ALtruism via Kin-Selection Strategies That RELy on ARBITRary TAGS With Which They COEvolve

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Abstract.—Hamilton’s rule explains when natural selection will favor altruism between conspecifics, given their degree of relatedness. In practice, indicators of relatedness (such as scent) coevolve with strategies based on these indicators, a fact not included in previous theories of kin recognition. Using a combination of simulation modeling and mathematical extension of Hamilton’s rule, we demonstrate how altruism can emerge and be sustained in a coevolutionary setting where relatedness depends on an individual’s social environment and varies from one locus to another. The results support a very general expectation of widespread, and not necessarily weak, conditional altruism in nature.

Key words.—Armpit effect, Hamilton’s rule, inclusive fitness, Price equation, self-recognition, viscous population.

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Hamilton’s rule states that natural selection will favor altruism between conspecifics when $rb - c > 0$, where $r$ is their genetic relatedness, $b$ is the benefit to the recipient, and $c$ is the cost to the donor (Hamilton 1964). In practice, indicators of relatedness (such as scent) coevolve with strategies based on these indicators, a fact not included in previous theories of kin recognition (Crozier 1986; Reeve 1989; Ratnieks 1991; Agrawal 2001; Lehmann and Perrin 2002). We show with an evolutionary model how contingent altruism can be sustained even when arbitrary heritable indicators of relatedness, called “tags”, coevolve with the strategies governing behavior. Discrimination based on tags is not assumed, but rather evolves endogenously in a viscous population (i.e., local reproduction and local interaction) and is selected for even when phenotypic matching is very coarse-grained. We also show how to extend Hamilton’s rule to establish the conditions under which kin recognition can support discriminating altruism even when coevolution causes the reliability of indicators of relatedness to vary with each individual’s evolving social environment. This multitrait extension requires the calculation of different relatednesses for different traits. The simulation and the mathematical analysis show how discriminatory altruism can evolve in realistic settings where assessment of relatedness is based on weak and potentially deceptive indicators.

To explore the evolution of tag-based altruism, our model embodies three mechanisms. To allow altruism, but not direct reciprocity, fitness is determined by neighbors interacting in a one-move prisoner’s dilemma. To allow behavior that is conditioned on indicators of relatedness, strategies can take account of observable tags, such as scent. Tags differ from signals (Spence 1974; Grafen 1990) by being inflexible expressions of an individual’s genotype rather than subject to individual control (Hochberg et al. 2003). To allow competition for scarce resources, the population is viscous, and the population size is fixed. Because the tags and strategies are not linked, the model allows for the possibility of “cheaters” who can be free riders in the group whose tag they carry. The resulting agent-based model is based on a model previously developed to study ethnocentrism in humans (Axelrod and Hammond 2003). The present model is not meant to be a literal representation of biological processes. Instead, our model is designed to illuminate the consequences of the fact that kin discrimination typically entails coevolution of three things: the strategies governing behavior, the reliability of the tags on which the behavior may be conditioned, and the population structure that determines who interacts with whom.

The model is very simple. An individual agent has three traits, each a haploid genetic locus. The first trait is a tag that can be one of four observable types, such as scents. The second and third traits specify the agent’s strategy. The second trait has two alleles to specify whether the agent cooperates or defects (i.e., is altruistic or selfish) when meeting an individual of its own scent. Likewise, the third trait specifies whether the agent cooperates or defects when meeting an agent of a different scent. For example, the discriminatory strategy is cooperation with agents of one’s own scent and defection with others. In this model, the discriminatory strategy is only one of four possible strategies.

The simulation begins with a population of 2000 individuals (with random genotypes) each placed at random in its own site on a $50 \times 50$ lattice. The space has wrap-around borders so that each site has exactly four neighboring sites. Each period consists of two stages: interaction and reproduction.

