intrinsic alignment into the analysis. Stringent scale cuts are applied to ensure that the results are not sensitive to baryon modelling. The design of the analysis, combined with the different sensitivity of peak counts to intrinsic alignment modelling, provides an alternative and complementary measurement to the main cosmic shear analysis of the DES Y3 data (Amon et al. 2021; Secco et al. 2022).

This analysis is done in a blinded way to avoid intentional or unintentional confirmation biases. We formulate a number of criteria that need to be satisfied before unblinding. This work starts by introducing the DES Y3 shape catalogue and the DARKGRIDV1 simulation suite in Section 2. The various systematic effects affecting weak lensing measurements are discussed in Section 3 and their treatment in this study is outlined. Section 4 explains the forward modelling of the DES Y3 mass maps and the derived statistics, which are then compared to the statistics measured from the DES Y3 mass maps. This section also explains the inference pipeline. Section 5 discusses the blinding procedure followed in this work as well as the different unblinding tests that were performed. The inferred cosmological constraints are presented, discussed, and compared to the results of other studies in Section 6. We summarize our findings in Section 7.
Figure 1. Tomographic redshift distributions $n(z)$ of the galaxies in the DES Y3 shape catalogue. The calculation of the tomographic redshift distributions was performed using the SOMPZ method (Myles et al. 2021). The distributions shown are normalized by the number of galaxies in each bin. The distributions span the redshift range $z = 0 - 3$.

2 DATA

2.1 Dark energy survey year 3 shape catalogue

This work uses data from the first three years of data (Y3) of the Dark Energy Survey (DES; The Dark Energy Survey Collaboration 2005; Dark Energy Survey Collaboration 2016). DES is a photometric imaging survey that observed the Southern hemisphere in five optical-NIR broad-bands (grizY) over six years (2013–2019). The processing of the raw images was performed by the DES Data Management (DESDM) team. We refer the reader to Morganson et al. (2018), Dark Energy Survey Collaboration (2018) for a detailed description of the image processing pipeline. In particular, we use the fiducial DES Y3 weak lensing shape catalogue presented in Gatti et al. (2021). The shear measurement pipeline used to create the catalogue is METACALIBRATION (Huff & Mandelbaum 2017; Sheldon & Huff 2017), which allows the self-calibration of the measured shapes against most of the shear and selection multiplicative biases by measuring the mean shear and selection response matrix of the sample. An additional multiplicative calibration (at the level of 2–3 per cent) to correct for detection and blending biases is provided based on image simulations (MacCrann et al. 2020). A number of null tests presented in Gatti et al. (2021) prove the catalogue to be robust against additive biases. The final sample comprises about a hundred million objects, for an effective number density of $n_{\text{eff}} = 5.59$ galaxies arcmin$^{-2}$, spanning an effective area of 4143 deg$^2$. The galaxies of the DES Y3 shape catalogue are further divided into four tomographic bins and redshift estimates for each of the tomographic bins are provided by the SOMPZ method (Myles et al. 2021). We present the normalized, tomographic redshift distributions in Fig. 1.

2.2 N-Body simulation suite DARKGRID1

We rely on an emulator approach to predict the angular power spectra and peak counts at different cosmologies. The emulator is built on numerical predictions of the statistics from simulations. Therefore, we require a suite of simulations spanning the studied cosmological parameter space, namely the $\Omega_m - \sigma_s$ plane. We use the same simulation suite as was used by Z21, but extended with additional simulations; we dub this larger suite DARKGRID1. The simulations sample the $\Omega_m - \sigma_s$ plane at 58 different cosmologies; their distribution is shown in Fig. 2. The simulation grid is centred at the fiducial cosmology inferred by the DES Y1 cosmic shear analysis (Troxel et al. 2018a) (marked by the star in Fig. 2) and the simulations are distributed along lines of approximately constant $\mathcal{S}_s$. Fifty independent full-sky simulations were run for the fiducial cosmology and five simulations for every other cosmology. The simulations at the fiducial cosmology are used to estimate the covariance matrix while the remaining simulations are used to train the emulator (see Section 4).

All simulations were produced using the publicly available code PKDGRAV3 (Potter et al. 2017). This dark-matter-only N-Body code features a full-tree algorithm and a fast multipole expansion, yielding a run-time that increases linearly with the number of particles in the simulation. PKDGRAV3 runs on CPUs and GPUs simultaneously. In each simulation 768$^3$ particles and a unit box with a side-length of 900 Mpc h$^{-1}$ were used. To cover the necessary redshift range up to $z = 3.0$ a large enough cosmological volume must be sampled; hence, the unit box is replicated up to 14 times along each dimension (14$^3$ replicas in total) using periodic boundary conditions. At the fiducial cosmology ten replicas along each dimension are sufficient to achieve the necessary volume. Such a replication scheme is known to underpredict the variance on very large scales (see Fluri et al. (2019) for example). We confirm that our simulations recover the angular power spectrum as predicted from the theory code CLASS (Lesgourgues 2011) on all scales considered in this analysis and beyond (see Appendix E). Nevertheless, we apply a scale cut of $\ell \geq 30$ for the angular power spectra to avoid the inclusion of scales strongly affected by mode-mixing with supersurvey modes that might be underestimated in the simulations.

Apart from the varying $\Omega_m$ and $\sigma_s$ parameters, all remaining cosmological parameters are fixed to the (LCDM, TT, TE, EE+lensing) results of Planck 2018 (Aghanim et al. 2020). This corresponds to a baryon density $\Omega_b = 0.0493$, a scalar spectral index $n_s = 0.9649$, a dark energy equation-of-state parameter $w = -1$, and a dimensionless Hubble parameter of $h = 0.6736$. The dark energy density $\Omega_d$ is adapted for each cosmology to achieve a flat geometry. All simulations include three massive neutrino species with a mass of $m_\nu = 0.02$ eV per species. A degenerate mass hierarchy was adopted. The neutrinos are modelled as a relativistic fluid in the simulations following the treatment described in Tram et al. (2019). This results in a neutrino density of $\Omega_\nu \approx 0.0014$ today.

The particle positions are returned in $\sim$87 particle shells distributed between $z = 3.0$ and $z = 0.0$, using the light-cone mode

\footnote{We define the Hubble constant as $H_0 = 100 \times h \text{ km s}^{-1} \text{ Mpc}^{-1}$.}
of PKDGRAV3. The exact number of shells varies slightly with cosmology as the shells are equally spaced in proper time. The default precision settings of PKDGRAV3 are used and the initial conditions of all simulations are generated at $z = 99.0$.

To model the additional measurement uncertainty from the remaining, unconstrained ΛCDM parameters that are fixed in the main simulation suite ($Ω_m$, $n_s$, and $h$) we require an additional set of simulations. Each of the simulations in this suite varies only one of the mentioned parameters, holding the others fixed to their fiducial values. Each parameter direction is explored using simulations at four different locations distributed around the fiducial parameter values. This results in simulations with

$$Ω_b \in \{0.0453, 0.0473, 0.0513, 0.0533\},$$

$$n_s \in \{0.9249, 0.9449, 0.9849, 1.0249\},$$

$$h \in \{0.6336, 0.6536, 0.6936, 0.7136\}.$$

As for the main simulation grid we run five individual PKDGRAV3 simulations per cosmology. We use the same five initial conditions in all these simulations. We refer the reader to Section 4.5 for the details of the modelling of the influence of these parameters on the summation statistics.

### 3 SYSTEMATIC EFFECTS

The results of cosmic shear studies are influenced by a variety of systematic effects that arise from unaccounted physical effects as well as inaccuracies in the shear estimation process; if not treated, they will bias our outcomes. We therefore take into account the major systematic effects that are known to bias cosmic shear results: shear calibration bias, uncertainties in the redshift distribution estimation of the source galaxies, galaxy intrinsic alignment, and baryonic physics. Additionally, source clustering is known to potentially bias the results inferred using peak counts (see Section 3.5).

We include in the inference process a treatment of the multiplicative shear bias, photometric redshift uncertainty, and galaxy intrinsic alignment. We incorporate the amplitude of the galaxy intrinsic alignment signal $A_{iA}$ as an additional parameter in our analysis due to its strong influence on the outcomes of cosmic shear studies (see e.g. Zürcher et al. 2021). The values of the remaining systematics parameters considered in this work have been found to be largely unconstrained in weak lensing measurements (see e.g. Troxel et al. 2018a). Hence, we model their influence on the summary statistics in a cosmology independent way and marginalize them out over their priors (see Table 1).

We adopt a different strategy to mitigate a second set of potential systematics, namely those due to baryonic physics, source clustering, and additive shear biases: we apply appropriate scale cuts to the statistics to control the induced bias in parameters of interest. In the following, we give an overview of these systematic effects and we describe how they are treated in this study.

#### 3.1 Photometric redshift uncertainty

Surveys aiming at performing cosmological measurements using cosmic shear require the imaging of a large number of galaxies. For such surveys, determining the redshifts of the galaxies using spectroscopy is currently not feasible, and instead the redshifts are measured using photometry. Inaccuracies or catastrophic failures in the redshift measurement can propagate to the redshift distributions of the source galaxies. It was demonstrated that an incorrect redshift distribution can alter the cosmological constraints inferred in cosmic shear studies (see e.g. Hutera et al. 2006; Choi et al. 2016; Hildebrandt et al. 2020). We take the uncertainty of the redshift distributions into account by introducing the nuisance parameters $Δ_{z,i}$ in the analysis. The index $i$ runs over the four tomographic bins. The parameters $Δ_{z,i}$ incorporate the uncertainty of the redshift distributions by describing a shift of the distributions $n_i(z)$ according to

$$n_i(z) = n_i(z - Δ_{z,i}).$$

This method of incorporating the uncertainty of the redshift distributions into the analysis was used in previous studies (see Troxel et al. 2018a, for example) and was demonstrated to be adequate for the DES Y3 shape catalogue (Cordero et al. 2020; Amon et al. 2021). We treat the influence of the nuisance parameters $Δ_{z,i}$ as a second-order effect and neglect its dependence on cosmology. The relative variation (as a function of $Δ_{z,i}$) of $d_i$ (the j-th element of the data vector belonging to tomographic bin i) is denoted $d_{i,j}(Δ_{z,i})$, so that

$$d_i(Ω_m, σ_8, Δ_{z,i}) = d_i(Ω_m, σ_8, Δ_{z,i}) = 0(1 + f_{i,j}(Δ_{z,i})).$$

We model $f_{i,j}$ as a quadratic polynomial:

$$f_{i,j}(Δ_{z,i}) = c_{i,j}^1Δ_{z,i} + c_{i,j}^2Δ_{z,i}^2.$$  

We find a quadratic fit to minimize the error in the cross-validation test while a cubic fit tends to overfit (see Appendix B). The coefficients $c_{i,j}^1$ and $c_{i,j}^2$ are fitted individually for each element of the data vector, based on a set of simulations at the fiducial cosmology in which the $n_i(z)$ has been shifted by $Δ_{z,i}$. The simulations span the range $Δ_{z,i} \in [−0.1, 0.1]$ in nine linearly spaced steps with 200 realizations each that are built from the 50 PKDGRAV3 simulations at the fiducial cosmology (see Section 2.2).

We test that the chosen model is sufficiently accurate (so that its imperfections should not alter the results of the study) using a leave-one-out cross-validation strategy (see Appendix B). The priors used for the individual $Δ_{z,i}$ parameters are listed in Table 1.

#### 3.2 Shear bias

The inference of the cosmic shear field from the observed galaxy shapes requires a detailed understanding of how the intrinsic shapes of the galaxies are altered due to gravitational lensing. The Earth’s atmosphere, the telescope, and the detector itself further alter the observed shapes of the galaxies. Their influence is typically modelled using the point spread function (PSF) (Bernstein & Jarvis 2002b). Furthermore, noise rectification or misspecification of the noise

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Prior</th>
</tr>
</thead>
<tbody>
<tr>
<td>$Ω_m$</td>
<td>$U(0.1, 0.5)$</td>
</tr>
<tr>
<td>$σ_8$</td>
<td>$U(0.3, 1.4)$</td>
</tr>
<tr>
<td>$Ω_b \times 10^2$</td>
<td>$N(4.93, 0.33)$</td>
</tr>
<tr>
<td>$n_s$</td>
<td>$N(0.9649, 0.042)$</td>
</tr>
<tr>
<td>$h$</td>
<td>$N(0.6736, 0.054)$</td>
</tr>
<tr>
<td>$A_{iA}$</td>
<td>$U(−6, 6)$</td>
</tr>
<tr>
<td>$η$</td>
<td>$U(−5, 5)$</td>
</tr>
<tr>
<td>$m_0 \times 10^2$</td>
<td>$N(−0.63, 0.91)$</td>
</tr>
<tr>
<td>$m_2 \times 10^2$</td>
<td>$N(−1.98, 0.78)$</td>
</tr>
<tr>
<td>$m_3 \times 10^2$</td>
<td>$N(−2.41, 0.76)$</td>
</tr>
<tr>
<td>$Δ_{z,1} \times 10^2$</td>
<td>$N(0.0, 1.8)$</td>
</tr>
<tr>
<td>$Δ_{z,2} \times 10^2$</td>
<td>$N(0.0, 1.5)$</td>
</tr>
<tr>
<td>$Δ_{z,3} \times 10^2$</td>
<td>$N(0.0, 1.1)$</td>
</tr>
<tr>
<td>$Δ_{z,4} \times 10^2$</td>
<td>$N(0.0, 1.7)$</td>
</tr>
</tbody>
</table>

Table 1. Priors used throughout this work. $U$ denotes a flat prior with the indicated lower and upper bounds, while $N$ denotes a normal prior with the indicated mean and scale.
The measured shear $\gamma_{\text{obs}}$ of a single galaxy is commonly modelled as being composed of three terms:

$$\gamma_{\text{obs}} = m \gamma + \tilde{c} + \delta \epsilon_{\text{noise}},$$

where $\gamma$ denotes the actual cosmic shear (Heymans et al. 2006; Mandelbaum et al. 2014). The noise component $\delta \epsilon_{\text{noise}}$ is modelled to have zero mean and its contribution to the averaged shear signal $\langle \gamma_{\text{obs}} \rangle$ is expected to vanish ($\langle \delta \epsilon_{\text{noise}} \rangle = 0$), if the average is taken over a large enough number of galaxies. The multiplicative and additive shear biases are denoted as $m$ and $\tilde{c}$, respectively. Both biases can arise from a variety of sources. An error in the estimation of the size of the PSF can introduce a multiplicative bias, whereas an error in the estimation of its ellipticity can contribute to the additive bias. Other sources of bias include selection and detection effects as well as calibration errors in the shear estimation process itself (Kaiser 2000; Bernstein & Jarvis 2002b; Kacprzak et al. 2012; Bernstein et al. 2016; Fenech Conti et al. 2017; Hoekstra, Viola & Herbonnet 2017; Sheldon & Huff 2017).

