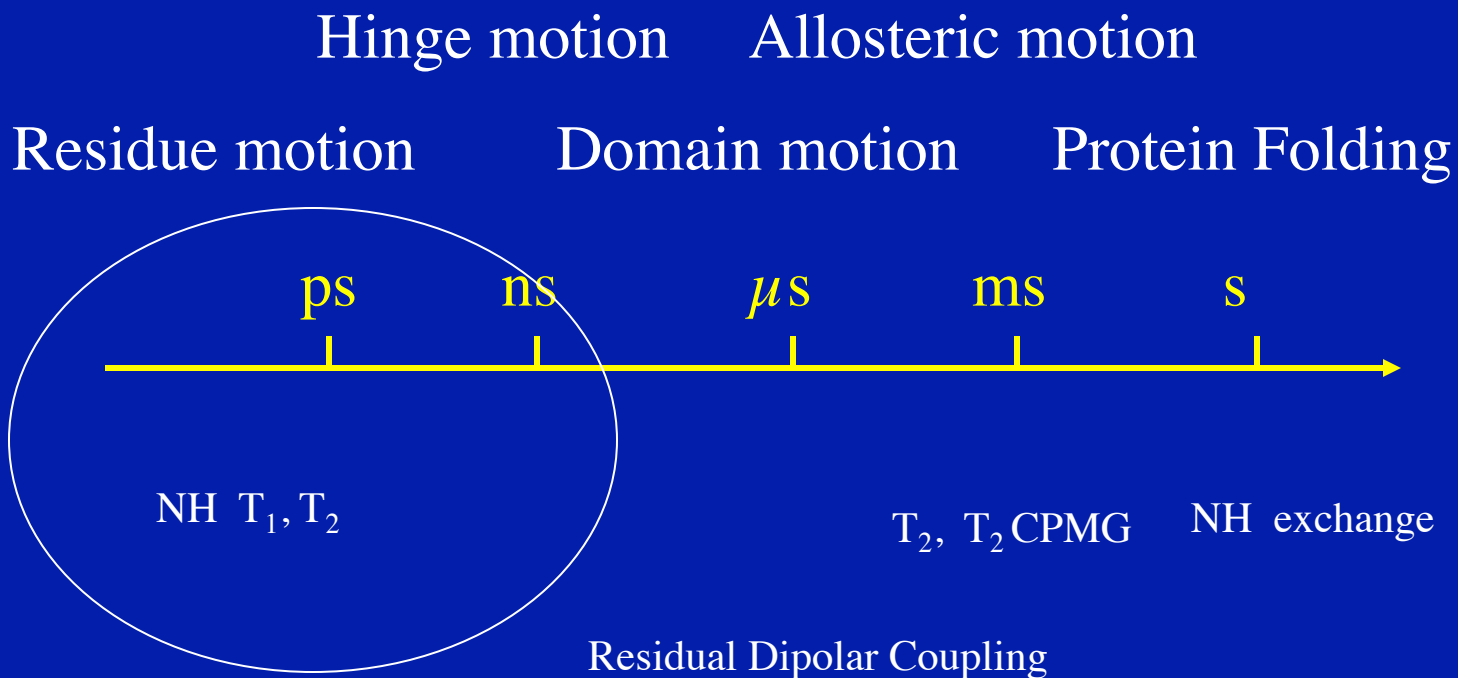


NMR relaxation detects  
pervasive motions  
in proteins on many timescales

Dynamics research in the Zuiderweg Lab  
1993-2010

# Common NMR relaxation



Boltzmann

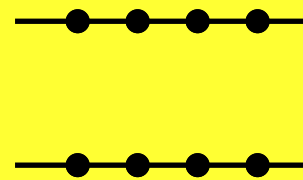


800 MHz

R.F.