In stage 1, each agent in the population receives an initial value of 0.12 as its potential to reproduce (PTR). Each pair of adjacent agents interacts in a one-move prisoner’s dilemma in which each player independently chooses whether or not to help the other. Giving help has a cost, namely a decrease in the agent’s PTR by 0.01. Receiving help has a benefit, namely an increase in the agent’s PTR by 0.03.
In stage 2, each agent is given a chance to reproduce asexually with probability equal to its PTR. An offspring receives the traits of its parent, with a mutation rate of 0.001 per trait. The expanded population of adults and infants is then culled at random to bring it back to its original size of 2000. The surviving offspring are then placed as close as possible to their parent’s cell. Placement starts with orphans who are placed in their deceased parent’s cell. Next to be placed are offspring who can find an empty cell adjacent to their surviving parent, and so on for increasing distances from the parent. (Distance is measured by “city-blocks.”)

The simulation results show that contingent altruism evolves even though there is no explicit bias for it in the model. Averaging over the final 100 periods of 30 2000-period runs, 76.6% of the agents have the discriminatory strategy. This high rate of discriminatory altruism results in 91.6% of same tag interactions being cooperative, and 82.7% of different tag interactions being noncooperative.

Notice that the model allows for deception by egoists who defect against everyone. In a region of discriminators of a certain scent, a lone egoist of the same scent will receive donations from its neighbors without itself donating. Analyzing the dynamics of the simulation reveals how contingent altruism suppresses egoists. A successful agent and its offspring quickly form a more or less coherent region. Consider what happens when an agent belonging to a region of discriminatory agents with a common tag interacts with an agent belonging to a region of, for example, egoists of a different scent. In this case, the discriminatory agent will do better overall because it gets help from other agents in its own region, while the egoist gets no help from other agents in its own region. The result is that a region of discriminators will tend to expand at the expense of an adjacent region of egoists of a different scent. In fact, a region of discriminators will tend to expand at the expense of a region of a different scent that uses any one of the three other strategies. In this way, discriminators of one scent hold egoists of other scents in check. Since the tag (scent) locus does not go to fixation, egoism is controlled. (A Quicktime movie at umich.edu/~axe/AHG/ illustrates the spatial dynamics of the simulation.)

The success of contingent altruism is robust under a wide range of parameters. When any of the following parameters are either halved or doubled, at least 63% of strategies are discriminatory and at least 68% of the choices are cooperative: lattice width, number of alleles on the tag locus, mutation rate, or duration of the run (Table 1). Changes in the size of the population relative to the lattice size also have minimal effect. For example, halving the proportion of empty space leads to an increase in the average distance between parents and their offspring, thereby weakening localism as a signal of relatedness. Even in this case, 58% of the agents use the discriminatory strategy, and 60% of the behavior is cooperative (Table 2). The simulation results are also not very sensitive to the possibility that an agent will occasionally misperceive whether or not the other agent in the interaction has the same scent. Even when agents make this mistake 10% of the time, the proportion of discriminatory strategy, level

In Table 1, the robustness of the simulation model is shown. The data are averaged over the last 100 iterations of the 30 replications of each variant. The base case parameter settings are: cost (c) = 0.01, benefit (b) = 0.03, number of colors = 4, mutation rate = 0.001, lattice size = 50 × 50, run length = 2000, proportion empty space = 20%.

In Table 2, the effects of variation in proportion of vacant space are shown. The less crowded the environment, the closer the offspring can be placed to their parents, resulting in higher levels of cooperation. Conversely, the more crowded the space, the further the offspring tend to be from their parents, and the more the results resemble the case of completely random placement. The data are averaged over the last 100 iterations of the 30 replications of each variant.
of contingent altruism, and the overall level of cooperation all remain over 75%.

Thus, contingent altruism evolving from local reproduction and local interaction can support cooperation, even when the interactions are one-move prisoner’s dilemma games. Indeed, some localism in both reproduction and interaction is necessary; if the simulation is run with either random placement of offspring or random interaction, less than 2% of the strategies are discriminatory and less than 1% of the interactions are cooperative. (The small amounts of cooperation are due to mutation-selection balance.) Even with localism, cooperation requires a sufficiently high ratio of benefit to cost. When the benefit is no greater than the cost, cooperation fails and the egoist strategy is dominant; but as the benefit/cost ratio increases, egoism gives way to altruism (Fig. 1).