The DES Y3 METACALIBRATION shape catalogue used in this study underwent extensive testing for shear biases by Gatti et al. (2021). The METACALIBRATION shear estimation method does not account for a potential shear dependence in the detections and blending of sources. Therefore, MacCrann et al. (2020) used image simulations to detect and correct for remaining sources of additive biases. Additionally, Gatti et al. (2021) performed a series of null tests on the catalogue level to investigate known sources of shear biases, such as stellar contamination. A null test using the B-mode signal was performed and an investigation on the correlations between galaxy properties and the shear signal was carried out. Lastly, a set of PSF diagnostics were used to assess the accuracy of the PSF estimation and to model additive biases arising from insufficient PSF modelling. However, Gatti et al. (2021) point out that some small additive biases from PSF mismodelling still remain. While they do not correct the shape catalogue for these biases, they do provide an estimate of their contribution to the galaxy shapes.

Hence, we confirm that the estimated additive shear bias does not change the outcomes of this study (see Appendix C) and we refrain from including an additional treatment of the additive shear bias in the inference process.

On the other hand, we treat the tomographic multiplicative shear biases $m_i$ as nuisance parameters, as even small multiplicative biases are expected to alter the results of cosmic shear studies. The index $i$ denotes the tomographic bin. We treat the multiplicative shear bias as a second-order effect independent of cosmology and use a treatment analogous to that used for the photometric redshift uncertainty (see Section 3.1). The fitting is based on a set of simulations at the fiducial cosmology that span the range $m_i \in [-0.1, 0.1]$ in nine linearly spaced steps with 200 realizations each (based on the 50 PKDGRAV3 simulations at the fiducial cosmology). The multiplicative shear bias is incorporated in the simulations by altering the cosmological convergence signal according to

$$\kappa_{m_i} = (1 + m_i) \kappa_{m_i=0}.$$  

The accuracy of the model is tested in Appendix B and the priors used on the parameters $m_i$ are included in Table 1.

3.3 Galaxy intrinsic alignment

Weak gravitational lensing causes distortions of the shapes of galaxies of $\sim 1$ per cent of the intrinsic ellipticities of the galaxies. Therefore, cosmic shear studies must gain in statistical power by averaging over multiple galaxies in a patch of the sky. Under the assumption that the intrinsic shapes of the galaxies are randomly distributed, the intrinsic shapes average out and the cosmic shear signal becomes measurable.

This assumption does not hold true in reality as the intrinsic ellipticities of galaxies are correlated with each other as well as with the large-scale structure. This effect, which is typically not incorporated in dark-matter-only simulations, is referred to as galaxy intrinsic alignment (IA). The IA signal can be broken down into two components: (1) intrinsic–intrinsic (II), describing the correlation between the ellipticities of the galaxies and the large-scale structure, and (2) gravitational–intrinsic (GI), describing the correlation between the sheared background galaxies and the ellipticities of the foreground galaxies (Heavens, Refregier & Heymans 2000b).

We include a treatment of IA in the inference process as IA is known to potentially bias cosmological parameter constraints inferred in cosmic shear studies if neglected (Heavens et al. 2000b). We use a map-level implementation of the non-linear intrinsic alignment model (NLA), which was first introduced in Fluri et al. (2019), to generate IA signals from the dark matter simulations. We refer the reader to Z21 for the details of the implementation. The NLA model was developed by Hirata & Seljak (2004), Bridle & King (2007), Joachimi et al. (2011), and has three model parameters: $A_{IA}$, the IA amplitude, governs the overall strength of the signal, while $\eta$ and $\beta$ allow a dependence of the IA signal on the galaxy’s redshift and luminosity, respectively. The dependencies are modelled around arbitrary pivot parameters $z_0$ and $L_0$. We include the IA amplitude $A_{IA}$ and $\eta$ as nuisance parameters in our inference pipeline but we neglect the luminosity dependence of the IA signal by setting $\beta = 0$. This parameter choice for the modelling of the IA signal was used previously in Troxel et al. (2018a). The redshift dependence is modelled around the median redshift $z_{\text{med}} \approx 0.6$ of the global redshift distribution of the galaxies in the DES Y3 data.

The influence of $A_{IA}$ on the summary statistics is modelled using simulations and incorporated in the emulator (see Section 4.4). The value of $A_{IA}$ is measured in the inference process. On the other hand, we treat the redshift dependence of the IA signal as a second-order, cosmology-independent effect. The effect of $\eta$ on the data vector level is modelled, analogously to the effect of photometric redshift uncertainty and multiplicative shear bias, using a quadratic polynomial (see Section 3.1). The coefficients are fitted using a set of simulations at the central cosmology that span the range $\eta \in [-5, 5]$ in nine linearly spaced steps with 200 realizations each (based on the 50 PKDGRAV3 simulations at the fiducial cosmology). The amplitude of the IA signal was fixed to $A_{IA} = 1$ in these simulations. The accuracy of the model is tested in Appendix B and the priors used on $A_{IA}$ and $\eta$ are listed in Table 1.

3.4 Baryons

The presence of baryons heavily affects the small-scale fluctuations of the observable Universe. While radiative cooling can lead to a faster collapse of haloes and therefore steeper halo profiles (Yang et al. 2013), feedback effects arising from active galactic nuclei or stellar winds and supernovae can counteract the collapse of structures (Osato, Shirasaki & Yoshida 2015). The individual contributions of the different baryonic effects depend strongly on the mass of the host halo and its redshift as well as the feedback model adopted (McCarthy et al. 2017). The complexity of the modelling of such baryonic physics often restricts the accessibility of small scales in cosmic shear studies. While there exist models such as HMCODE (Mead...
et al. 2015) that include baryonic effects in the theory predictions for the angular power spectra, no such models are currently available for peak counts. In a forward-modelling approach as followed in this work, the baryonic effects would have to be added to the dark-matter-only simulations. Recent, successful approaches to alter dark-matter-only simulations to mimic the effect of baryonic physics include the use of parametric models to change the positions of the simulated particles (Schneider et al. 2019) and the use of deep learning techniques to paint the baryon effects on to the lensing maps as inferred from hydrodynamic simulations (Tröster et al. 2019). The impact of baryons on the peak counts was studied in Weiss et al. (2019), who found that it becomes small for large smoothing scales.

Due to the large uncertainty in the feedback model the inclusion of baryonic effects in the analysis would require the introduction of several additional nuisance parameters, increasing the computational cost of the analysis significantly. Instead, we decided to quantify the impact of baryonic effects on the resulting cosmological parameter constraints using baryon-contaminated mock simulations. We then restrict ourselves to the use of scales that are not significantly biased by baryonic physics. The details of the test and the results are outlined in Appendix F. Based on the results of the test, we restrict ourselves to spherical harmonics with $\ell \leq 578$ for the angular power spectra and to peaks identified on maps that were smoothed with a Gaussian kernel with full-width-at-half-maximum (FWHM) $\geq 7.9$ arcmin, avoiding the need for a full treatment of baryonic effects.

### 3.5 Source clustering

The strength of the lensing signal depends on the arrangement of the source galaxies and the corresponding foreground lenses along the lines of sight. The lensing signal reaches its maximum when the distance between the observer and the lens is equal to the distance between the lens and the source galaxy. Hence, the strength of the lensing signal of a certain lens depends on the redshift distribution of the corresponding source galaxies behind the lens. In order to accurately reproduce the lensing signal measured in the data, the redshift distribution of the source galaxies in the simulations at the position of a lens of a certain strength must match the corresponding distribution in the data.

While we match the global, tomographic redshift distributions of the source galaxies in our simulations with those in the data, we do not take into account the variation of the redshift distributions across the survey region. Such variations can be caused by the varying depth of the survey across the sky, as well as by source clustering and blending.

Source clustering refers to the alteration of the local redshift distribution of the source galaxies at the location of a massive galaxy cluster due to a large number of galaxies residing at the redshift of the cluster.

While source clustering increases the number of galaxies at the redshift of the lens, blending counteracts this effect to some extent, as the increased number of galaxies in the same region of the sky inevitably causes the loss of some galaxies due to overlaps in their light profiles.

Neither blending nor source clustering are reproduced realistically in our simulations; the galaxies in the simulations are located in the same positions as in the DES Y3 shape catalogue and are not correlated with the dark matter density (see Section 4.2). In a non-tomographic analysis or in a case of highly overlapping redshift bins, this can lead to a difference in the $κ$ measurement at positions of clusters, where the shear signal would be diluted by the cluster members, which carry no shear signal associated with the cluster. The effect of source clustering can be accounted for by modifying the signal-to-noise-ratio (SNR) of the detected lensing peaks according to a ‘boost factor’ correction (Mandelbaum et al. 2005). However, in the case of a sufficient separation of sources and lenses, this effect is negligible.

As we use a tomographic analysis in this work and past studies have found blending to be subdominant compared to source clustering, we expect blending to have marginal impact on our results (K16). That is why we only investigate the influence of source clustering in our analysis. To infer the boost factors we follow the approach outlined in appendix C of K16. Using the boost factor corrections, we measure the impact of source clustering on the cosmological constraints inferred using peak counts. We find that source clustering does not constitute a significant source of bias in this survey setup and hence we neglect it in this analysis (see Appendix D).

### 4 METHOD

We infer cosmological constraints from the DES Y3 data using two map-based statistics: angular power spectra and peak counts. To avoid needing analytical predictions for the peak counts we rely on a forward modelling approach. Based on a suite of numerical simulations, we forward-model DES Y3-like mass maps for different cosmologies, conserving the original survey properties (e.g. galaxy number density, shape noise properties, etc.). By measuring the statistics on the simulated mass maps we obtain predictions for the selected cosmologies sampled with simulations. An emulator is used to predict the summary statistics at other cosmologies.

Our analysis closely follows the approach outlined in Z21. In the following, we introduce the mass map simulation procedure, the calculation of the summary statistics, and the inference process, including a description of the emulator, covariance, and likelihood.

We use an updated version of the NGSF⁶ (Non-Gaussian Statistics Framework) software as well as estats⁷ (as introduced in Z21). The complete code base is publicly available to ensure the reproducibility of the presented results.

### 4.1 Mass mapping

The HEALPIX⁸ software (Gorski et al. 2005) is used to produce a pixelized version of the observed shear field $γ_{\text{obs}}$ from the METACALIBRATION shear catalogue described in Section 2.1

$$ γ_{\text{obs}} = \frac{\sum_{j=1}^{N_{\text{pix}}} w_j \epsilon_j \exp(i\phi_j)}{R \sum_{j=1}^{N_{\text{pix}}} w_j}, \tag{6} $$

using a resolution of $\text{NSIDE} = 1024$. The index $j$ runs over all $N_{\text{pix}}$ galaxies in a pixel. The individual galaxies are weighted according to their METACALIBRATION weights $w_j$ and the average METACALIBRATION response of the galaxy catalogue $R$.

The shear field is decomposed into its coefficients $z^2 Y_{\ell m} = z^2 \mathcal{P}_{E,\ell m} + i z^2 \mathcal{P}_{B,\ell m}$ in the basis of spin-2 spherical harmonics $2Y_{\ell m}(\theta, \phi)$ as

$$ \tilde{γ}(\theta, \phi) = \sum_{\ell=0}^{\infty} \sum_{m=-\ell}^{\ell} z^2 \mathcal{P}_{\ell m} Y_{\ell m}(\theta, \phi) \tag{7} $$

using the MAP2LAM routine of HEALPIX.