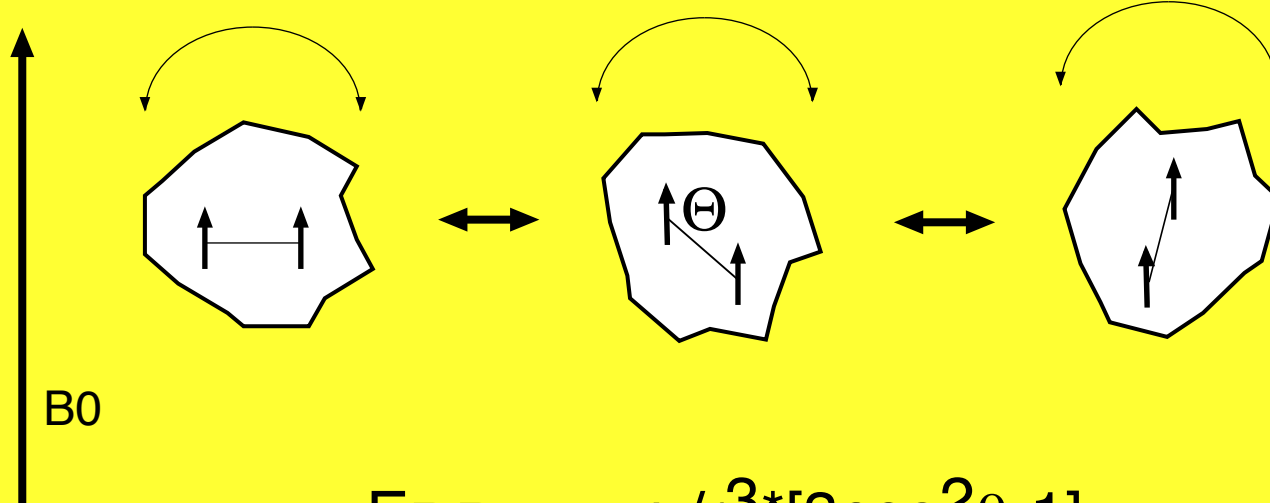
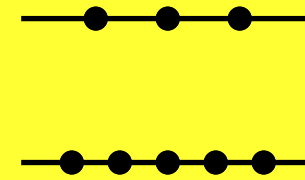
perturbed