A remarkable result of the simulation model is that discrimination based on an unreliable and potentially deceptive indicator of kinship can actually increase the total amount of cooperation in the population. As we have seen, when four alleles of the tag locus could be distinguished, 91.0% of all interactions were cooperative. In contrast, when all tags look alike, the rate of cooperation falls to 15.6%.

In this simulation, the indicator of relatedness evolves separately from the genes that control behavior, making the indicator potentially deceptive. Moreover, the indicator’s reliability can vary throughout the population because reproduction and interaction are local. This variability is representative of an important class of biological reality. Previous models of altruism have assumed fixed relatednesses (Reeve 1989; Agrawal 2001; Lehmann and Perrin 2002), or fixed levels of altruism (Crozier 1986; Ratnieks 1991). We now show how to extend Hamilton’s rule (henceforth HR) to cover coevolving traits and variably reliable indicators of relatedness, accounting for the evolution of contingent altruism under these very general conditions.

We begin by analyzing the social environment of the individual, defining the following variables: \( m \) is one if there is a match (same tag) between two interacting individuals and zero if there is not; \( A_m \) is one if the individual is altruistic toward a neighbor of type \( m \) and zero if not; \( A_m \) is the average \( A_m \) of neighbors, and \( N_m \) is the number of neighbors of type \( m \). For example, \( A_1 = 1 \) indicates altruism toward matching neighbors, and \( A_0 = 1 \) indicates altruism toward nonmatching neighbors. With these definitions, the individual’s PTR is

\[
P = a + b(A^*_1N_1 + A^*_0N_0) - c(A_1N_1 + A_0N_0),
\]

where \( a \) is the initial PTR before social interaction. In the simulation, \( a = 0.12 \), \( b = 0.03 \), and \( c = 0.01 \). With hard selection, relative fitness is \( W = (1 + P)/(1 + \bar{P}) \), where \( \bar{P} \) is the average \( P \) over the entire population for the period in question. Following Queller (1992), we substitute this formula for \( W \) into the population genetic Price equation (Price 1970) with perfect transmission

\[
\Delta E[A_m] = \text{cov}(A_m, W)
\]

and obtain an expression for the expected change in the mean of \( A_m \) before mutation

\[
k\Delta E[A_m] = b[\text{cov}(A_m, A^*_1N_1) + \text{cov}(A_m, A^*_0N_0)] - c[\text{cov}(A_m, A_1N_1) + \text{cov}(A_m, A_0N_0)],
\]

where \( k = 1 + \bar{P} \).

HR has been shown to apply (Grafen 1985) if \( r \) is measured in terms of genetic similarity rather than kinship, where genetic similarity at a single locus, for a given allele (whose frequency is \( p \)), is defined as:

\[
r = \frac{\sum H_j(R_j - p)}{\sum H_j(D_j - p)},
\]

where \( D_j \) and \( R_j \) are the potential donor and potential recipient’s genotype at that locus, and \( H_j \) equals one if a donation was made on the \( j \)th occasion on which a donation might be made and zero otherwise.

We now extend this analysis and add subscripts to define \( r_{mn} \), a relatedness at a locus \( m \) in relation to donations caused by locus \( n \), to provide a two-locus (or as we shall see later more generally a two-trait) version of HR. Each directed pair of neighbors will be considered an occasion and indexed by \( j \). \( H_{nj} \) is defined as one if an altruistic act is made through locus \( n \) on occasion \( j \), \( R_{nj} \) as one if the recipient on occasion \( j \) has the \( A_n = 1 \) allele, and \( D_{nj} \) as one if the potential donor on occasion \( j \) has the \( A_m = 1 \) allele; and each variable is zero otherwise. The generalization of \( r \) is

\[
r_{mn} = \frac{\sum H_{nj}(R_{nj} - p_m)}{\sum H_{nj}(D_{nj} - p_m)}.
\]