---

⁶https://cosmo-gitlab.phys.ethz.ch/cosmo_public/NGSF
⁷https://cosmo-gitlab.phys.ethz.ch/cosmo_public/estats
⁸http://healpix.sf.net
We use the spherical Kaiser–Squires (KS) mass mapping method (Kaiser & Squires 1993; Wallis et al. 2022) to produce the DES Y3 mass maps from the pixelized shear fields. The KS routine relates the spherical harmonics coefficients \( \phi^*_{\ell m} = \phi_{E,\ell m} + i \phi_{B,\ell m} \) of the convergence field to the spherical harmonics coefficients \( \tilde{Y}_{\ell m} \) of the shear field via
\[
\phi^*_{\ell m} = D_{\ell}^{-1} \cdot \tilde{Y}_{\ell m},
\]
where the kernel \( D_{\ell} \) is defined as
\[
D_{\ell} = -\frac{1}{\ell (\ell + 1)} \sqrt{\frac{\ell (\ell + 2)!}{(\ell - 2)!}}.
\]
The curl-free (\( \kappa_{E} \)) and divergence-free (\( \kappa_{B} \)) convergence maps are then reconstructed from the spherical harmonics coefficients \( \phi^*_{\ell m} \) using the HEALPIX routine ALM2MAP as
\[
\begin{align*}
\kappa_{E}(\theta, \phi) &= \sum_{\ell=0}^{\infty} \sum_{m=-\ell}^{\ell} \phi_{E,\ell m} \cdot Y_{\ell m}(\theta, \phi), \\
\kappa_{B}(\theta, \phi) &= \sum_{\ell=0}^{\infty} \sum_{m=-\ell}^{\ell} \phi_{B,\ell m} \cdot Y_{\ell m}(\theta, \phi).
\end{align*}
\]

4.2 Mass map simulations

The PKDGRAV3 simulation suite introduced in Section 2.2 is used to predict DES Y3-like mass maps at 58 different cosmologies distributed in the \( \Omega_{m} - \sigma_{8} \) plane. We use the UFalcon\(^9\) software to convert the discrete particle density shells of the PKDGRAV3 simulations into mass maps in the same fashion as Z21. We refer the reader to Sigier et al. (2019) for a complete description of the UFalcon software.

Using the Born approximation, UFalcon avoids relying on a full ray-tracing treatment that would otherwise be necessary to produce the mass maps. Given the distribution \( n(z) \) of source galaxies in redshift space, the projected convergence signal \( \kappa \) in direction \( \vec{n} \) is estimated as
\[
\kappa(\vec{n}) \approx \frac{3}{2} \Omega_{m} \sum_{b} W_{b}(n(z)) \int_{\Delta_{b}} \frac{dz}{E(z)} \delta \left( \frac{c}{H_{0}} D(z) \vec{n}, z \right),
\]
where \( \delta \) indicates the density contrast at redshift \( z \) projected onto the sphere and the shell weights \( W_{b}(n(z)) \) are defined as
\[
W_{b}(n(z)) = \int_{\Delta_{b}} dz \int_{z_{1}}^{z_{2}} dz_{1} \frac{n(z_{1})}{a(z_{1}) E(z_{1})} \frac{D_{\ell m}(z, z_{1}, z_{2})}{D_{\ell m}(z)}.
\]
The particle shells have a finite thickness \( \Delta_{b} \) in redshift space and \( z_{1} = 3.0 \) in our setup. The speed-of-light is denoted as \( c \), the Hubble constant as \( H_{0} \), and the scale factor of the Universe at redshift \( z \) as \( a(z) \). The function \( E(z) \) is defined as
\[
dE = \frac{dz}{E(z)},
\]
with \( D(z_{1}, z_{2}) \) indicating the dimensionless comoving distance between two redshifts \( z_{1} \) and \( z_{2} \).

The use of the Born approximation might introduce some deterioration of the accuracy of the simulated mass maps as compared to a full ray-tracing treatment. Although Petri, Haiman & May (2017) have demonstrated that the bias introduced by such inaccuracies is negligible in the presence of shape noise, even for an LSST-like survey, we test that the angular power spectra of the simulated mass maps agree with predictions from a state-of-the-art theory code (see Appendix E).

In order to realistically reconstruct the properties of the original DES Y3 mass maps, a statistically equivalent shape noise component has to be added to the cosmological convergence signal. We perform the addition of shape noise and cosmological signal in shear space. Hence the cosmological convergence signal \( \kappa \) must first be converted to a shear signal \( \tilde{\gamma} \). We make use of the KS routine again for this purpose (see Section 4.1).

The shape noise signal \( \tilde{\gamma}_{\text{noise}} \) is drawn from the original DES Y3 shear catalogue by rotating the galaxy ellipticities \( \tilde{\eta}_{i} \) in place by a randomly drawn phase \( \phi_{i} \) for each galaxy. The addition of shape noise and the cosmological signal is performed at the pixel level to obtain the total simulated shear signal \( \tilde{\gamma}_{\text{sim}} \):
\[
\tilde{\gamma}_{\text{sim}} = \tilde{\gamma}_{\text{noise}} + \tilde{\gamma} = \sum_{i=1}^{N_{\text{pix}}} w_{i} \tilde{\eta}_{i} \exp(i\phi_{i}) + \tilde{\gamma}.
\]

The individual galaxies are weighted according to their METACALIBRATION weights \( w_{i} \) (note that the average METACALIBRATION response of the sample \( R = 1 \) in the simulations). The final, forward modelled mass \( \kappa_{\text{sim}} \) is then obtained by applying the spherical KS mass mapping method on the \( \tilde{\gamma}_{\text{sim}} \) map. The pixelization of the sphere was again performed using the HEALPIX software with a resolution of \( \text{NSIDE} = 1024 \). The mass maps simulated by this procedure contain a statistically equivalent shape noise component and have the same survey mask as the original DES Y3 mass maps. Hence, we do not require to correct the predicted mass map statistics for masking or mode mixing effects in our analysis as these are forward modelled and included in the predictions. A visual comparison of such a simulated mass map to the DES Y3 mass map is shown in Fig. 3.

To optimally use the full-sky simulations we rotate the DES Y3 galaxy coordinates on the sky in order to produce four independent simulations of the survey from a single simulation in DARKGRIDV1. As demonstrated in Appendix E, these rotations leave the angular power spectra of the maps unaffected.

4.3 Summary statistics

Two-point summary statistics, such as the angular power spectra, are sufficient statistics in the case of a homogeneous, isotropic Gaussian random field with zero mean. This assumption is violated for mass maps due to the non-linear nature of gravitational collapse at late times leading to the maps becoming non-Gaussian. It has been found that additional statistics, such as peak counts, ought to be considered in order to fully describe the mass maps (Petri et al. 2014). In this work, we extract information from the mass maps using two statistics: the angular power spectrum and peak counts. In the following, we introduce the theoretical background of the two statistics and describe how we measure them from the mass maps in this analysis.

4.3.1 Angular power spectrum

Two-point statistics have been well studied and have been used extensively and successfully to extract cosmological information from mass maps in weak lensing surveys (see Heymans et al. 2013; Hildebrandt et al. 2017; Troxel et al. 2018a; Hikage et al. 2019; Amon et al. 2021; Heymans et al. 2021; Secco et al. 2022, for example). One of their main advantages is that they can be well modelled from the accurately predictable power spectrum using the Limber approximation (Limber 1953). It was found that

\(9\)https://cosmology.ethz.ch/research/software-lab/UFalcon.html

\textbf{MNRAS 511, 2075–2104 (2022)}
Figure 3. Comparison of the non-tomographic DES Y3 mass map and a simulated mass map from DARKGRIDV1, produced using PKDGRAV3 and following the procedure outlined in Section 4.2. The maps were smoothed using a Gaussian smoothing kernel with a full-width-at-half-maximum (FWHM) of 60 and 10 arcmin for the full and the zoomed in maps, respectively.

Gravitational lensing does not produce any B-modes ($C_\ell^B$), but systematic effects, arising for example from imperfections in the shear-calibration process or selection biases, can do so. Hence, B-modes are often used to test for unaccounted systematic effects in weak lensing studies (see for example Zuntz et al. 2018 or Gatti et al. 2021). We perform a null test on the B-mode signal as part of our unblinding procedure in Section 5. The angular power spectra are measured in 32 square-root-spaced bins between $\ell = 8$ and $\ell = 2048$. However, not all bins are used in the inference procedure (see Section 5). We measure the angular power spectra from the mass maps using the anafast routine of the healpy software (Zonca et al. 2019).

4.3.2 Peak counts

Massive structures of the local Universe such as dark matter haloes get imprinted on mass maps as local maxima, known as peaks. The study of peaks provides a way to extract information from such
highly non-linear structures that is largely complementary to the information captured by two-point statistics (Tyson, Valdes & Wenk 1990; Miralda-Escude 1991; Kaiser & Squires 1993; Yang et al. 2011). A straightforward way to use peaks for cosmological inference is to measure the number of peaks of a mass map. The term peak function has emerged in recent literature for such a record of the number of peaks as a function of either the signal-to-noise ratio \( SNR = \kappa\sigma_e \) or the convergence \( \kappa \) of the peaks. Here, \( \sigma_e \) denotes the standard deviation of the mass map. We choose to bin the detected peaks as a function of \( \kappa \) as this binning has been demonstrated to carry a stronger cosmological signal due to the self-similarity of the peak functions at different cosmologies in the SNR binning scheme (Z21). The peak function is divided into 15 equally spaced bins. In order to suppress the contribution from shot noise and obtain an approximately Gaussian likelihood the ranges of the outermost bins were chosen such that at least 30 peaks are recorded in each bin, independent of cosmology. We restrict ourselves to peaks with SNR \( \leq 4 \), as it is known from past studies that peaks with an SNR \( > 4 \) are strongly affected by source clustering, leading to biased results (K16; Harnois-Déraps et al. 2021).

There are different ways to detect peaks on weak lensing mass maps. Some studies record peaks as local maxima on aperture-mass maps (see for example K16; Harnois-Déraps et al. 2021; Martinet et al. 2021). However, such optimized aperture mass filters only work under a flat-sky approximation. Instead, we detect peaks as local maxima on spherical mass maps directly. We measure peaks on maps smoothed with Gaussian filters of different scales. We use 12 such filters with a full-width-at-half-maximum (FWHM) ranging from 2.6 to 31.6 arcmin resulting in 12 peak functions per tomographic bin. We use the same selection of smoothing scales as Fluri et al. (2018b), who showed that the inclusion of more scales does not further improve the cosmological constraints. Similarly, as for the angular power spectra, not all of the scales were used in the inference procedure (see Section 5). We regard a pixel of the smoothed mass maps as a peak if its convergence value is higher than the value of its nearest neighbour pixels.

We detect peaks separately on each one of the tomographic convergence maps \( \kappa_i(\theta, \phi) \), where the index \( i \) indicates the tomographic bin number. These maps can be written in the basis of the spin-0 spherical harmonics \( Y_{\ell m}(\theta, \phi) \) as

\[
\kappa_i(\theta, \phi) = \sum_{\ell=0}^{\ell_{\text{max}}} \sum_{m=-\ell}^{\ell} \hat{\kappa}_{i,\ell m} Y_{\ell m}(\theta, \phi),
\]

where the upper limit \( \ell_{\text{max}} \) is dictated by the pixel resolution of the maps (\( \ell_{\text{max}} = 3072 \) in our case).\(^{10}\) The inclusion of peaks detected from maps constructed using multiple tomographic bins (hereafter called ‘cross-peaks’) was demonstrated to provide additional information beyond using solely ‘autopeaks’ by Martinet et al. (2020), Harnois-Déraps et al. (2021). In this work, we explore the potential of cross-peaks, identified on spherical, convolved convergence maps \( \kappa_{ij}(\theta, \phi) \)

\[
\kappa_{ij}(\theta, \phi) = \sum_{\ell=0}^{\ell_{\text{max}}} \sum_{m=-\ell}^{\ell} \hat{\kappa}_{i,\ell m} \hat{\kappa}_{j,\ell m} Y_{\ell m}(\theta, \phi),
\]

where the indices \( i \) and \( j \) indicate the two different tomographic bins. We apply the same set of Gaussian filters to the convolved convergence maps before peak detection, as we do for the autopeaks. We include cross-peaks in the fiducial setup of this analysis.

Further information beyond the peak function can be extracted by including other peak-based statistics that are not used in this study such as for example the density profiles around mass map peaks (Marian et al. 2013) or the clustering of peaks Marian et al. (2013), Davies et al. (2021).

4.4 Emulator

We require a means to predict the angular power spectra and the peak counts for different cosmologies as well as different configurations of nuisance parameters. As galaxy intrinsic alignment is strongly degenerate with cosmology, we model the amplitude of the intrinsic alignment signal \( A_{IA} \) as being dependent on the cosmological parameters \( \Omega_m \) and \( \sigma_8 \). The influence of the remaining nuisance parameters on the statistics are treated as second-order effects and are modelled as being independent of cosmology to first order (see Section 3). We train a Gaussian Process Regression (GPR) emulator to predict the values of the statistics for different inputs of \( \Omega_m \), \( \sigma_8 \), and \( A_{IA} \) (see e.g. Quinonero-Candela & Rasmussen 2005).

The training of the GPR emulator is based on simulations at 58 different locations in the \( \Omega_m - \sigma_8 \) space. At each parameter point nine different setups are used with \( A_{IA} \) varying from \(-6 \) to \( 6 \) (linearly spaced). This results in the full parameter space \( \Omega_m - \sigma_8 - A_{IA} \) being sampled in 522 different parameter locations.

A map-based implementation of the non-linear intrinsic alignment model (NLA) is used to generate \( A_{IA} \neq 0 \) simulations from the DARKGRIDS1 to sample the remaining parameter space (see Section 3.3). As each point in the parameter space is sampled using five independent simulations and subsequently four survey rotations are applied (see Section 4.2), \( 522 \times 5 \times 4 = 10,440 \) truly independent simulations are generated. Additionally, ten shape-noise realizations are produced per simulation. We note that this leads to simulations that are only pseudo-independent. While the noise signal is different for each simulation, some simulations contain the same cosmological signal (we discuss the implications of this in Section 4.7). The resulting 104 400 simulations are used to predict the mean values of the statistics at the 522 locations of the parameter space. The GPR emulator is then trained using these predictions.

We use the GPR implementation GaussianProcessRegressor of scikit-learn (Pedregosa et al. 2011) and a radial-based function (RBF) kernel. The length scale is optimized prior to training to minimize fitting errors. A different GPR emulator is trained individually for each element of the data vectors.