relaxation

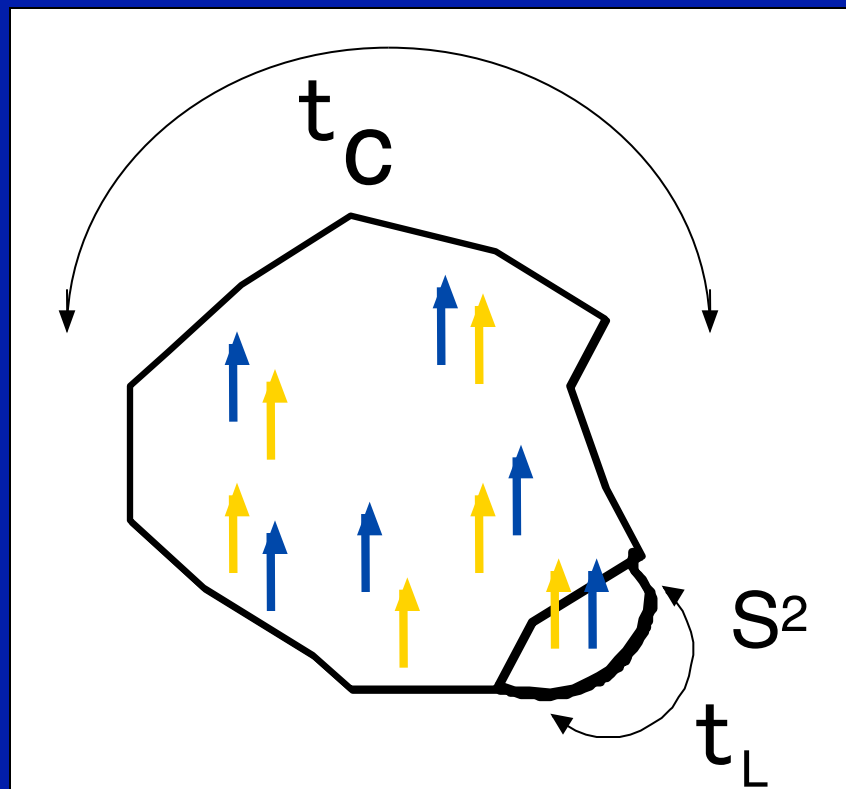


Boltzmann



$$E_{DD} = \mu_a \mu_b / r^3 [3 \cos^2 \theta - 1]$$

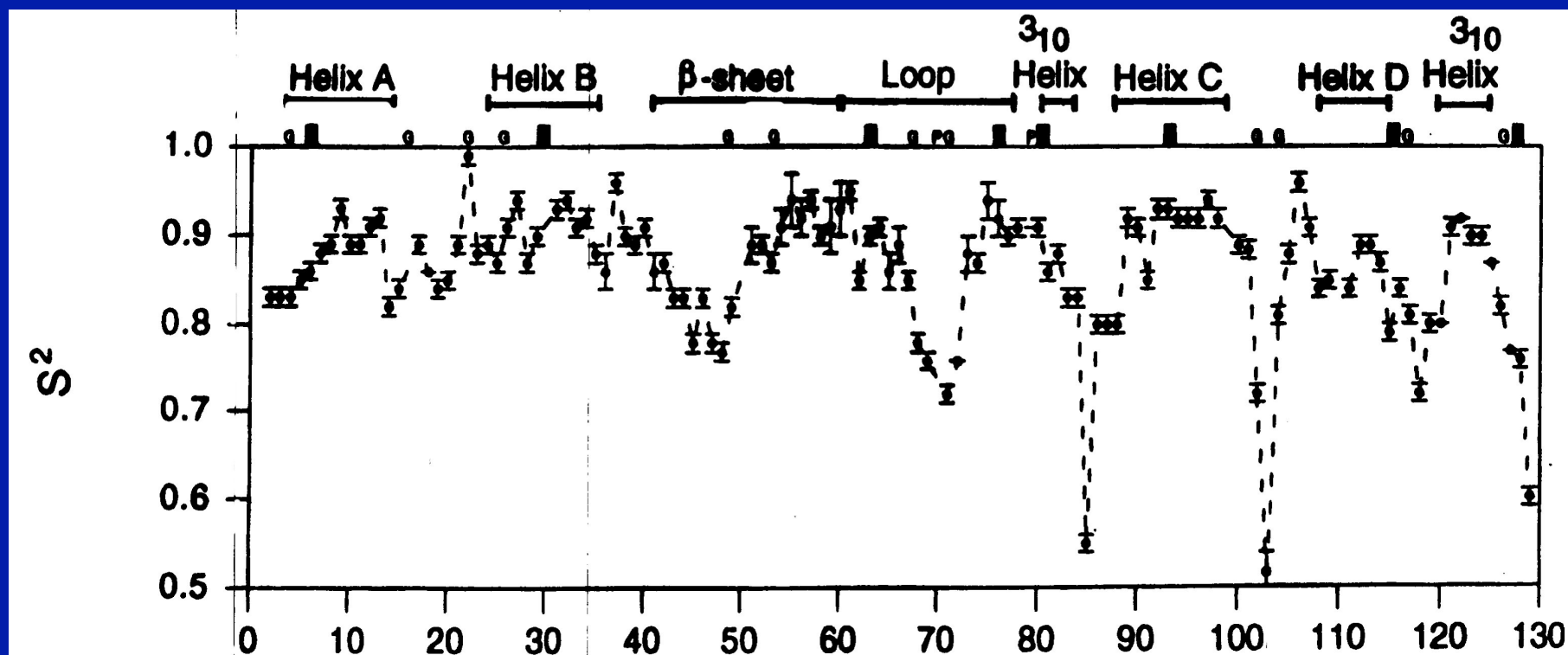
$$\text{Relax\_Eff} \sim \langle E_{DD}^2 \rangle \sim K / r^6 F(t_c)$$



$$R \propto K \frac{1}{r_{ab}^6} F(\tau_{MOL}, \omega_{NMR})$$

$$R \propto K \frac{1}{r_{ab}^6} \left[ \frac{S^2 \tau_C}{1 + \omega^2 \tau_C^2} + \frac{(1 - S^2) \tau_L}{1 + \omega^2 \tau_L^2} \right]$$

# $^{15}\text{N}$ - $^1\text{H}$ vector (amide) Order parameters of Lysozyme



# NMR Dynamics and Entropy

Model motion as a probability distribution  $P(\theta)$

and compute averaged spherical harmonics

$$\langle P_2(\cos\theta_{0-\infty}) \rangle = \frac{1}{4\pi} \int_0^{2\pi} P_2(\cos\theta) P(\theta) \sin\theta \, d\theta$$

