a)

The Block Diagram can be simplified using the feedback equation

$$
T=\frac{G}{1+G H}
$$

Using $G=1 /(s+1)(s+2)$ and $H=(1 / s)$, we find $T=s /\left(s^{\wedge} 3+3 s^{\wedge} 2+2 s+1\right)$.

Combining with the K block in cascade, we write
Gnew (s) $=\mathrm{Ks} /\left(s^{\wedge} 3+3 s^{\wedge} 2+2 s+1\right)$
Finally, we can use feedback again to simplify to a single block

Tfinal(s) $=K s /\left(s^{\wedge} 3+3 s^{\wedge} 2+(K+2) s+1\right)$
b)

We can use a Routh table to check for stability

| $s^{\wedge} 3$ | 1 | $K+2$ |
| :--- | :--- | :--- |
| $s^{\wedge} 2$ | 3 | 1 |
| $s^{\wedge} 1$ | $(5+3 K) / 3$ | 0 |
| $s^{\wedge} 0$ | 1 |  |

To keep the first row positive, we need (5+3K)/3>0 or $K>-5 / 3$.