We report on the accuracy of the emulator in Fig. B1 in Appendix B. The accuracy of the emulator was tested using a ‘leave-one-out’ cross-validation strategy. We conclude that the emulator is sufficiently accurate that its imperfections will not alter the results of this study significantly.

The predicted angular power spectra and peak counts for different values of \( S_8 \) are presented in Fig. 4 and Fig. 5, respectively. The predictions are compared to the angular power spectra and peak counts measured from the DES Y3 mass maps.

4.5 Approximate marginalization over remaining ΛCDM parameters

While past studies have found that weak lensing measurements can put tight constraints on a combination of \( \Omega_m \) and \( \sigma_8 \) they also showed
that the remaining ΛCDM parameters are largely unconstrained by weak lensing data (see Troxel et al. 2018a for example). Hence, we refrain from measuring the remaining ΛCDM parameters (Ω_b, n_s, and h) in this analysis. Instead, we model their influence on the summary statistics in a similar fashion as for the photometric redshift uncertainty, multiplicative shear bias, and redshift dependence of the galaxy intrinsic alignment signal.

We model the dependence of the summary statistics on the individual parameters at the DARKGRID fiducial cosmology. Following the same strategy as for the emulation of the systematic effects (see equations 2 and 3), for each parameter θ ∈ \{Ω_b, n_s, h\} and each data vector element j, we define f_j(θ) to be the relative variation in d_j as a function of θ, so that

\[
d_j(\Omega_m, \sigma_8, \theta) = d_j(\Omega_m, \sigma_8)(1 + f_j(\theta)).
\]

We then model f_j(θ) as a quadratic polynomial:

\[
f_j(\theta) = c_j^1(\theta - \theta_{\text{fiducial}}) + c_j^2(\theta - \theta_{\text{fiducial}})^2,
\]

where \(\theta_{\text{fiducial}}\) indicates the Planck 2018 (Aghanim et al. 2020) value of the parameter in question. Note that this treatment can be understood to be an expansion of the likelihood function in the parameters \(\Omega_b, n_s,\) and \(h\) around their fiducial values. Hence, the parameters \(\Omega_b, n_s,\) and \(h\) are treated as nuisance parameters in the inference process and are marginalized out over their priors. As
Figure 5. Comparison between the predicted peak counts at different \( S_8 \) (coloured curves) and the peak counts measured from the DES Y3 mass maps (black data points). The error bars indicate the standard deviation estimated from the simulations at the fiducial cosmology. For the sake of presentation, the number of random peaks, estimated from noise-only simulations, were subtracted. For brevity, we only present the results for a filter scale of FWHM = 21.1 arcmin. The best-fitting simulation to the data yields a global \( \chi^2/dof = 1.13 \) and a \( p \)-value of \( p = 34 \) per cent and is shown as a black curve in each panel.

the parameters \( \Omega_0 \), \( n_s \), and \( h \) are fixed to the values found in the Planck 2018 (Aghanim et al. 2020) study in all simulations used to train the GPR emulator, we choose normal priors centred at these values. The widths of the priors are chosen as ten times the width of the Planck 2018 (Aghanim et al. 2020) posteriors, primarily to account for the additional uncertainty on the \( h \) parameter due to the tension between early and late Universe measurements. The priors used are listed in Table 1. We confirm that the chosen marginalization scheme does not bias our results by running a set of tests in which the values of \( \Omega_0 \), \( n_s \), and \( h \) were fixed to their fiducial values (see Table 2). Furthermore, we test that the chosen marginalization scheme does not exhibit a significant dependence on cosmology (see Appendix H).

We do not constrain parameters outside of the \( \Lambda \)CDM model in this study and we leave that to future work. However, we mention that Harnois-Déraps et al. (2021) found that the additional non-Gaussian information extracted using peak counts can help us to constrain the dark energy equation of state parameter \( w \). Especially, cross-peaks are expected to greatly improve such constraints (Martinet et al. 2021).

Counts of peaks with a high SNR \( \gtrsim 4 \) have also been identified as a powerful means to constrain the sum of neutrino masses (Li...
et al. 2019; Ajani et al. 2020). While we do not infer the sum of neutrino masses in this study, we are potentially biased by a sum of neutrino masses that is different from $\sum m_\nu = 0.06$ eV as adopted in the simulations. Feng et al. (2019) found that in a Stage-3-like weak lensing survey setup only peaks with an SNR > 3.5 are significantly affected by changes in the sum of neutrino masses and that effects from baryonic physics dominate otherwise. As we have already chosen scale cuts that mitigate the effects from baryonic physics and most of the cosmological constraining power is obtained from peaks with low or medium SNR we apply no additional cuts to accommodate for this effect.

4.6 Covariance matrix
A stable estimate of the covariance matrix is needed to accurately infer cosmological parameters. We use a set of $N_\text{c} = 10 000$ pseudo-independent, simulated realizations $\hat{X}_i$ of the summary statistics at the central cosmology ($\Omega_m = 0.26$, $\sigma_8 = 0.84$) to robustly estimate the covariance matrix $\Sigma$ according to

$$\hat{\Sigma} = \frac{1}{N_\text{c} - 1} \sum_{i=1}^{N_\text{c}} (\hat{X}_i - \hat{X}) (\hat{X}_i - \hat{X})^T,$$

(21)

where $\hat{X}$ is the estimated mean data vector at the fiducial cosmology. The 10 000 simulations are generated from 50 independent simulations. Four survey rotations as well as 50 shape noise realizations are used per simulation, yielding the final 10 000 simulations that are used to estimate $\Sigma$. Fig. 6 shows the combined, tomographic correlation matrix $C_{\ell \ell'}$ of the angular power spectra and peak counts. The ordering of the tomographic bin combinations for the angular power spectra and peak counts is from left to right 1x1, 1x2, 2x2, 1x3, 3x3, 1x4, 1x4, 3x4, and 4x4. For each power spectrum all 32 bins ranging from $\ell = 8$ to $\ell = 2048$ are shown. For each tomographic bin combination the peak counts are visualized for all scales 31.6, 29.0, 26.4, 23.7, 21.1, 18.5, 15.8, 13.2, 10.5, 7.9, 5.3, and 2.6 arcmin from left to right. The correlation matrix is estimated based on 10 000 simulations at the central cosmology ($\Omega_m = 0.26$, $\sigma_8 = 0.84$). We note that not all data vector bins shown here are used in the inference (see Section 5).
relation matrix \( C_{ij} \equiv \Sigma_{ij} / \sqrt{\Sigma_{ii} \Sigma_{jj}} \) including all angular power spectra and peak counts at all scales.

We find similarly positive correlations between peaks identified on different scales and using different redshift bins as in past studies (see Z21 for example). Further, we observe that the cross-peaks are only mildly correlated with the autopeaks indicating that they indeed probe a different kind of information. However, we also find some strong correlations between different cross-peaks similarly as in Harnois-Dérap et al. (2021).

The covariance matrix has two major constituents; (1) A highly correlated shape-noise component originating from the uncertainty of the intrinsic shapes of the source galaxies as well as measurement noise, and (2) a cosmic variance term accounting for the randomness in the cosmic matter density field itself.

We compare the angular power spectrum part of our estimated covariance matrix to the covariance matrix used in Doux & DES Collaboration (in preparation). While we estimate our covariance matrix from simulations, Doux & DES Collaboration (in preparation) use an analytical covariance matrix. They calculate the Gaussian part of the covariance matrix with NaMaster (Alonso et al. 2019). The non-Gaussian part is computed using the CosmoLike software (Eifler et al. 2014; Krause & Eifler 2017), taking into account supersample covariance and the contribution from the connected four-point covariance originating from the shear field trispectrum. We find that the two covariance matrices agree very well, despite the differences in the two approaches (see Doux & DES Collaboration, in preparation for details). The agreement further strengthens our belief in the accuracy of the simulations and the used methodology. Since the analytical covariance matrix includes an accurate estimate of the supersample covariance the agreement especially alleviates prior concerns about the underestimation of such supersurvey modes in the FKDGRAV simulations (see Section 2.2).

4.7 Data compression

As we estimate the covariance matrix from a finite number of data vector realizations the resulting covariance matrix is noisy. To reduce the noise we apply data compression in order to shorten the length of the data vectors prior to the computation of the covariance matrix. We compress the data vectors using the MOPED data compression algorithm (Tegmark, Taylor & Heavens 1997; Heavens, Jimenez & Lahav 2000a; Gualdi et al. 2018). We implement the MOPED compression following the algorithm described in Gatti et al. (2020). The algorithm yields a compression matrix that reduces the length of the original data vectors to the number of model parameters that are inferred in the analysis (15 in our case). The calculation of the MOPED compression matrix follows a Karhunen-Loève algorithm as in Heavens et al. (2000a) and Gatti et al. (2020). The \( i \)-th component of the compressed data vector \( \tilde{X}^{\text{comp}} \) is calculated from the uncompressed data vector \( \tilde{X} \)

\[
\tilde{x}^{\text{comp}}_i = \frac{\partial \tilde{X}}{\partial p_i} \sum^{-1} \tilde{X},
\]

where \( p_i \) denotes the \( i \)-th model parameter. The partial derivatives \( \frac{\partial \tilde{X}}{\partial p_i} \) are calculated analytically using the GPR emulator.

The MOPED compression algorithm requires an estimate of the precision matrix \( \Sigma^{-1} \) in the original data space. We use the 10 000 pseudo-independent simulations at the fiducial cosmology to estimate this precision matrix. Out of these 10 000 simulations only 200 of them are truly independent (see Section 4.6). This might raise the concern that the contribution from cosmic variance might be underestimated since only 200 different cosmological signals are used in the estimate. However, said precision matrix is only used to calculate the MOPED compression matrix. A potential bias caused by an imperfect compression due to an underestimation of the cosmic variance is alleviated by a simultaneous broadening of the parameter constraints. For the estimation of the precision matrix in the MOPED space only the 200 truly independent realizations at the fiducial cosmology are used.

4.8 Likelihood

We model the likelihood as Gaussian assuming a Gaussian noise model. This assumption is approximately justified by the central limit theorem and by choosing the bins of the peak functions such that for each cosmology at least 30 peaks are recorded in each bin. However, as we do not predict the covariance matrix analytically but rather estimate it from simulations, the intrinsic uncertainty of the covariance matrix itself needs to be incorporated in the likelihood function as well. According to Sellentin & Heavens (2015) the resulting likelihood is no longer Gaussian but instead is a modified version of a multivariate \( t \)-distribution. Furthermore, the additional uncertainty due to the estimation of the statistics at different cosmologies must be taken into account, leading to an additional correction of the likelihood (Jeffrey & Abdalla 2019). Given a location \( \pi \) in parameter space, the probability of observing the data vector \( \tilde{X} \) reads

\[
L(\tilde{X}|\pi) \propto \left(1 + \frac{N_\pi}{(N_\pi + 1)(N_\pi - 1)} Q\right)^{-N_\pi/2},
\]

with

\[
Q = (\tilde{X} - \hat{X}(\pi))^T \Sigma^{-1} (\tilde{X} - \hat{X}(\pi)).
\]

Here, \( \hat{X}(\pi) \) denotes the prediction of the data vector at location \( \pi \). The prediction of \( \hat{X}(\pi) \) is based on at least 200 simulations depending on \( \pi \) \( (N_\pi \geq 200) \). \( N_\pi \) denotes the number of simulations used to estimate the covariance matrix in the MOPED space \( (N_\pi = 200) \).

We efficiently sample the parameter space using the Markov Chain Monte Carlo (MCMC) sampler emcee (Daniel et al. 2013). All constraints presented in this work were generated using 60 walkers with an individual chain length of 200 000 samples. We follow the suggestions in the emcee documentation and use the integrated autocorrelation times of the individual chains as a measure of convergence of the chains. Following the emcee documentation, we confirm that the chains are long enough to obtain a stable estimate of the integrated autocorrelation times. We regard all chains used in this study as converged. The priors used throughout the analysis are listed in Table 1.

5 BLINDING

In order to avoid intentional or unintentional confirmation biases as well as fine tuning of the data by the experimenters, we followed a strict two-stage blinding scheme throughout the analysis.

5.1 Stage 1

We built the analysis framework using a blinded shape catalogue. The catalogue was blinded according to the scheme used in Zuntz et al. (2018) and Gatti et al. (2021). The ellipticities \( \epsilon \) of the galaxies in the catalogue were transformed as \( |\eta| \equiv 2 \text{arctanh}|\epsilon| \to f(|\eta|) \).
using a fixed but unknown $0.9 < f < 1.1$. This transformation preserves the confinement of the ellipticities to the unit disc, while rescaling all inferred shear values. Hence, the transformation leaves the performance of systematic tests intact, while changing the results of the analysis (Zuntz et al. 2018). Using the blinded catalogue the analysis pipeline was developed and tested. In order to continue to stage 2 the following criteria had to be met:

(i) The angular power spectra calculated from the simulated full sky mass maps have to agree with the predictions from theory. Similarly, the angular power spectra measured from the partial-sky, fully forward-modelled mass maps have to agree with the theory predictions. We use a pseudo-$C_\ell$ approach to incorporate the masking effects into the theory predictions (Hikage et al. 2011). The tests are described in Appendix E.

(ii) The accuracy of the GPR emulator as well as the polynomial models used to emulate the second-order systematic effects has to be sufficient. We follow a ‘leave-one-out’ cross-validation strategy in the tests, which are outlined in more detail in Appendix B.

(iii) Using synthetic data vector realizations, the analysis pipeline has to be able to recover the input cosmology within the uncertainty bounds.