Straightforward substitution yields order

parameter

$$S_{NMR}^2 \propto \left\langle \frac{3}{2} \cos^2 \theta_{0-\infty} - \frac{1}{2} \right\rangle^2 \equiv \langle P_2 \cos\theta_{0-\infty} \rangle^2$$

and relaxation rate

$$R \propto K \frac{1}{r_{ab}^6} \left[ \frac{S^2 \tau_C}{1 + \omega^2 \tau_C^2} + \frac{(1 - S^2) \tau_L}{1 + \omega^2 \tau_L^2} \right]$$

Compare with experiment and adapt  $P(\theta)$

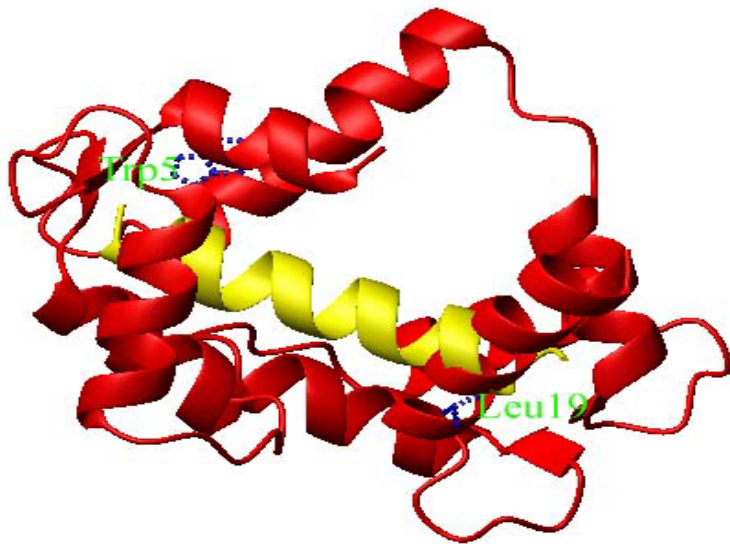
Take best  $P(\theta)$  and compute entropy from basic

statistical mechanics

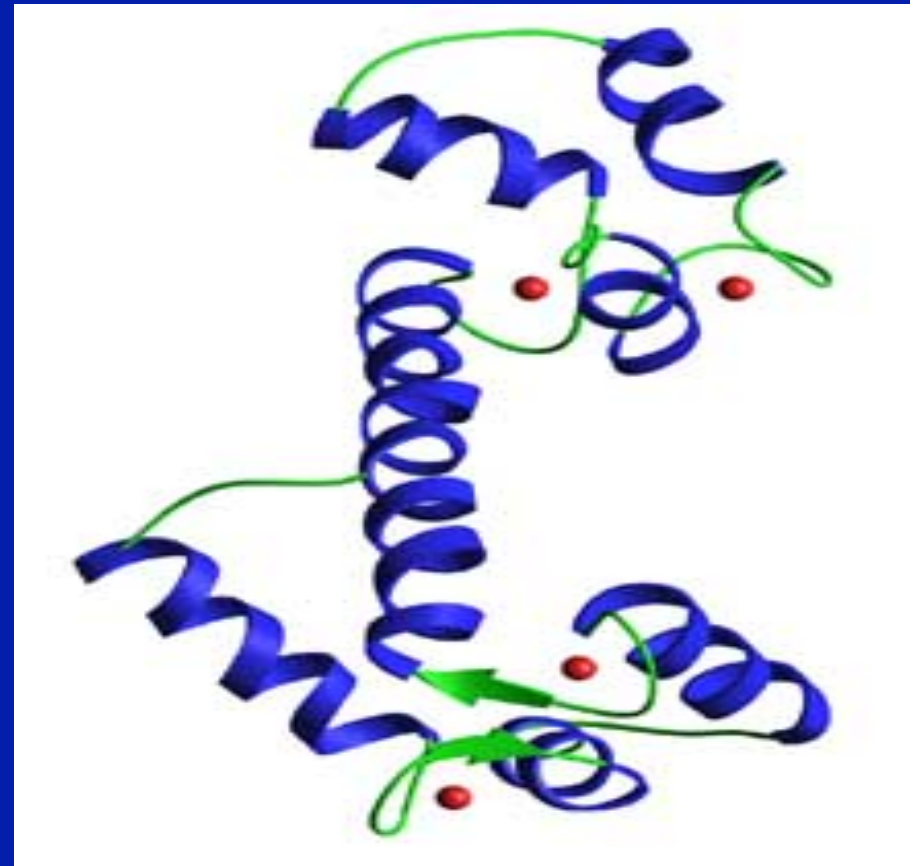
$$S_{CONFIG} = \int_0^{2\pi} P(\theta) \ln(P(\theta)) \sin\theta \, d\theta$$