We now show how this formula can be used to analyze the forces of selection. Let \( S_m \) equal one if a donation would be made if the donor had allele \( A_m = 1 \) and zero otherwise, so that \( S_{nj} = 1 \) if the pair have the same tag, and \( S_{0j} = 1 \) if the pair have different tags. Noting that \( H_{mj} = D_{mj}S_{mj} \), we obtain the following identities:

\[
\sum_j H_{nj} = \sum_j D_{nj}S_{nj} = \sum_j R_{nj}S_{nj}, \quad \text{(6a)}
\]

\[
\sum_j H_{nj}R_{mj} = \sum_j D_{mj}R_{nj}S_{nj}, \quad \text{(6b)}
\]

\[
\sum_j H_{nj}D_{mj} = \sum_j D_{mj}D_{nj}S_{nj}, \quad \text{(6c)}
\]

of contingent altruism, and the overall level of cooperation all remain over 75%.

Thus, contingent altruism evolving from local reproduction and local interaction can support cooperation, even when the interactions are one-move prisoner’s dilemma games. Indeed, some localism in both reproduction and interaction is necessary: if the simulation is run with either random placement of offspring or random interaction, less than 2% of the strategies are discriminatory and less than 1% of the interactions are cooperative. (The small amounts of cooperation are due to mutation-selection balance.) Even with localism, cooperation requires a sufficiently high ratio of benefit to cost. When the benefit is no greater than the cost, cooperation fails and the egoist strategy is dominant; but as the benefit/cost ratio increases, egoism gives way to altruism (Fig. 1).

![Figure 1](image)

**FIG. 1.** Effect of variation in benefit/cost ratio. The benefit parameter \( b \) is systematically varied from 0.01 to 0.10 by increments of 0.01, with the cost parameter held constant at \( c = 0.01 \). The strategy distribution data are averaged over the last 100 iterations of the 30 replications of each variant.
where we have sometimes reversed the role of donor and recipient, $D_j$ and $R_j$. Such a reversal merely changes the order of the summation. It does not change the corresponding $S_{nj}$ because reversing roles does not affect whether two given individuals match on a specific locus. These identities allow us to show that

$$r_{mn} = \frac{\sum_j D_{nj} R_{nj} S_{nj} - p_m \sum_j R_{nj} S_{nj}}{\sum_j D_{nj} D_{nj} S_{nj} - p_m \sum_j D_{nj} S_{nj}}$$

$$= \frac{E[A_m A'_n N_j] - E[A_m]E[A'_n N_j]}{E[A_m A'_n N_j] - E[A_m]E[A'_n N_j]} = \frac{\text{cov}(A_m, A'_n N_j)}{\text{cov}(A_m, A'_n N_j)}. \quad (7)$$

Geometrically, $r_{mn}$ is the regression coefficient of $A'_n$ on $A_m$, using only data from directed pairs where a donation is caused by locus $n$; but forcing the line to pass through the point $E[A_m], E[A'_n N_j]$ (Grafen 1985). The same approach defines a cross-locus regression that measures linkage disequilibrium

$$\beta_{mn} = \frac{\sum_j H_{nj} (D_{nj} - p_m)}{\sum_j H_{nj} (D_{nj} - p_m)} = \frac{\text{cov}(A_m, A'_n N_j)}{\text{cov}(A_m, A'_n N_j)}. \quad (8)$$

This is the slope of $A_m$ on $A_n$ among individuals that make a donation caused by locus $n$, forcing the line to pass through the point $E[A_m], E[A'_n N_j]$.

