# Chapter 7 of <br> Data Analysis for Experimental Design 

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August 23, 2009

## 1 Pairwise Tests

### 1.1 Bonferroni

The Bonferroni does not require a separate command because as described in the text one merely changes the Type I error criterion.

### 1.2 Tukey Test

The Tukey test is easy to run in R. It takes as argument the output from the $\operatorname{aov}()$ command (see R notes for Chapter 6). For the following I'm using the data with 5 groups from Chapter 6 (which is different than what appears in Chapter 7).

```
group <- c(rep (1,8), rep (2,8), rep (3,8), rep(4,8), rep (5,8))
data <- c(16, 18, 5, 12, 11, 12, 23, 19, 16, 7, 10, 4, 7, 23, 12, 13, 2,
    10, 9, 13, 11, 9, 13, 9, 5, 8, 8, 11, 1, 9, 5, 9, 7, 11, 12, 9, 14, 19, 16, 24)
group <- factor(group)
output <- aov(data~group)
summary(output)
TukeyHSD(output)
    diff lwr upr p adj
2-1 -3.0 -10.06753766 4.0675377 0.7397203
```

```
3-1 -5.0 -12.06753766 2.0675377 0.2715178
4-1 -7.5 -14.56753766 -0.4324623 0.0329680
5-1 -0.5 -7.56753766 6.5675377 0.9995988
3-2 -2.0 -9.06753766 5.0675377 0.9246855
4-2 -4.5 -11.56753766 2.5675377 0.3729049
5-2 2.5 -4.56753766 9.5675377 0.8458204
4-3 -2.5 -9.56753766 4.5675377 0.8458204
5-3 4.5 -2.56753766 11.5675377 0.3729049
5-4 7.0 -0.06753766 14.0675377 0.0532717
```


## 2 Scheffe'

To my knowledge full use of Scheffe in R would require some programming. There is a plotting tool that uses Scheffe intervals in the CAR library.

I'll illustrate the use of R programming and its versatility. There are ways of working directly from the aov() output object rather than typing the actual numerical values, but I want to keep things relatively straightforward so the reader can see each step.

For the following I'm using the data with 5 groups from Chapter 6 (which is different than what appears in Chapter 7).

```
#you specify alpha level and degrees of freedom error
alpha.criterion <- . }9
dferror <- 36
#compute group means
groupmeans <- by(data,group,mean)
k <- length(groupmeans)
#calculate F
F <- qf(alpha.criterion, k-1, dferror)
tprime <- sqrt( (k-1)*F)
tempdiff <- matrix(0,k*(k-1)/2,5)
#nested for loops to compute all possible pairwise differences; store in
#matrix tempdiff
counter <- 1
for (i in 1:(k-1))
    for (j in (i+1):k) {
tempdiff[counter,1] <- i
tempdiff[counter,2] <- j
```

```
tempdiff[counter,3] <- groupmeans[i]
tempdiff[counter,4] <- groupmeans[j]
tempdiff[counter,5] <- (groupmeans[i]-groupmeans[j])/se
counter <- counter+1
}
dimnames(tempdiff) <- list(NULL,c("group i", "group j", "mean i",
    "mean j", "normalized diff"))
print(tempdiff)
print(paste("test statistic to beat (absolute value): ",
    round(tprime,3),sep=""))
```

|  | group i group j mean i mean j normalized diff |  |  |  |  |
| :--- | :--- | ---: | ---: | ---: | ---: |
| $[1]$, | 1 | 2 | 14.5 | 11.5 | 3.8461538 |
| $[2]$, | 1 | 3 | 14.5 | 9.5 | 6.4102564 |
| $[3]$, | 1 | 4 | 14.5 | 7.0 | 9.6153846 |
| $[4]$, | 1 | 5 | 14.5 | 14.0 | 0.6410256 |
| $[5]$, | 2 | 3 | 11.5 | 9.5 | 2.5641026 |
| $[6]$, | 2 | 4 | 11.5 | 7.0 | 5.7692308 |
| $[7]$, | 2 | 5 | 11.5 | 14.0 | -3.2051282 |
| $[8]$, | 3 | 4 | 9.5 | 7.0 | 3.2051282 |
| $[9]$, | 3 | 5 | 9.5 | 14.0 | -5.7692308 |
| $[10]$, | 4 | 5 | 7.0 | 14.0 | -8.9743590 |
| $[1]$ "test statistic to beat: $3.945 "$ |  |  |  |  |  |