5.2 Stage 2

After the criteria defined in stage 1 were met, the shape catalogue was unblinded to perform a series of systematic tests, without unblinding the E-mode data vectors used for cosmological inference nor the cosmological constraints themselves. It was investigated how the cosmological constraints react to contamination by systematic effects that are not included in the analysis. The tested effects include:

(i) Additive shear biases (see Appendix C)
(ii) Baryonic physics (see Appendix F)
(iii) Source clustering (see Appendix D).

The details of the tests appear in the corresponding appendices. Contamination due to source clustering or an additive shear bias component did not lead to a significant shift of the cosmological constraints. No additional scale cuts were imposed based on these tests. However, neglecting the impact of baryonic physics caused a significant shift of the $\Omega_m - S_8$ constraints. Hence, as we do not model the impact of baryons in this study, we restrict ourselves to scales that are only mildly affected by baryonic physics. This led to the decision to exclude multipoles $\ell > 578$ in the angular power spectra and peaks identified on maps smoothed with a Gaussian kernel with FWHM $< 7.9$ arcmin. After these scale cuts, we estimate the shift of the cosmological constraints due to the un-modelled baryonic physics to be smaller than 0.3σ (see Appendix F). The imposed threshold of 0.3σ is in accordance with the unblinding criteria defined in appendix D of Dark Energy Survey Collaboration (2021).

Additionally, a B-mode null test was performed. We compare the measured DES Y3 B-mode signal to a pure shape noise signal that we estimate from simulations without the addition of a cosmological signal. As gravitational lensing does not produce any B-modes, the signals are expected to match. A disagreement would point towards a remaining contamination of the data by some unaccounted systematic effect. We present the noise-subtracted B-mode signals of the angular power spectra and the peak counts in Appendix G. Following the unblinding criteria defined in Appendix D of Dark Energy Survey Collaboration (2021) we find the B-mode null test to be passed.

The DES Y3 shape catalogue used in this study underwent extensive testing by Gatti et al. (2021). We conducted further systematic tests (baryonic physics, source clustering, and additive shear bias), as well as map-level null B-mode tests using angular power spectra and peak counts. However, unknown or un-modelled systematic effects can further bias our results. We test for such unaccounted systematic effects by performing a set of blinded robustness tests leaving out a different subset of the data vector each time. More specifically, we test for a scale-dependent systematic effect by splitting the data vectors into a small-scale and a large-scale sample. For the angular power spectra and the peak counts the small-scale samples contain $\ell \in [258, 578]$ and FWHM $\in [7.9, 18.5]$ arcmin, respectively, while the large-scale samples contain $\ell \in [30, 257]$ and FWHM $\in [21.1, 31.6]$ arcmin, respectively. Further, we test for an unaccounted redshift-dependent systematic effect by leaving out all data vector elements involving a certain tomographic bin at a time. None of the alterations led to a significant shift of the constraints.

Lastly, before unblinding the E-mode data vectors and constraints, we performed a ‘goodness-of-fit’ test to check if the complexity of our model is able to reproduce the data sufficiently well. The best-fitting model was chosen as the prediction of the emulator that yields the maximum posterior given the data. The best-fitting models are included in Fig. 4 and Fig. 5 alongside the predictions from simulations for different cosmologies. For the angular power spectra we find $\chi^2/\text{dof} = 1.49$ and $p = 17$ per cent while for the peak counts we find $\chi^2/\text{dof} = 1.13$ and $p = 34$ per cent, passing the imposed requirement of $p = 1$ per cent, that was chosen in accordance with the unblinding criteria defined in Appendix D of Dark Energy Survey Collaboration (2021).

6 COSMOLOGICAL CONSTRAINTS

In this work, we use angular power spectra and peak counts to constrain the matter density $\Omega_m$ and the amplitude of density fluctuations $\sigma_8$ of the Universe, as well as the structure growth parameter $S_8 \equiv \sigma_8 \sqrt{\Omega_m/0.3}$. As the remaining $\Lambda$CDM parameters ($\Omega_b$, $n_s$, and $h$) are mostly unconstrained by weak lensing data, we take the additional uncertainty into account by treating them as nuisance parameters and marginalizing them out over their priors (see Section 4.5). Further, we take into account the major systematic effects known to bias weak lensing studies: photometric redshift uncertainty, multiplicative shear bias, and galaxy intrinsic alignment (see Section 3).

In this section, we present our fiducial cosmological parameter constraints and our findings regarding galaxy intrinsic alignment. Furthermore, we discuss the outcomes of a range of internal consistency tests that we performed and we compare our findings to the results found in other studies that make use of the DES Y3 data as well as external data sets.

In the following, the numerical 1D posteriors of the parameters are presented as the median parameter values as well as their projected 68 per cent confidence region. A complete record of the numerical results of this study can be found in Table 2 and a visual comparison of the constraints on $S_8$ is presented in Fig. 10.

6.1 Fiducial results

We selected the fiducial data vector configurations for the angular power spectra and peak counts based on the results of previous studies, as well as the tests described in Section 5. While we measured the angular power spectra in 32 square-root-spaced bins between $\ell = 8$ and $\ell = 2048$ we do not use all scales in the analysis; instead, we decided to only use the scales $\ell \in [30, 578]$. The lower scale cut $\ell \geq 30$ is driven primarily by the decision to exclude scales that might
be affected by mixing with supersurvey modes (see Section 2.2). The upper scale cut $\ell \leq 578$ is imposed to stay unbiased to baryonic physics (see Section F). In order to be sensitive to peaks of different spatial extent, the mass maps are smoothed with a set of Gaussian kernels prior to identifying the peaks. Initially 12 such kernels were used, with FWHM = [31.6, 29.0, 26.4, 23.7, 21.1, 18.5, 15.8, 13.2, 10.5, 7.9, 5.3, 2.6] arcmin. Again, a scale cut is applied in order to avoid biases from baryonic physics. Hence, we restrict ourselves to using peaks identified on maps that were smoothed with a Gaussian kernel with an FWHM $\geq 7.9$ arcmin (see Section F).

We present our fiducial constraints on the cosmological parameters $\Omega_m$, $\sigma_8$ and $S_8$ in the left-hand plot in Fig. 7. For completeness, we include the corresponding constraints of the full cosmological parameter space in Appendix A. Using solely angular power spectra we find

$$\begin{align*}
\Omega_m &= 0.278^{+0.008}_{-0.011} \\
\sigma_8 &= 0.85^{+0.11}_{-0.18} \\
S_8 &= 0.783^{+0.026}_{-0.019} \text{ (precision 2.9 per cent)},
\end{align*}$$

while the peaks analysis yields

$$\begin{align*}
\Omega_m &= 0.252^{+0.030}_{-0.060} \\
\sigma_8 &= 0.867^{+0.10}_{-0.068} \\
S_8 &= 0.780 \pm 0.016 \text{ (precision 2.1 per cent)}.
\end{align*}$$

We note that the results obtained using the two different summary statistics are well in agreement with each other, without tensions in any of the parameters. Furthermore, we note that the peaks analysis yields tighter constraints on all studied parameters as expected from past studies (see e.g. Z21; Harnois-Dérap et al. 2021), with the $S_8$ constraint tightening up by 29 per cent over the angular power spectra analysis. This is different from past studies like K16 where peaks and 2-point statistics led to similar constraints. We attribute this primarily to the inclusion of the additional cross-tomographic information in the peak counts.

We also observe a mild breaking of the $\Omega_m - \sigma_8$ degeneracy due to the non-Gaussian information extracted using the peak counts. The degeneracy breaking is not as pronounced as in past studies due to the scale cut of FWHM $\geq 7.9$ arcmin. Another way to help us to break the $\Omega_m - \sigma_8$ degeneracy is the addition of small-scale shear ratios (Sánchez et al. 2021) as demonstrated in Amon et al. (2021), Secco et al. (2022), and Gatti (2021). However, we do not include shear ratios in this study.

The combination of angular power spectra and peak counts yields

$$\begin{align*}
\Omega_m &= 0.276^{+0.034}_{-0.086} \\
\sigma_8 &= 0.850^{+0.13}_{-0.068} \\
S_8 &= 0.797^{+0.015}_{-0.013} \text{ (precision 1.8 per cent),}
\end{align*}$$

leading to a further improvement of the $S_8$ constraint by 13 per cent over the peaks-only analysis. We find a shift of 1 $\sigma$ towards larger $S_8$ values. We attribute this to a strong break of the $S_8$ constraint by the combination of the two summary statistics. This effect is discussed in more detail in Section 6.2.

### 6.2 Constraints on galaxy intrinsic alignment

Galaxy intrinsic alignment is one of the major systematic effects driving the uncertainty of the cosmological parameter constraints in cosmic shear analyses and is known to potentially bias the cosmological parameter constraints if unaccounted for (Heavens et al. 2000b). We present, in the right-hand plot in Fig. 7, the constraints found on the amplitude of the intrinsic alignment signal $A_{IA}$ and its correlation with the inferred cosmological parameters. We find a strong correlation between $S_8$ and $A_{IA}$ for both summary statistics with lower $A_{IA}$ values leading to lower $S_8$ values. While both summary statistics find an $A_{IA}$ constraint consistent with zero, the angular power spectra analysis prefers values lower than the peaks analysis ($A_{IA} = -0.72^{+0.72}_{-0.39}$ for angular power spectra and $A_{IA} = 0.11^{+0.22}_{-0.49}$ for peaks). We find a tight constraint of $A_{IA} = -0.03 \pm 0.23$ and we observe the hoped-for breaking of the $S_8$.
$A_{1a}$ degeneracy when the two summary statistics are combined. As can be seen from the right-hand plot in Fig. 7 this also leads to a shift of 1σ of the $S_8$ constraint towards larger values when compared to the peaks-only case.

Furthermore, we find that the additional tomographic information obtained with the cross-tomographic peaks strongly contributes to constraining $A_{1a}$, tightening the $A_{1a}$ constraints by 43 per cent over the autopeaks only case. Nevertheless, a similar break of the $S_8$ – $A_{1a}$ degeneracy can also be observed when the angular power spectra and autopeaks are combined, but with the angular power spectra dominating the $A_{1a}$ constraints. In this case a lower value of $A_{1a} = -0.28_{-0.18}^{+0.32}$ is obtained due to the dominance of the angular power spectra.

While the observed breaking of the $S_8$ – $A_{1a}$ degeneracy provides a promising way for future weak lensing analyses to improve the robustness of cosmological parameter constraints with respect to galaxy intrinsic alignment, we note that we used a rather simple galaxy intrinsic alignment model in this analysis. It is left to future studies to investigate if this holds true when more realistic galaxy intrinsic alignment models, such as the Tidal Alignment and Tidal Torquing model (TATT; Blazek et al. 2019), are used.

6.3 Internal consistency checks

A suite of blinded consistency tests using alternative data vector configurations were performed to test for unaccounted systematic effects as discussed in Section 5. We repeat these tests after unblinding to assess the internal consistency of the data. The resulting parameter constraints are included in Table 2.

6.3.1 Tomographic bins

We obtain cosmological constraints leaving out subsets of the data vector that are associated with a certain tomographic bin. The results in the $\Omega_m$ – $S_8$ plane are presented in the left-hand plot of Fig. 8.

With tomographic bins 1 and 2 contributing little to the overall constraining power, their removal from the data vector has little impact on the results. On the other hand, we find that removing either the contributions from bin 3 or bin 4 leads to a shift towards smaller $S_8$ values by over 1σ while increasing the uncertainty by $\sim 50$ percent. The shift in $S_8$ can be explained by the significantly increased uncertainty on $\Omega_m$. As most of the constraining power on $\Omega_m$ is gained from bins 3 and 4, their removal from the data vector allows for larger $\Omega_m$ values to become acceptable, which leads to the observed shift in $S_8$. This effect is illustrated in Fig. 8. While our findings are similar to the trends observed in Amon et al. (2021) the shift in $S_8$ is larger in our case if either bin 3 or bin 4 are removed. We attribute this to the additional small scale information from shear ratios that is included by Amon et al. (2021), which disfavors large $\Omega_m$ values.

6.3.2 Angular scales

We split the data vector into a small and a large scale sample as described in Section 5. The results in the $\Omega_m$ – $S_8$ plane for the combination of angular power spectra and peak counts are presented in the right-hand plot of Fig. 8, while the individual comparisons are presented in Appendix I. We find a similar trend as Amon et al. (2021), Secco et al. (2022), with the removal of the large scales leaving $S_8$ intact, while the removal of the small scales leads to a shift in $S_8$ towards smaller values. We also note that the uncertainty increases significantly more if the small scales are removed, indicating once more that most information is gained from the smaller scales.

6.4 Comparison to other studies using DES Y3 data

We compare the parameter constraints found in this study using the combination of angular power spectra and peak counts to the results of other analyses that make use of the DES Y3 data. We find that
all results agree well between the different studies, indicating a high level of internal consistency within the DES Y3 data. The parameter constraints found in the considered studies were added to Table 2 and a visual comparison of the cosmological constraints is shown in the left-hand plot in Fig. 9.

6.4.1 DES Y3 $\xi_{\pm}$

We compare our results with the fiducial $\Lambda$CDM constraints found by the DES Y3 cosmic shear analysis (Amon et al. 2021) that uses angular two-point shear correlation functions as well as small-scale shear ratios. We note that a direct comparison between our results and the DES Y3 $\xi_{\pm}$ results is not meaningful for several reasons: (1) we use normal priors on $\Omega_0$, $n_s$, and $h$, while the DES Y3 $\xi_{\pm}$ analysis uses flat priors, (2) we adopt a fixed sum of the neutrino masses (see Section 2.2), while the DES Y3 $\xi_{\pm}$ analysis keeps the sum of the neutrino masses as a free parameter, (3) we model the galaxy intrinsic alignment signal in our simulations using the NLA model, while the DES Y3 $\xi_{\pm}$ analysis uses the more complex TATT model, (4) we impose scale cuts in harmonic space, while the DES Y3 $\xi_{\pm}$ analysis imposes scale cuts in real space, further complicating the comparison.

