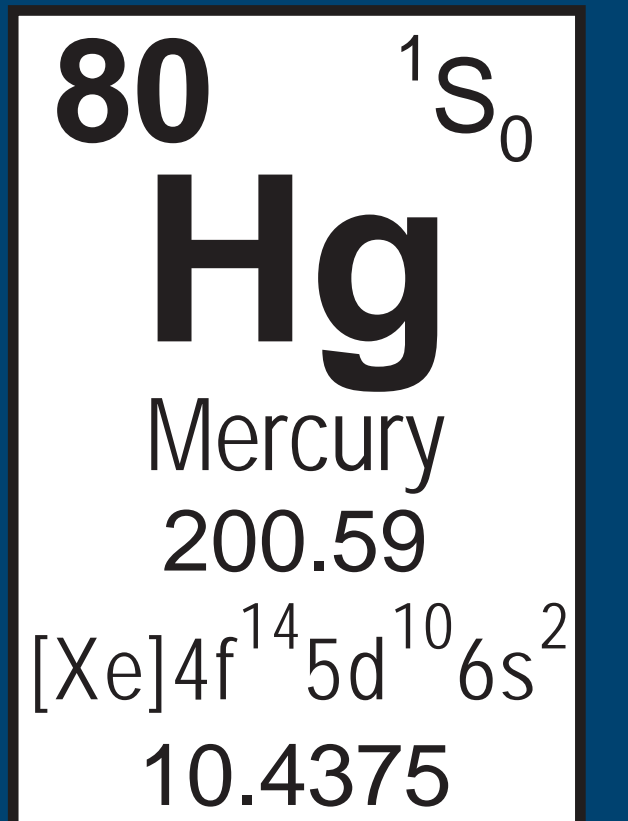




# A Hot Two-Photon E1-M1 Optical Clock

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## Frequency Standards

$$\sigma_\nu = \frac{\Delta\nu}{\nu} \sqrt{\frac{T}{\tau N}}$$

An allowed, two-photon E1-M1 transition from the  $^1S_0$  ground state to the  $^3P_0$  clock state creates a more portable optical frequency standard than the current generation of optical clocks. It can be implemented in thermal vapor cells. Improvements in frequency standards advance metrology for everyday applications such as GPS and for tests of fundamental physics.

$\Delta\nu$  transition linewidth       $T$  experiment duty cycle  
 $\nu$  excitation laser frequency     $\tau$  total experiment time     $N$  sample size

## E1-M1 Excitation Scheme

Probability of exciting an atom into  $^3P_0$

$$N_{3P_0} = P_{3P_0}(\Omega_{R2\gamma}, \bar{t}_B) \times$$

$$\Omega_{R2\gamma} = \frac{2I}{\hbar^2 c^2 \epsilon_0} \frac{\langle ^3P_0 || \mu || ^3P_1 \rangle_{M1} \langle ^3P_1 || D || ^1S_0 \rangle_{E1}}{\Delta}$$

Atom	amu	n	E1/ $ea_0$	M1/ $\mu_B$	$\Omega_{R2\gamma}$ [Hz]
Ra	226.0	7	1.2 [7]	$\sqrt{1.9}$ [7]	$1.4 \times 10^3$
Ba	137.3	6	0.45 [8]	$\sqrt{2}$	$6 \times 10^2$
Yb	173.1	6	0.54 [9]	$\sqrt{2}$ [9]	$5.1 \times 10^2$
Hg	200.6	6	0.44 [10]	$\sqrt{2}$	$1.9 \times 10^2$
Sr	87.6	5	0.15 [11]	$\sqrt{2}$	$1.8 \times 10^2$
Ca	40.1	4	0.036 [11]	$\sqrt{2}$	39
Mg	24.3	3	0.0057 [11]	$\sqrt{2}$ [10]	4.3
Be	9.1	2	0.00024 [10]	$\sqrt{2}$	0.19