Equation (3) can now be rewritten, assuming $n$ is the other strategy locus from $m$, as

$$k \Delta E[A_m] = \text{cov}(A_m, A'_n N_n)(r_{mn} b - c) + \text{cov}(A_n, A'_n N_n)\beta_{mn}(r_{mn} b - c), \quad (9)$$

and we immediately interpret terms as direct selection of $A_m = \text{cov}(A_m, A'_n N_n)(r_{mn} b - c)$, opportunity-weighted variation at $A_m = \text{cov}(A_m, A'_n N_n)$, HR term for $A_m$ over donations controlled by locus $m = r_{mn} b - c$, indirect selection via $A_m = \text{cov}(A_m, A'_n N_n)\beta_{mn}(r_{mn} b - c)$, opportunity-weighted variation at $A_n = \text{cov}(A_n, A'_n N_n)$, linkage disequilibrium with $A_n = \beta_{mn}$, and HR term for $A_n$ over donations controlled by locus $n = r_{mn} b - c$.

The generalization of HR in equation (9) directs a biological interpretation of the simulation results. Each term can be calculated from each period of the simulation data to provide a numerical analysis of selection over time, and the analysis is exact in expectation apart from the effects of mutation. To obtain an exact analysis, the relatednesses have been specially constructed, and they measure genetic similarity and not coancestry. This is the first version of HR to consider two traits simultaneously. We now turn to the interpretation.

First, it turns out that indirect selection is small enough to be neglected compared to direct selection. Thus, whether selection favors altruism toward matching neighbors ($A_1 = 1$) depends on the sign of the HR term $r_{11} b - c$, and whether selection favors altruism toward nonmatching neighbors ($A_0 = 1$) depends on the sign of the HR term $r_{00} b - c$. Inequality between the two relatednesses is necessary to achieve $r_{11} b - c > 0 > r_{00} b - c$, the condition for selection for discrimination.

This focuses attention on the relatednesses, $r_{11}$ and $r_{00}$. They can be compared to a third measure of relatedness based on the tag locus, say $r_t$. The ordering of relative relatedness is $r_{11} > r_t > r_{00}$, numerically after 2000 periods in the standard case, 0.328 (±0.014) > 0.222 (±0.036) > −0.047 (±0.074), where the standard errors derive from 30 replications of the simulation. The explanation is as follows. The relatednesses are measured over the opportunities for action, so $r_{11}$ is measured between same-tag neighbors while $r_{00}$ is measured between different tag neighbors. Within the relatively stable blocks composed of the same tag, neighbors are likely to share much recent common ancestry. By contrast, different tag neighbors are likely to descend from different tag parents, on either side of a tag-boundary, except in the relatively rare instances of recent mutation at the tag locus. This difference between relatednesses allows the evolution of discriminating altruism.

The time course of development of the relatednesses is also of interest. Unlike the analytical relatednesses employed by Taylor and Irwin (2000), our relatednesses, like those of Hamilton (1964), are statistical within the model, and so do not rely on an assumption of weak selection. Their statistical nature does mean that the mechanisms underlying them need to be studied. As the simulations begin with randomly placed random genotypes, both relatednesses begin at zero. After 25 generations, $r_{11}$ has climbed to 0.626 (±0.006) while $r_{00}$ still remains near zero: clusters of same-tagged individuals are forming so that same-tag neighbors share common ancestry, while opposite-tag neighbors do not. This value of $r_{11}$, if sustained, would result in $A_1 = 1$ going very close to fixation. However, as noted above, by 2000 generations, $r_{11}$ has fallen to 0.328 (±0.013), around the value of $c/b$, stabilizing the frequency of $A_1 = 1$. This fall must arise from the increased size of the same-tag clusters. The parents of same-tag neighbors may now be some distance away, even if in the same cluster. Furthermore, individuals on the inside of clusters have the highest fitness as they benefit most from altruism. Thus, there is higher pressure of offspring within a cluster to fill the gaps caused by culling than on its boundary. Large clusters have relatively larger insides, and so their offspring will on average be placed further from parents than in small clusters, and so reduce neighbor-neighbor relatedness. This effect of cluster-size on relatedness has a negative feedback effect and holds the population back from complete same-tag altruism.