Therefore, we additionally compare to a modified version of the DES Y3 $\xi_{\pm}$ analysis (which we will refer to as ‘DES Y3 $\xi_{\pm}$ (comp)’) in which the sum of the neutrino masses is fixed to the same value adopted in our analysis and the galaxy intrinsic alignment model is changed to NLA. These modifications account for the primary sources of potential shifts in the parameter constraints that might arise due to the differences in the analysis choices making the comparison between the median parameter constraints more meaningful. However, due to the different scale cuts and prior choices a direct comparison between the found confidence regions is not straightforward.

Including these modifications we find that our results are in good agreement with the DES Y3 $\xi_{\pm}$ (comp) constraints, yielding no differences beyond 1 $\sigma$ in any of the constrained parameters. Both studies find an intrinsic alignment signal that is consistent with each other and with a null signal. We also note that Amon et al. (2021) obtains even tighter $\Lambda$CDM constraints thanks to the inclusion of small scale shear ratios in the analysis.

6.4.2 DES Y3 3$\times$2pt

The DES Y3 3$\times$2pt analysis uses information from galaxy-clustering and galaxy–galaxy lensing in addition to cosmic shear to constrain cosmology (Dark Energy Survey Collaboration 2021). The same caveats as for the comparison between this study and the DES Y3 $\xi_{\pm}$ analysis also apply for the comparison with the DES Y3 3$\times$2pt results. Therefore, we again compare our results not only to the fiducial DES Y3 3$\times$2pt analysis but also to a modified version called ‘DES Y3 3$\times$2pt (comp)’. The same modifications as for DES Y3 $\xi_{\pm}$ (comp) were made. The change from the TATT to the NLA model results in an increase in the constraining power. As we did not adapt the scale cuts to reflect this it has to be noted that the DES Y3 3$\times$2pt (comp) analysis does not pass the criteria defined in Appendix D of Dark Energy Survey Collaboration (2021) and the results might be biased. As a consequence we decided to centre the constraints at the fiducial cosmology adapted in the simulations ($\Omega_m = 0.26, \sigma_8 = 0.84$).

6.4.3 DES Y3 moments

We use peak counts to extract non-Gaussian information from the convergence field, but other summary statistics have also emerged as powerful tools to capture non-Gaussian information of the convergence field. Gatti (2021) use the second and third moments of the convergence field to capture Gaussian as well as non-Gaussian
information from the DES Y3 shear data. Additionally, Gatti (2021) use small-scale shear ratios to further tighten their cosmological constraints. As Gatti (2021) use the NLA galaxy intrinsic alignment model and keep the sum of the neutrino masses fixed in their analysis we directly compare to their fiducial results without any modifications. We again report no tension in any of the inferred parameters beyond 1 $\sigma$ and both studies measure a galaxy intrinsic alignment signal that is consistent with zero.

6.5 Comparison to external studies

The increased sensitivity of current LSS surveys brought to light some moderate tensions between the measurements of the structure growth parameter $S_8$ in the different surveys. Hence, we compare our findings to the recent results of the KiDS 1000 survey (Asgari et al. 2021). With the precision of LSS surveys on the $S_8$ parameter approaching the precision of CMB experiments mild tensions between LSS and CMB studies are arising as well. Therefore, we also compare our results to the Planck 2018 study (Aghanim et al. 2020). We estimate the tensions between our results and the external studies using the tensiometer software, allowing for a reliable, multidimensional estimate of the tensions taking into account non-Gaussianities in the posterior distributions (Raveri & Hu 2019; Raveri, Zacharegkas & Hu 2020; Raveri & Doux 2021). A visual comparison between the results of this study and the findings of the KiDS 1000 and Planck 2018 surveys is presented in the right-hand plot of Fig. 9. We restrict the discussion to the comparisons with KiDS 1000 and Planck 2018, but we also include the results from other surveys in Table 2 and Fig. 10 that might be of interest to the reader.

6.5.1 KiDS 1000 $\xi_{\perp}$

The KiDS 1000 cosmic shear study uses three different summary statistics to constrain cosmology from the cosmic shear field: COSEBIs, band powers, and the shear two-point correlation functions (Asgari et al. 2021). We compare our results to the most constraining KiDS 1000 result obtained using the shear two-point correlation functions. The KiDS 1000 survey uses a similar inference setup as our study keeping the sum of neutrino masses fixed and using the NLA galaxy intrinsic alignment model. Hence, we do not require any modifications for a meaningful comparison. We find our results to be in agreement with the KiDS 1000 results at the $0.3 \sigma$ level. However, we stress again that a comparison is not straightforward due to the non-trivial differences in the scale cuts, the treatment of systematic effects (such as galaxy intrinsic alignments) as well as the different choices of parameters and priors that can lead to a difference in the parameter constraints (Joachimi et al. 2021). Furthermore, the KiDS and DES surveys should not be treated as being fully independent, which further complicates the comparison.

6.5.2 Planck 2018

We compare our constraints to the ($\Lambda$CDM, TT, TE, EE+low E+lensing) results of Planck 2018 (Aghanim et al. 2020), finding a mild tension of $1.5 \sigma$. The measured tension is slightly lower than that recorded in other weak lensing studies. This can be attributed to the near zero value of $A_{\text{tilt}}$ and the breaking of the $S_8 - A_{\text{tilt}}$ degeneracy achieved by the combination of angular power spectra and peak counts (see right-hand plot in Fig. 7).
7 SUMMARY

Lensing peaks are sensitive to the highly non-linear features of the mass maps that get imprinted through massive objects in the LSS of the Universe. As such, lensing peaks have been found to extract additional non-Gaussian information of the mass maps that is missed by the more commonly used 2-point statistics. We combine the constraining power of peak counts with that of angular power spectra, which primarily target the complementary, Gaussian part of the information. We also include additional redshift information from cross-tomographic peak counts. We constrain the matter density \( \Omega_m \) as well as the amplitude of density fluctuations \( \sigma_8 \) of the Universe and the structure growth parameter \( S_8 \) (defined as \( S_8 \equiv \sigma_8 \sqrt{\Omega_m / 0.3} \) in this work) within the \( \Lambda \)CDM model. It should be noted that peak counts experience a different \( \Omega_m - \sigma_8 \) degeneracy than two-point statistics and the chosen definition of \( S_8 \) is not optimal for peak counts but most customary in weak lensing analyses. We infer cosmological constraints using the first three years (Y3) of cosmic shear data recorded by the DES containing about a hundred million galaxy shapes and spanning 4143 deg\(^2\) of the southern sky. The uncertainty from the remaining \( \Lambda \)CDM parameters \((\Omega_b, n_s, \text{ and } h)\), that are largely unconstrained in weak lensing studies, is taken into account by marginalizing them out over their priors.

Our method is based on a forward-modelling approach with numerical simulation. We simulate a large suite of DES Y3-like mass maps, dubbed DARKGRYV1, to predict the peak counts as well as the angular power spectra. We model these functions using a Gaussian Process Regression emulator. We follow the methodology outlined in Z21 to generate the simulated mass maps from a suite of PKDGRAV3 (Potter et al. 2017) dark-matter-only N-Body simulations sampling the \( \Omega_m - \sigma_8 \) space. We confirm that our simulations accurately recover the angular power spectra predicted by the theory code \textsc{CLASS} (Lesgourgues 2011). Further, we consider the major weak lensing systematics in our analysis: multiplicative shear bias, photometric redshift uncertainty, and galaxy intrinsic alignment. While we infer the amplitude of the galaxy intrinsic alignment signal \( A_{IA} \), we treat the redshift dependence of the signal as a nuisance parameter and marginalize over it. We test that our results are robust and not biased by either additive shear biases or source clustering. As we do not include a treatment of baryonic effects in this work, we estimate the impact of the presence of baryons on our results and impose stringent scale cuts to avoid potential biases.

Throughout the analysis we follow a strict two-stage blinding scheme. Before unblinding we performed a range of robustness checks, a null B-mode test, and a ‘goodness-of-fit’ test.

This work together with Gatti (2021) demonstrates the potential of using additional summary statistics beyond the commonly used 2-point functions to constrain cosmology from cosmic shear data. The main conclusions of this work include:

(i) In this study, we successfully apply the methodology developed in Z21 to the DES Y3 data. We perform a range of tests that validate the accuracy and applicability of the simulation used and the inference pipeline for this kind of data. We confirm that we recover the angular power spectra predicted from \textsc{CLASS} (Lesgourgues 2011) using the simulated DES Y3 like mass maps. Further, we assess that the accuracy of the emulator used is adequate for this sort of analysis.

(ii) We investigate several potential sources of systematic errors. While we conclude that our analysis is unlikely to be biased by source clustering effects or additive shear bias we apply stringent scale cuts to our data vectors to avoid biases from unmodelled baryonic physics.

(iii) Furthermore, we run a set of robustness tests to test for remaining redshift or scale-dependent systematic effects. We perform a map-level null B-mode test finding the noise-subtracted B-mode angular power spectra and peak counts of the DES Y3 data to be consistent with a null signal.

(iv) Using a combination of convergence angular power spectra and peak counts, we measure the structure growth parameter \( S_8 = \sigma_8 \sqrt{\Omega_m / 0.3} = 0.797^{+0.015}_{-0.013} \) at 68 per cent confidence within the \( \Lambda \)CDM model. This corresponds to a 1.8 per cent precision constraint and constitutes a 38 per cent and 13 per cent improvement over the angular power spectra and peaks only cases, respectively.

(v) We compare our results to the findings of other studies that constrain cosmology using DES Y3 data. We find agreement between our results and the other studies at the 1 \( \sigma \) level in all cosmological parameters constrained in this work.

(vi) Considering all constrained parameters in this study, we find our constraints to be statistically consistent with the results from the KiDS 1000 (Heymans et al. 2021) survey at the 0.7 \( \sigma \) level. Furthermore, we record a mild tension of 1.5 \( \sigma \) between our findings and the results from Planck 2018 (Aghanim et al. 2020).

(vii) We find that the combination of angular power spectra and peak counts tightly constrains the amplitude of the galaxy intrinsic alignment signal to \( A_{IA} = -0.03 \pm 0.23 \) and breaks the typically observed \( S_8 - A_{IA} \) degeneracy, greatly improving cosmological constraints. We further notice that the addition of cross-tomographic peaks significantly contributes to the constraining power of weak lensing peaks on \( A_{IA} \).

Having witnessed the potential of using peak counts to constrain cosmology from cosmic shear data, we look ahead to the application of the developed methodology to future data such as the DES Year 6 release. Such future surveys will be able to resolve the small-scale structure of the LSS even better than in current data. We plan to include a treatment of baryonic physics that allows us to incorporate and forward-model small-scale baryonic effects in our simulation pipeline and that will allow us to include more small-scale information, considerably improving the cosmological constraining power.

Another way to further increase the amount of cosmological information available is given by including other summary statistics such as Minkowski functionals or minima counts (Z21). A compromise between computational cost and the number of cosmological parameters that can be constrained had to be made. This led to the decision to only measure the parameters \( \Omega_m \) and \( \sigma_8 \) that are constrained most strongly by weak lensing data. We hope to extend our analysis to the full \( \Lambda \)CDM parameter space in a future project.

We observed that the combination of angular power spectra and peak counts puts tight constraints on \( A_{IA} \) and breaks the degeneracy between \( S_8 \) and \( A_{IA} \). However, we assume the rather simple NLA model to incorporate galaxy intrinsic alignment in this work. It is left to future studies to check if this remains true in the context of more complex alignment models such as the TATT model (Blazek et al. 2019).

ACKNOWLEDGEMENTS

The ETH Zurich Cosmology group acknowledges support by grants 200021/J192243 and 200021/169130 of the Swiss National Science Foundation. Some of the results in this paper have been derived using the healpy and HEALPix packages.
In this study, we made use of the functionalities provided by numpy (Walt, Colbert & Varoquaux 2011), scipy (Virtanen et al. 2020), matplotlib (Hunter 2007), scikit-learn (Pedregosa et al. 2011), Polychord.

We thank Antony Lewis for the distribution of GetDist, on which we relied to produce some of the plots presented in this work (Lewis 2019).

We would also like to thank Uwe Schmitt from ETH Zürich for his support with the GitLab server and CI engine.

Funding for the DES Projects has been provided by the U.S. Department of Energy, the U.S. National Science Foundation, the Ministry of Science and Education of Spain, the Science and Technology Facilities Council of the United Kingdom, the Higher Education Funding Council for England, the National Center for Supercomputing Applications at the University of Illinois at Urbana-Champaign, the Kavli Institute of Cosmological Physics at the University of Chicago, the Center for Cosmology and Astro-Particle Physic at the Ohio State University, the Mitchell Institute for Fundamental Physics and Astronomy at Texas A&M University, Financiadora de Estudos e Projetos, Fundacao Carlos Chagas Filho de Amparo a Pesquisa do Estado do Rio de Janeiro, Conselho Nacional de Desenvolvimento Científico e Tecnológico and the Ministerio da Ciencia, Tecnologia e Inovacao, the Deutsche Forschungsgemeinschaft and the Collaborating Institutions in the Dark Energy Survey. The Collaborating Institutions are Argonne National Laboratory, the University of California at Santa Cruz, the University of Cambridge, Centro de Investigaciones Energéticas, Medioambientales y Tecnológicas-Madrid, the University of Chicago, University College London, the DES-Brazil Consortium, the University of Edinburgh, the Eidgenössische Technische Hochschule (ETH) Zurich, Fermi National Accelerator Laboratory, the University of Illinois at Urbana-Champaign, the Institut de Ciencies de l’Espai (IEEC/CSIC), the Institut de Física d’Altes Energies, Lawrence Berkeley National Laboratory, the Ludwig-Maximilians Universität München and the associated Excellence Cluster Universe, the University of Michigan, NFS’s NOIRLab, the University of Nottingham, the Ohio State University, the University of Pennsylvania, the University of Portsmouth, SLAC National Accelerator Laboratory, Stanford University, the University of Sussex, Texas A&M University, and the OzDES Membership Consortium. Based in part on observations at Cerro Tololo Inter-American Observatory at NSF’s NOIRLab (NOIRLab Prop.ID 2012B-0001; PI: J. Frieman), which is managed by the Association of Universities for Research in Astronomy (AURA) under a cooperative agreement with the National Science Foundation.