Total number of addressed atoms

$$N_{tot}(T, \omega_0)$$

$$e^{-\frac{10^4}{T}} \left\{ \frac{1}{\omega_0} \right\} \frac{1}{\sqrt{T}}$$

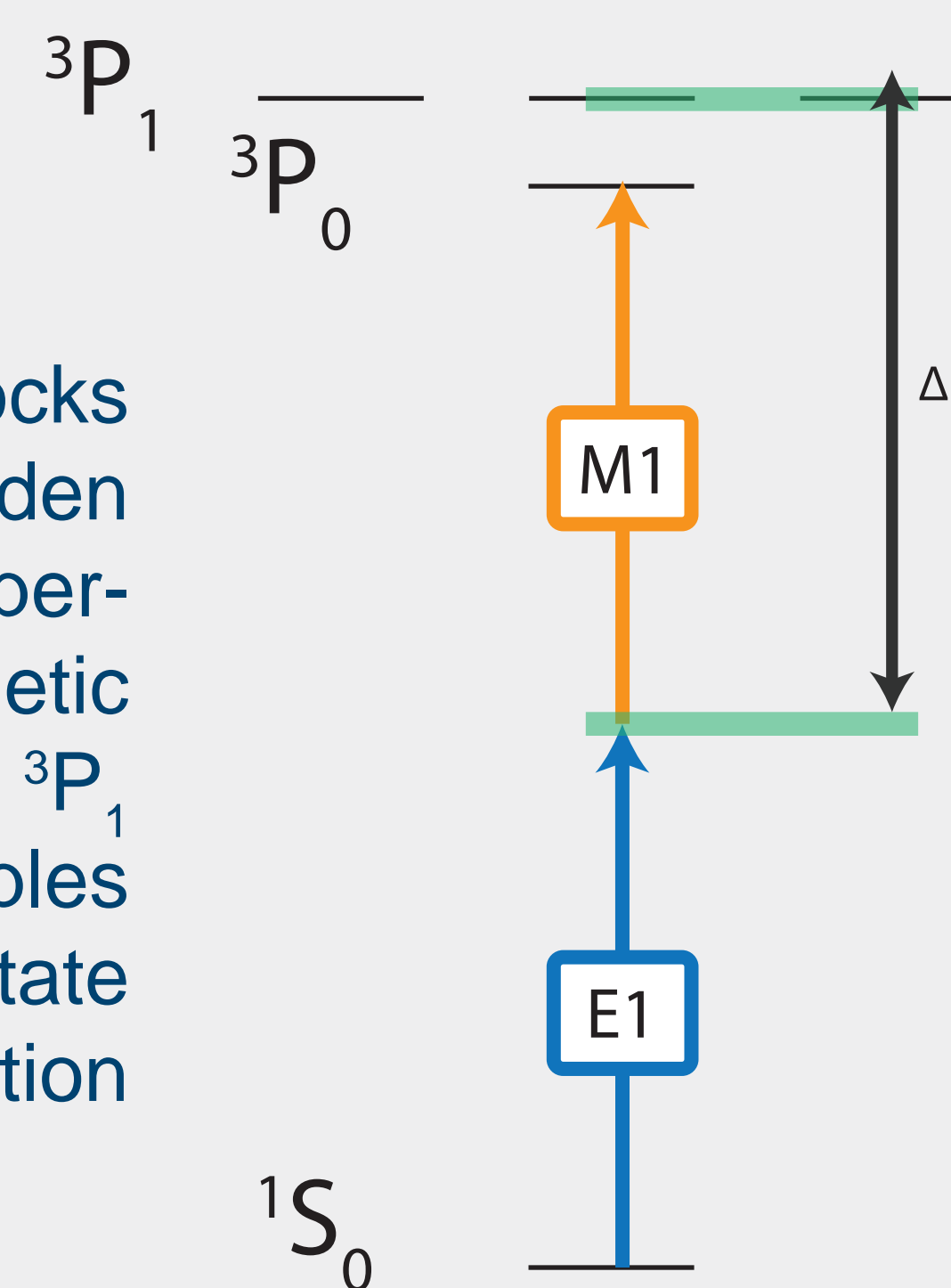
Optimal Parameters

large  $T$   
small  $\omega_0$

## References

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Current optical-frequency atomic clocks based on the electric dipole E1 forbidden  $^1S_0 > ^3P_0$  transition require either hyperfine structure or an applied magnetic field to induce mixing of the  $^3P_0$  and  $^3P_1$  levels. A two-photon excitation couples the  $^1S_0$  ground state to the  $^3P_0$  clock state through an allowed E1 and M1 excitation sequence.