There is an important extension not required for the simulations but that adds to the importance of the analysis of selection presented here. Provided the expected fitness is linear in the variables $A_m$, we can relax the requirement that $A_1$ and $A_0$ are each determined by a single haploid locus. Instead, $A$ can be any p-score (Grafen 1985). Thus, there can be any number of alleles at the locus, specifying arbitrary numerical values for $A$. The population could be diploid (or more generally polyplid), provided the value of $A$ is obtained by adding the numerical values of the alleles present. $A$ could even be determined by summing numerical values from the alleles present at more than one locus, provided all the loci have the same inheritance pattern. The analysis of selection retains exactly the same form, and the interpretations of the terms as regression coefficients of relatedness, regression
measures of genetic covariance, and measures of genetic variation, remain the same. Mitteldorf and Wilson (2000) study simulations that also have local competition and limited dispersal, and introduce noninclusive fitness arguments to supplement the original form of HR. In contrast, our analysis generalizes HR, and so incorporates the effects of local competition and dispersal into the overall framework of inclusive fitness, thus preserving the one conceptual framework with the capacity to embrace all work on selection of social traits.

The algebraic method above is the first published analysis of selection for kin recognition with simultaneous variation at the indicator and altruistic loci. This method helps us understand the conditions under which kin recognition can support discriminating altruism even when the reliability of indicators of kinship depends on the individual’s social environment. The simulation was specially designed to make net fitness linear in the values of the altruistic loci, so that benefits and costs of altruism in the algebraic analysis can be calculated directly from the specification of the simulation. The analytical approach can be applied in simulations with non-linear fitnesses by following Queller (1992) in obtaining ‘empirical’ estimates of $b$ and $c$ from a linearized fitness function.

The value of being able to distinguish tags can be understood in terms of inclusive fitness theory that takes into account the degree of relatedness between two agents (Hamilton 1964; Lacy and Sherman 1983; Riolo et al. 2001). While proximity alone can be an indication of relatedness, being able to distinguish among heritable tags, as in the armpit effect (Dawkins 1982; Hauber and Sherman 2000; Hauber et al. 2000; Mateo and Johnson 2000; Isles et al. 2001), allows a still better indication of relatedness, for example among sessile cnidarians (Grosberg and Quinn 1989; Grafen 1990). The discriminatory abilities required for the armpit effect are likely to be widespread. The self-recognition required for multicellularity provides them from intimate contact, and the need to distinguish conspecifics for mating provides them more generally for animals. In both cases, a hardwired comparison known as the green beard effect (Hamilton 1964; Dawkins 1976; Haig 1996; Grafen 1998; Keller and Ross 1998) would seriously slow evolution and make speciation almost impossible.

Viscosity is ubiquitous because few populations completely mix from one generation to the next. Hamilton (1964) believed that simple viscosity was a widespread sufficient cause of fairly weak altruism, and various models have found that viscosity can indeed foster cooperation (Getty 1987; Pollock 1989; Nowak and May 1992; Nakamaru et al. 1997). However, this general claim is now considered doubtful. The balance between increased relatedness and increased competition between neighbors may tilt toward or away from cooperation (Taylor 1992; Wilson et al. 1992; West et al. 2002). Taylor and Irwin (2000) have suggested that with overlapping generations, and with altruism dispensed as benefits to fecundity, there is a tendency for population viscosity to support altruism. The 15.6% cooperation found in our model with one tag is on the one hand more than zero, supporting Taylor and Irwin, but on the other hand is rather limited. Adding observable tags shows that proximity can sustain cooperation based on contingent altruism, even if the very correlation of tags and relatedness evolves. By putting both the matching and the altruism under explicit genetic control, the model shows how altruism conditional on heritable tags can evolve despite substantial costs of cooperation. Thus, the present model, which combines viscosity, the armpit effect, and endogenous use of discrimination in a genetically explicit way, creates a very general expectation of widespread, and not necessarily weak, conditional altruism in nature.

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Literature Cited


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