Based on observations obtained with Planck,11 an ESA science mission with instruments and contributions directly funded by ESA Member States, NASA, and Canada.

DATA AVAILABILITY

The simulated data used in this work has been generated using the public code PKDGRAV (Potter et al. 2017). The full meta-calibration catalogue will be made publicly available following publication, at the URL https://des.ncsa.illinois.edu/releases. The code used in this article is publicly available at the URL https://cosmo-gitlab.phys.ethz.ch/cosmo_public.

REFERENCES

Albrecht A. 2006 APS Meeting Abstracts
Amon A. et al., 2021, Astrophysics - Cosmology and Nongalactic Astrophysics, 105, 23514
Bernstein G., Jarvis M., 2002b, AJ, 123, 583
Hikage C. et al., 2019, PASJ, 71, 43

11http://www.esa.int/Planck
APPENDIX A: FULL COSMOLOGICAL PARAMETER SPACE CONSTRAINTS

We present the constraints on the full cosmological parameter space for the fiducial data vector setups using the angular power spectra (Cls), peak counts (Peaks), and their combination (Cls + Peaks). The constraints are shown in Fig. A1.
APPENDIX B: EMULATOR ACCURACY

We check that the precision of the GPR emulator (used to predict the summary statistics for parameter configurations that are not sampled by numerical simulations directly) is sufficient. We do so following a ‘leave-one-out’ cross-validation strategy. We build the emulator for each point in the $\Omega_m - A_{IA} - S_8$ parameter space at which simulations were ran leaving out the simulations at this point. The error of the emulator is then estimated as the mean of the absolute, relative difference between the emulated data vector ($d_{emu}$) and the data vector obtained from the simulations ($d_{sim}$) that were left out when building the emulator

$$\epsilon_{emu} = \text{mean}\left(\frac{|d_{emu} - d_{sim}|}{|d_{sim}|}\right),$$

(B1)

where the mean is taken over all elements of the data vector.

We perform this test individually for the angular power spectra (top row of Fig. B1) and the peak counts (bottom row of Fig. B1). The maximum error found in both statistics is at the sub-percent level in most of the parameter space except for some points close to the borders of the investigated parameter space. We find the DES Y3 measurement precision to be $\sim 30$ per cent and $\sim 5$ per cent at the data vector level for the angular power spectrum and the peak counts, respectively. With the maximum error of the emulator being well below $\sim 5$ per cent of the DES Y3 measurement error on the

Figure A1. The fiducial constraints on all cosmological parameters obtained using angular power spectra (CLs), peak counts (Peaks), and their combination (CLs + Peaks). The contours indicate the 68 per cent and 95 per cent confidence regions. The constraints on $\Omega_b$, $n_s$, and $h$ are prior dominated (see Section 4.5 for details).

Figure B1. Visualization of the results of the accuracy tests for the GPR emulator in the $\Omega_m - S_8 - A_{IA}$ space. The top row shows the results for the angular power spectra and the bottom row shows the results for the peak counts. The left-hand and right-hand columns display the errors in the $\Omega_m - S_8$ and $A_{IA} - S_8$ subspaces, respectively. The colour of the data points indicates the mean relative error $\epsilon_{emu}$ of the GPR emulator, calculated according to equation (B1).
data vector level, we conclude that our results are not significantly biased by the inaccuracy of the GPR emulator.

We apply the same testing strategy to investigate the accuracy of the polynomial models used for the emulation of the second-order systematic effects, namely: multiplicative shear bias \( \alpha \), photometric redshift error \( \Delta z \), and the redshift dependence of the galaxy intrinsic alignment signal \( \eta \). The results for the angular power spectra and the peak counts, respectively, are presented in the top and bottom rows of Fig. B2, respectively. Again, we conclude that the errors originating from the emulation are subdominant compared to the precision of the DES Y3 measurement. Hence, we conclude that the complexity of the polynomial models is adequate for our analysis.

**APPENDIX C: ADDITIVE SHEAR BIAS**

Mismodelling of the PSF may lead to additive biases in the inferred shapes of source galaxies. Gatti et al. (2021) model the additive bias \( \delta e_{\text{PSF}} \) caused by PSF mismodelling in the DES Y3 shape catalogue as

\[
\delta e_{\text{PSF}} = \alpha e_{\text{model}} + \beta (e_s - e_{\text{model}}) + \eta \left( \frac{T_s - T_{\text{model}}}{T_s} \right),
\]

(C1)

following Paulin-Henriksson et al. (2008) and Jarvis et al. (2016). The modelled ellipticity and size of the PSF are denoted as \( e_{\text{model}} \) and \( T_{\text{model}} \), respectively. Correspondingly, \( e_s \) and \( T_s \) denote the PSF quantities measured from stars directly. The variables \( \alpha \), \( \beta \), and \( \eta \) are model parameters. Their values were inferred in Gatti et al. (2021) using a sample of reserved stars. We list the tomographic values of \( \alpha \), \( \beta \), and \( \eta \) in Table C1.

We estimate the additive shear bias \( \delta e_{\text{PSF}} \) of the DES Y3 shape catalogue according to equation (C1) individually for each tomographic bin using the values of the model parameters reported in Table C1. We check that the cosmological constraints do not shift significantly when the additive shear bias signal is added to the galaxy shapes according to

\[
e_{\text{mod}} = e + \delta e_{\text{PSF}}.
\]

(C2)

We use all multipoles \( \ell \in [8, 2048] \) for the angular power spectra and all scales FWHM \( \in [2.6, 31.6] \) arcmin for the peak counts in this test. We record a shift of the contours in the \( \Omega_m - \sigma_8 \) plane by less than 0.01\( \sigma \) for both the angular power spectra and the peak counts. We deem the estimated biases to be insignificant for our analysis and neglect additive shear bias in the inference process.

**APPENDIX D: BOOST FACTOR CORRECTIONS**

We estimate the boost factor corrections following the methodology outlined in Appendix C of K16 but neglecting the contribution from blending. We start by estimating the fractional excess of cluster galaxies \( e_{\text{cluster}}(\theta) \) around lensing peaks in the DES Y3 data relative to the number of galaxies in the field as

\[
e_{\text{cluster}}(\theta) = n_{\text{DES}}(\theta)/n_{\text{SIM}}(\theta).
\]

(D1)

The fractional excess \( e_{\text{cluster}}(\theta) \) is a function of angular distance \( \theta \) from the cluster centre. The number count of galaxies in the simulations \( n_{\text{SIM}} \) serves as a measure for the average number of galaxies around lensing peaks in the field, as the galaxy positions in our simulations are uncorrelated with the distribution of the dark matter. We measure \( e_{\text{cluster}}(\theta) \) as a function of scale and SNR, since the excess may vary depending on the SNR as well as the used smoothing scale. The galaxy excess functions \( e_{\text{cluster}}(\theta) \) inferred for an exemplary scale of 21.1 arcmin and the highest recorded SNR bin are shown in the top row of Fig. D1. While we observe a clear clustering signal in the non-tomographic sample, the signal is less pronounced in the tomographic sample and gets weaker with increasing redshift. As measured by K16, we observe that the clustering signal becomes stronger with increasing SNR of the lensing peaks.

Following the methodology outlined in greater detail in K16, we estimate the boost factor corrections \( f_{\text{corr}} = f_1/f_2 \) neglecting blending...
Figure D1. Top row: The fractional excess of cluster galaxies around lensing peaks in the DES Y3 data relative to the number of galaxies in the field (according to equation D1). The signal is measured around lensing peaks with an SNR of 3.6-4.0 as a function of radial distance $\theta$ from the centre of the peaks. For brevity we only present the results for peaks detected using a filter scale of 21.1 arcmin. The clustering signal is strongest in the non-tomographic sample, while being less pronounced in the tomographic case. Bottom row: The inferred boost factor corrections for the different tomographic bins as well as the non-tomographic sample as they apply to peaks with a scale of 21.1 arcmin. While we infer that a correction of up to $\sim$5 per cent is necessary for the non-tomographic sample, the corrections become smaller in the tomographic case.

APPENDIX E: ACCURACY OF SIMULATED MASS MAPS

A unit box with a side-length of 900 Mpc $h^{-1}$ and 768$^3$ particles was used in the PkDGRAV3 $N$-Body simulations. In order to cover a large enough cosmological volume the unit box has to be replicated up to 14 times per side for some cosmologies. It is expected that such a replication leads to the suppression of very large super-box modes. Further, the finite number of particles in the simulations leads to a shot-noise contribution.

The assembly of the particle shells into a projected convergence map is performed using UFalcon (Sgiyer et al. 2019). UFalcon avoids a full ray-tracing treatment by relying on the Born approximation, which can further contribute to a deterioration of the accuracy of the simulated convergence maps.

We test the accuracy of the simulations by comparing the full-sky angular power spectra of the 50 simulations at the fiducial cosmology to the prediction of an independent theory code. The comparison is displayed in Fig. E1. The theory prediction is obtained using the state-of-the-art theory code CLASS (Lesgourgues 2011). The Halofit code was used to predict the non-linear part of the power spectrum at small scales (Takahashi et al. 2012). We find that our simulations differ from the theory prediction by no more than $\approx 1.5$ per cent.
DES Y3 results: Cosmology with peaks

Figure E1. Absolute and relative comparison of the power spectra measured from the simulated full-sky mass maps at the fiducial cosmology (blue curves) and the predicted power spectra calculated using CLASS (red curves). Each panel shows the comparison for a different tomographic bin.

Figure E2. Absolute and relative comparison of the power spectra measured from the masked, noisy mass maps at the fiducial cosmology (blue curves) and the predicted power spectra obtained using CLASS (red curves). The effects of the mask were propagated to the theory prediction using the pseudo-$C_\ell$ method (Hikage et al. 2011) implemented in Sgier et al. (2021) and the average shape noise signal measured from simulations was added. Each panel shows the comparison for a different tomographic bin. Note that the range of the y-axis is different from the one in Fig. E1.

for $\ell \in [8, 2048]$ on average. The theory prediction for the matter power spectrum was found to vary by a few percent between different modelling implementations for the small scale signal (Martinelli et al. 2021). As the difference in the angular power spectrum is expected to be of the same order of magnitude we conclude that the disagreement between our simulations and the theory prediction is comparable to the disagreement between different theory predictions themselves. Hence, we deem the accuracy of the full-sky mass maps acceptable for this analysis.

We further test the accuracy of the fully forward-modelled mass maps. We do so by comparing the angular power spectra measured from the 10,000 simulated mass maps at the fiducial cosmology to a theory prediction calculated using CLASS. The effects arising from masking and shape noise are propagated to the theory prediction following the pseudo-$C_\ell$ method described in Sgier et al. (2021), based on Brown, Castro & Taylor (2008) and Kogut et al. (2003). The comparison is shown in Fig. E2. We find that the simulations agree with the theory prediction within $\approx 0.5$ per cent for all considered scales.
We again conclude that the accuracy of the simulated mass maps is sufficient for this analysis, following the same argument as for the full-sky power spectra.

**APPENDIX F: BARYONS**

The *PKDGRAV3* simulations used to predict the angular power spectra and peak counts at different cosmologies are dark-matter-only simulations that do not include effects arising from the presence of baryonic particles. As described in Section 3.4, significant biases caused by the missing baryonic physics in the simulations may arise. We investigate the shift of the constraints in the $\Omega_m - S_8$ plane caused by replacing a synthetic data vector with another synthetic, but baryon-contaminated, data vector at the same cosmology. Our methodology is similar to the approach used in Amon et al. (2021) where synthetic, baryon-contaminated shear data vectors were used to infer the necessary scale cuts.

The baryon-contaminated data vector was obtained from a simulation including baryonic corrections at the map level (Schneider & Teyssier 2015; Schneider et al. 2019). The baryon correction model was used to emulate these effects. This model allows us to mimic baryonic feedback effects by displacing particles around massive haloes in an N-Body simulation. The altered halo profiles resemble realistic profiles including effects from star formation and active galactic nucleus feedback. The locations of the haloes in the N-body simulation were identified using the {	exttt{AMIGA}} halo finder algorithm (Knollmann & Knebe 2009; Klement 2010). The baryonic correction model achieves good agreement with full hydrodynamical simulations as shown by Schneider et al. (2019). One of the major parameters driving the strength of the baryonic corrections in the model is the gas fraction of the haloes. Schneider et al. (2019) used X-Ray observations to constrain the gas fraction. However, the inferred gas fractions are prone to the uncertain hydrostatic mass bias. Schneider et al. (2019) propose three different models with three different hydrostatic mass biases. We used the best-guess model in this analysis (called model B in Schneider et al. 2019).