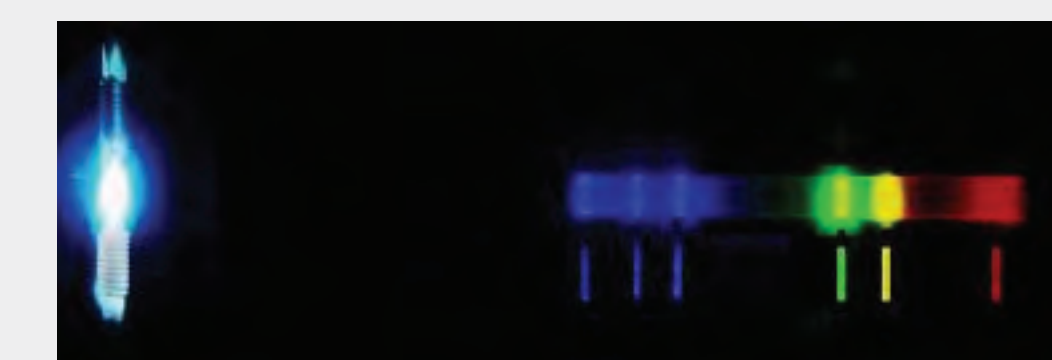
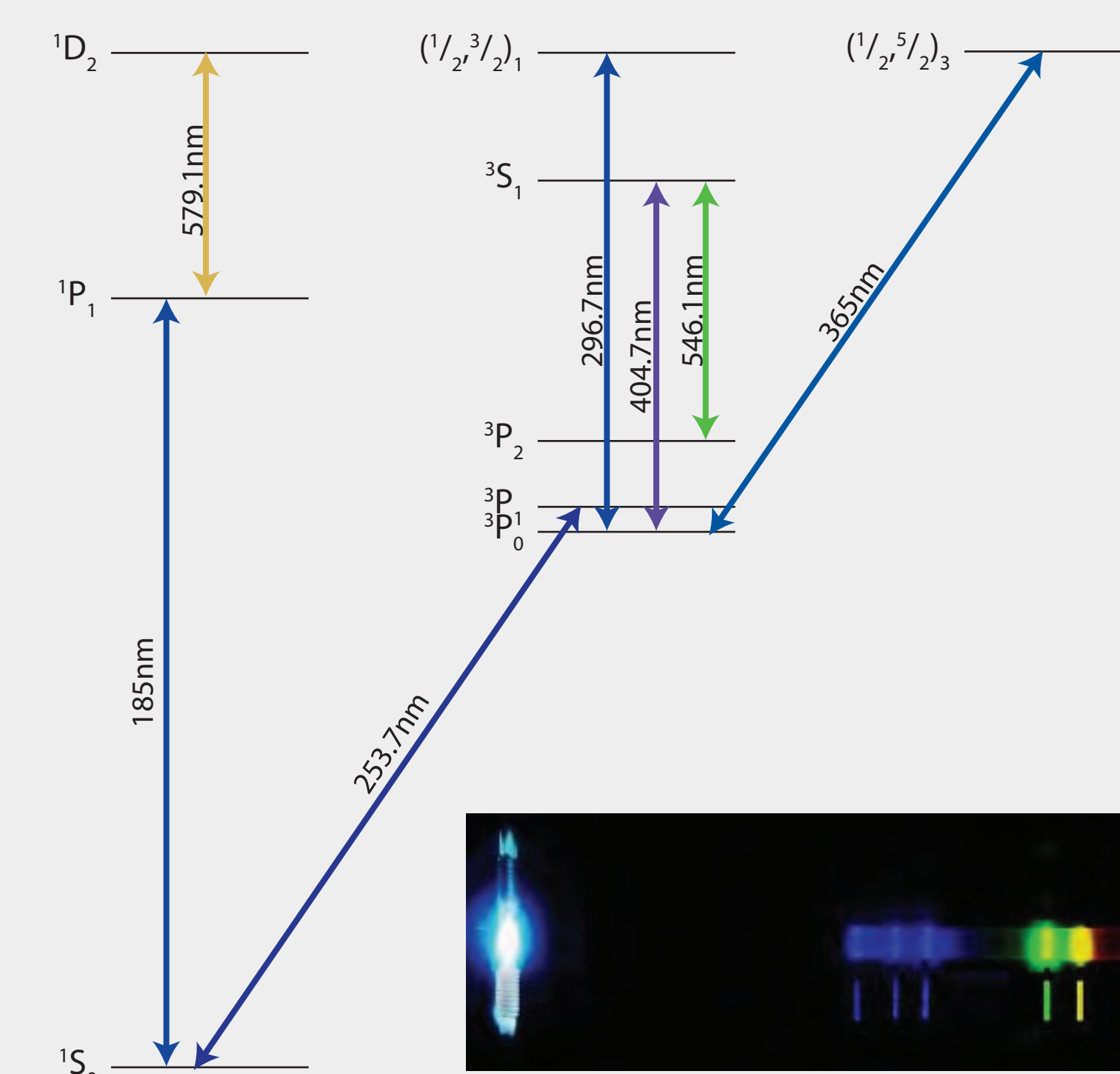


## Stability and Rate Estimates

Atom	T	$\omega_0$	$\sigma_\nu$
Hg	520 K	8.6e-04	5.03e-16
Yb	800 K	1.0e-03	5.57e-14
Ra	800 K	1.0e-03	8.65e-14
Sr	800 K	1.0e-03	5.81e-13
Ba	800 K	1.0e-03	2.25e-12
Ca	800 K	1.0e-03	1.03e-11
Mg	800 K	1.0e-03	1.07e-11
Be	800 K	1.0e-03	5.73e-08

N Clock Atoms			
Atom	T	$\omega_0$	$N_D$
Hg	620 K	1.1e-04	6.24e+12
Yb	800 K	1.7e-04	3.42e+08
Ra	800 K	1.9e-04	1.63e+08
Sr	800 K	1.8e-04	8.12e+06
Ba	800 K	2.0e-04	4.40e+05
Ca	800 K	1.8e-04	5.31e+04
Mg	800 K	1.5e-04	4.75e+04
Be	800 K	1.5e-04	4.34e-03

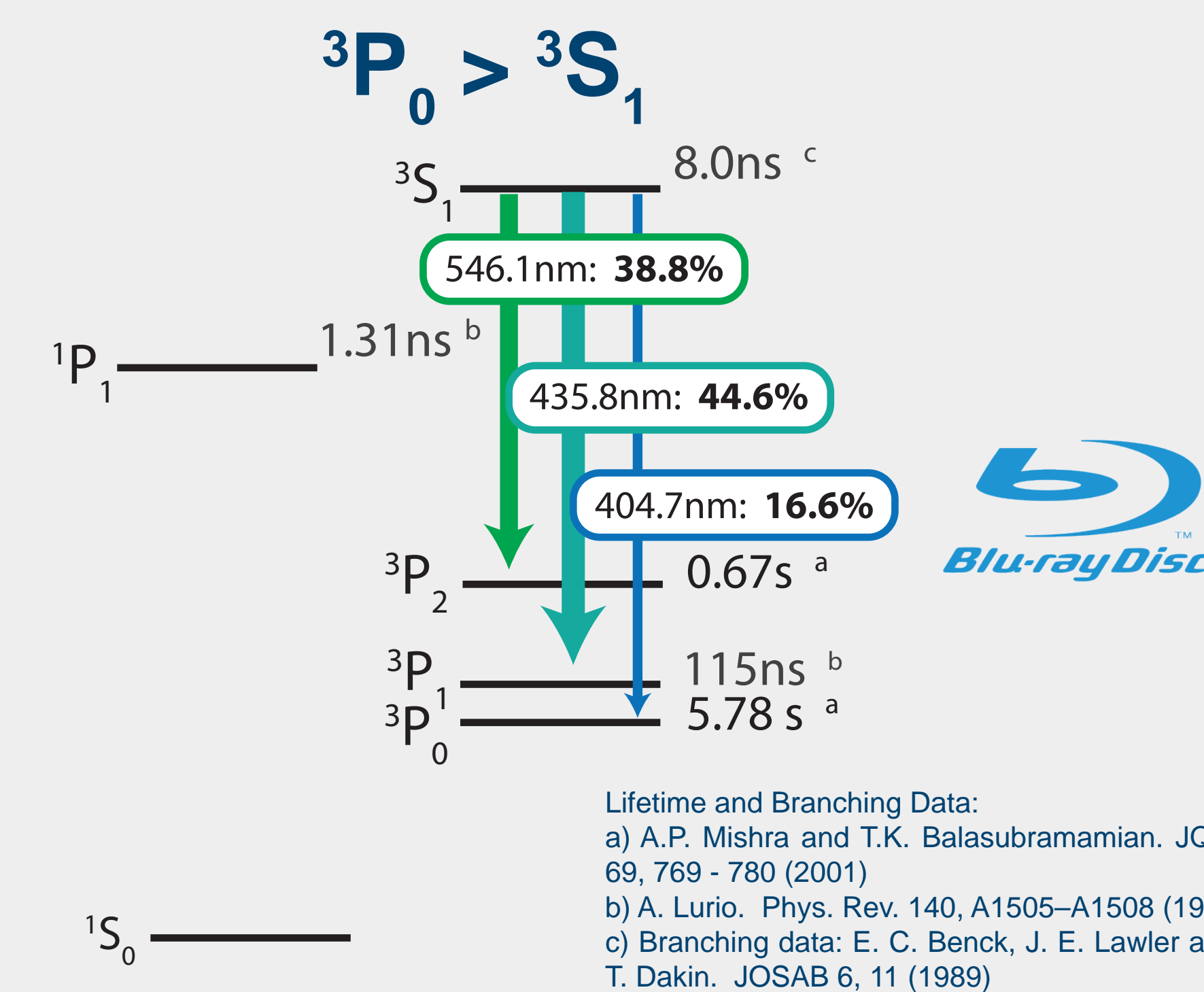
## Hg Electronic Structure



System	stability $\sigma_\nu \sqrt{\tau}$	Uncertainty $\sigma_\nu$
Hg $_{2\gamma}$	$10^{-16*}$	unk
Al $^+$	$3.7 \times 10^{-16}$	$8.6 \times 10^{-18}$
Yb $^+$	$3.2 \times 10^{-16}$	$1.6 \times 10^{-18}$
Sr	$2 \times 10^{-15}$	$1 \times 10^{-16}$
Rb	$7 \times 10^{-16}$	$3.7 \times 10^{-16}$
Hg $^+$	$9 \times 10^{-15}$	$7 \times 10^{-15}$
Hg $_{1\gamma}$		$5.7 \times 10^{-15}$
Yb	$5.1 \times 10^{-13}$	$1.4 \times 10^{-15}$
Cs	$5.8 \times 10^{-13}$	$10^{-15}$
Ag $_{2\gamma}$	$10^{-13*}$	
Quartz	$10^{-7}$	
Chronometer	$10^{0.5}$	

Common Systems Instability and Realized Uncertainties (\* denotes theorized values not experimentally realized)

## Experimental Setup



Lifetime and Branching Data:  
 a) A.P. Mishra and T.K. Balasubramanian, JQSRT **69**, 769 - 780 (2001)  
 b) A. Lurio, Phys. Rev. **140**, A1505-A1508 (1965)  
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