The estimated shifts of the contours in the $\Omega_m - S_8$ plane caused by the inclusion of baryonic effects for the angular power spectra and peak counts are illustrated in the left-hand and right-hand panels of Fig. F1, respectively. The scale cuts used in the production of the constraints presented in Fig. F1 were chosen such that the resulting shifts of the contours for both statistics is $\leq 0.3 \sigma$, which we deem acceptable for this analysis. The imposed threshold of $0.3 \sigma$ is in accordance with the unblinding criteria defined in Appendix D of Dark Energy Survey Collaboration (2021). This corresponds to $\ell \in [30, 578]$ for the angular power spectra and FWHM $\in [7.9, 31.6]$ arcmin for the peak counts. Our findings for the peak counts are in agreement with Weiss et al. (2019), who observed a non-negligible effect of baryonic physics on peak counts on scales below $\sim 8$ arcmin. For the combination of angular power spectra and peak counts we record a shift of $0.29 \sigma$, which fulfills the requirement of $\leq 0.3 \sigma$.

**APPENDIX G: B-MODES**

We present the noise-subtracted B-mode signals of the angular power spectra and the peak counts in Figs G1 and G2, respectively. We impose a requirement of $p > 1$ per cent for the null test to pass. This is in accordance with the unblinding criteria defined in Appendix D of Dark Energy Survey Collaboration (2021). For the angular power spectra we find $\chi^2$/dof $= 1.26$ and $p = 23$ per cent while for the peak counts we find $\chi^2$/dof $= 1.14$ and $p = 31$ per cent. Hence, we declare the B-mode null test as passed.

![Figure F1](https://academic.oup.com/mnras/article/511/2/2075/6511572)

**Figure F1.** Comparison between the obtained $\Omega_m - S_8$ constraints when using a baryon-contaminated synthetic data vector and a corresponding uncontaminated reference data vector. The left-hand and right-hand images display the comparison of the constraints for the angular power spectra and the peak counts, respectively. The shift of the constraints is noted in the bottom left-hand corner of the images. The scale cuts used in the production of these comparisons are $\ell \in [30, 578]$ for the angular power spectra and FWHM $\in [7.9, 31.6]$ arcmin for the peak counts.
Figure G1. The noise-subtracted angular power spectra DES Y3 B-modes. The noise signal was inferred using simulations with only a shape noise component but no cosmological signal. The shaded regions of the plots indicate where the scale cuts were imposed. Considering all angular power spectra with \( \ell \in [30, 578] \) we find a global \( \chi^2/\text{dof} = 1.26 \) and \( p = 23 \) per cent.
**Figure G2.** The noise-subtracted DES Y3 peak count B-modes for a selected smoothing scale of FWHM = 21.1 arcmin. The noise signal was inferred using simulations with only a shape noise component but no cosmological signal. Using the smoothing scales FWHM ∈ [7.9, 31.6] arcmin we find $\chi^2$/dof = 1.14 and $p = 31$ per cent.

**APPENDIX H: COSMOLOGY DEPENDENCE OF APPROXIMATE MARGINALIZATION SCHEME**

We confirm that the cosmology dependence of the used approximate marginalization scheme does not bias the results found in this study. To do so, we fit the polynomials $f_j(\theta)$ given in equation (20) at three different central cosmologies ($(\Omega_m, \sigma_8) \in \{(0.26, 0.826), (0.26, 0.84), (0.26, 0.875)\}$). The index $j$ runs over the different elements of the data vector and $\theta \in \{\Omega_b, n_s, h\}$. We then compare the cosmological constraints inferred using the three different fits (see Fig. H1 for the results for peaks for example). We record a maximal shift of $0.1\sigma$ of the constraints in the $\Omega_m - \sigma_8$ plane, which we deem acceptable for this analysis in accordance with the criteria defined in Appendix D of Dark Energy Survey Collaboration (2021).
Appendix I: Individual Scale Tests

We present how the results for the angular power spectra and peak counts change depending on the scale selection. To do so we split the data vectors into two parts: Large scales ($\ell \in [30, 257]$ and FWHM $\in [21.1, 31.6]$ arcmin) and small scales ($\ell \in [258, 578]$ and FWHM $\in [7.9, 18.5]$ arcmin). The resulting change of the $\Omega_m - S_8$ constraints is visualized in Fig. 11. Both statistics experience similar shifts.

$^1$Institute for Particle Physics and Astrophysics, Department of Physics, ETH Zürich, Wolfgang Pauli Strasse 27, CH-8093 Zürich, Switzerland
$^2$Department of Physics and Astronomy, University of Pennsylvania, Philadelphia, PA 19104, USA
$^3$Department of Physics and Astronomy, University College London, Gower Street, London WC1E 6BT, UK
$^4$Department of Astronomy and Astrophysics, University of Chicago, Chicago, IL 60637, USA
$^5$Kavli Institute for Cosmological Physics, University of Chicago, Chicago, IL 60637, USA
$^6$Department of Physics and Astronomy, Pevensy Building, University of Sussex, Brighton BN1 9QH, UK
$^7$Laboratoire de Physique de l’Ecole Normale Supérieure, ENS, Université PSL, CNRS, Sorbonne Université, Université de Paris, F-75005 Paris, France
$^8$Institute of Cosmology and Gravitation, University of Portsmouth, Portsmouth PO1 3FX, UK
$^9$Argonne National Laboratory, 9700 South Cass Avenue, Lemont, IL 60439, USA
$^{10}$Kavli Institute for Particle Astrophysics and Cosmology, P. O. Box 2450, Stanford University, Stanford, CA 94305, USA
$^{11}$Physics Department, 2320 Chamberlin Hall, University of Wisconsin-Madison, 1150 University Avenue Madison, WI 53706-1390, USA
$^{12}$Department of Physics, Carnegie Mellon University, Pittsburgh, PA 15312, USA
$^{13}$Department of Physics, Duke University Durham, NC 27708, USA
$^{14}$Center for Cosmology and Astro-Particle Physics, The Ohio State University, Columbus, OH 43210, USA
$^{15}$Lawrence Berkeley National Laboratory, 1 Cyclotron Road, Berkeley, CA 94720, USA
$^{16}$Department of Physics, Carnegie Mellon University, Pittsburgh, PA 15312, USA
$^{17}$NSF AI Planning Institute for Physics of the Future, Carnegie Mellon University, Pittsburgh, PA 15213, USA
$^{18}$Center for Cosmology and Astro-Particle Physics, The Ohio State University, Columbus, OH 43210, USA

Figure II. Left-hand panel: Scale robustness test for the angular power spectra. The shaded contour shows the constraints obtained using all scales. Either all the small ($\ell \in [258, 578]$) or large ($\ell \in [30, 257]$) scales were removed when obtaining the other two constraints. Right-hand panel: Analogous scale robustness test for the peak counts. The large and small scale samples consist of the scales FWHM $\in [21.1, 31.6]$ arcmin and FWHM $\in [7.9, 18.5]$ arcmin, respectively. The contour levels in both plots indicate the 68 per cent and 95 per cent confidence regions of the constraints.
This paper has been typeset from a 
\TeX/\LaTeX\ file prepared by the author.

\begin{flushright}
\textsuperscript{19}Department of Physics, The Ohio State University, Columbus, OH 43210, USA
\textsuperscript{20}Santa Cruz Institute for Particle Physics, Santa Cruz, CA 95064, USA
\textsuperscript{21}Jet Propulsion Laboratory, California Institute of Technology, 4800 Oak Grove Dr., Pasadena, CA 91109, USA
\textsuperscript{22}Faculty of Physics, Ludwig-Maximilians-Universität, Scheinerstr. 1, D-81679 Munich, Germany
\textsuperscript{23}Department of Physics, University of Oxford, Denys Wilkinson Building, Keble Road, Oxford OX1 3RH, UK
\textsuperscript{24}Jodrell Bank Center for Astrophysics, School of Physics and Astronomy, University of Manchester, Oxford Road, Manchester M13 9PL, UK
\textsuperscript{25}Department of Physics, University of Michigan, Ann Arbor, MI 48109, USA
\textsuperscript{26}Department of Applied Mathematics and Theoretical Physics, University of Cambridge, Cambridge CB3 0WA, UK
\textsuperscript{27}Perimeter Institute for Theoretical Physics, 31 Caroline St. North, Waterloo, ON N2L 2Y5, Canada
\textsuperscript{28}Department of Physics, Stanford University, 382 Via Pueblo Mall, Stanford, CA 94305, USA
\textsuperscript{29}SLAC National Accelerator Laboratory, Menlo Park, CA 94025, USA
\textsuperscript{30}Instituto de Física Gleb Wataghin, Universidade Estadual de Campinas, 13083-859 Campinas, SP, Brazil
\textsuperscript{31}Brookhaven National Laboratory, Bldg 510, Upton, NY 11973, USA
\textsuperscript{32}Institut d’Estudis Espacials de Catalunya (IEEC), E-08034 Barcelona, Spain
\textsuperscript{33}Institute of Space Sciences (ICE, CSIC), Campus UAB, Carrer de Can Magrans, s/n, E-08193 Barcelona, Spain
\textsuperscript{34}Laboratório Interinstitucional de e-Astronomia - LIneA, Carrer de Can Magrans, s/n, E-08193 Barcelona, Spain
\textsuperscript{35}CNRS, UMR 7095, Institut d’Astrophysique de Paris, F-75014 Paris, France
\textsuperscript{36}Sorbonne Universités, UPMC Univ Paris 06, UMR 7095, Institut d’Astrophysique de Paris, F-75014 Paris, France
\textsuperscript{37}Center for Astrophysical Surveys, National Center for Supercomputing Applications, 1205 West Clark St., Urbana, IL 61801, USA
\textsuperscript{38}Department of Astronomy, University of Illinois at Urbana-Champaign, 1002 W. Green Street, Urbana, IL 61801, USA
\textsuperscript{39}Institut de Física d’Altes Energies (IFAE), The Barcelona Institute of Science and Technology, Campus UAB, E-08193 Bellaterra (Barcelona) Spain
\textsuperscript{40}Jodrell Bank Center for Astrophysics, School of Physics and Astronomy, University of Manchester, Oxford Road, Manchester M13 9PL, UK
\textsuperscript{41}University of Nottingham, School of Physics and Astronomy, Nottingham NG7 2RD, UK
\textsuperscript{42}Astronomy Unit, Department of Physics, University of Trieste, via Tiepolo 11, I-34131 Trieste, Italy
\textsuperscript{43}INAF-Osservatorio Astronomico di Trieste, via G. B. Tiepolo 11, I-34143 Trieste, Italy
\textsuperscript{44}Institute for Fundamental Physics of the Universe, Via Beirut 2, I-34014 Trieste, Italy
\textsuperscript{45}Observatório Nacional, Rua Gal. José Cristino 77, Rio de Janeiro, RJ 20921-400, Brazil
\textsuperscript{46}Hamburger Sternwarte, Universität Hamburg, Gojenbergs Weg 112, D-21029 Hamburg, Germany
\textsuperscript{47}School of Mathematics and Physics, University of Queensland, Brisbane, QLD 4072, Australia
\textsuperscript{48}Centro de Investigaciones Energéticas, Medioambientales y Tecnológicas (CIEMAT), E-28040 Madrid, Spain
\textsuperscript{51}Department of Physics, IIT Hyderabad, Kandi, Telangana 502285, India
\textsuperscript{52}Department of Astronomy, University of Michigan, Ann Arbor, MI 48109, USA
\textsuperscript{53}Institute of Theoretical Astrophysics, University of Oslo, P.O. Box 1029 Blindern, NO-0315 Oslo, Norway
\textsuperscript{54}Instituto de Física Teórica UAM/CSIC, Universidad Autonoma de Madrid, E-28049 Madrid, Spain
\textsuperscript{55}Institute of Astronomy, University of Cambridge, Madingley Road, Cambridge CB3 0HA, UK
\textsuperscript{56}Kavli Institute for Cosmology, University of Cambridge, Madingley Road, Cambridge CB3 0HA, UK
\textsuperscript{57}Center for Astrophysics, Harvard and Smithsonian, 60 Garden Street, Cambridge, MA 02138, USA
\textsuperscript{58}Australasian Astronomical Optics, Macquarie University, North Ryde, NSW 2113, Australia
\textsuperscript{59}Lowell Observatory, 1400 Mars Hill Rd, Flagstaff, AZ 86001, USA
\textsuperscript{60}Centre for Gravitational Astrophysics, College of Science, The Australian National University, ACT 2601, Australia
\textsuperscript{61}The Research School of Astronomy and Astrophysics, Australian National University, ACT 2601, Australia
\textsuperscript{62}Departamento de Física Matemática, Instituto de Física, Universidade de São Paulo, CP 66318, São Paulo, SP 05314-970, Brazil
\textsuperscript{63}George P. and Cynthia Woods Mitchell Institute for Fundamental Physics and Astronomy, and Department of Physics and Astronomy, Texas A&M University, College Station, TX 77843, USA
\textsuperscript{64}Department of Astrophysical Sciences, Princeton University, Peyton Hall, Princeton, NJ 08544, USA
\textsuperscript{65}Institució Catalana de Recerca i Estudis Avançats, E-08010 Barcelona, Spain
\textsuperscript{66}Department of Astronomy, University of California, Berkeley, 501 Campbell Hall, Berkeley, CA 94720, USA
\textsuperscript{67}School of Physics and Astronomy, University of Southampton, Southampton SO17 1BJ, UK
\textsuperscript{68}Computer Science and Mathematics Division, Oak Ridge National Laboratory, Oak Ridge, TN 37831, USA
\textsuperscript{69}Max Planck Institute for Extraterrestrial Physics, Giessenbachstrasse, D-85748 Garching, Germany
\textsuperscript{70}Universitäts-Sternwarte, Fakultät für Physik, Ludwig-Maximilians Universität München, Scheinerstr. 1, D-81679 München, Germany