Is the backbone really  
the best indicator of motion

# Structure of Calmodulin with and without peptide



Smooth muscle myosin light chain kinase peptide

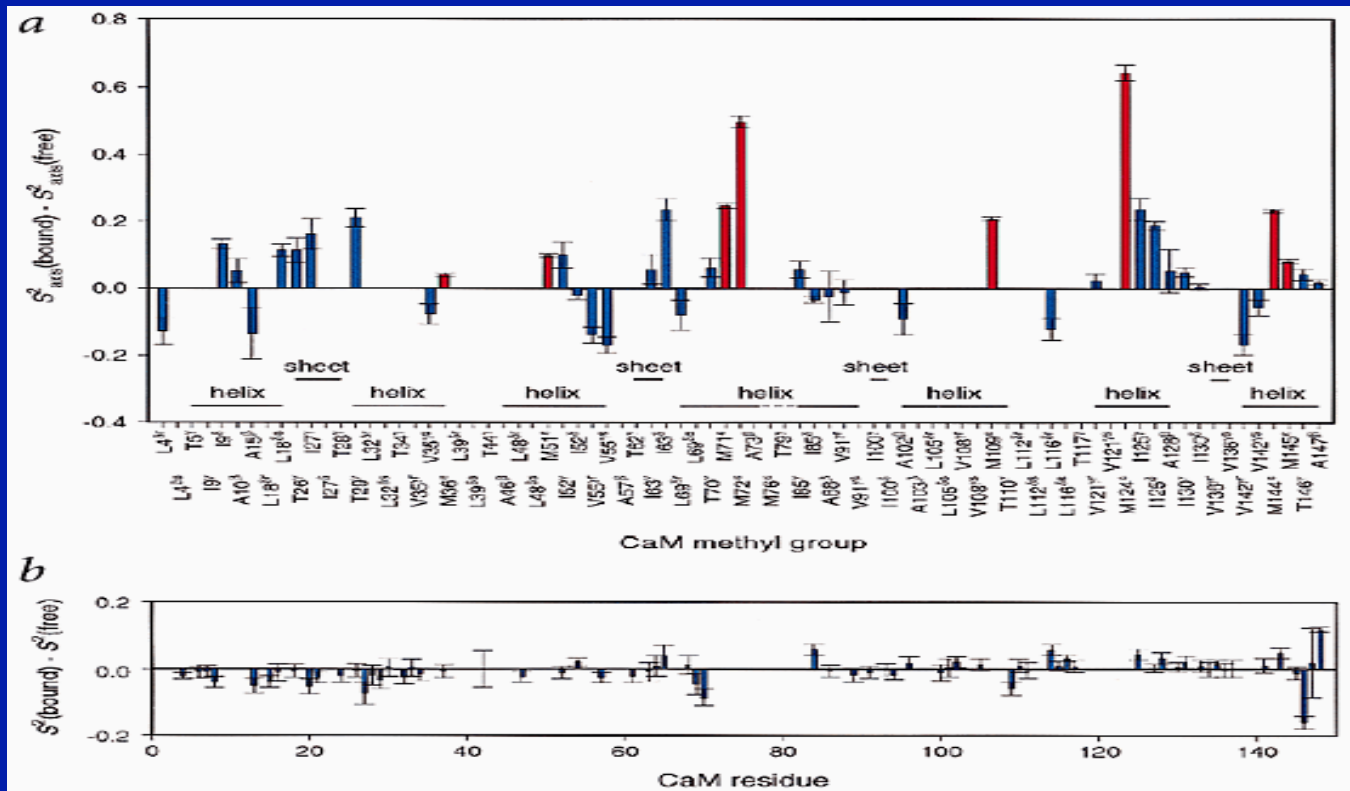




# Dynamics of Calmodulin with and without peptide

## Differences in order parameter (bound-free)

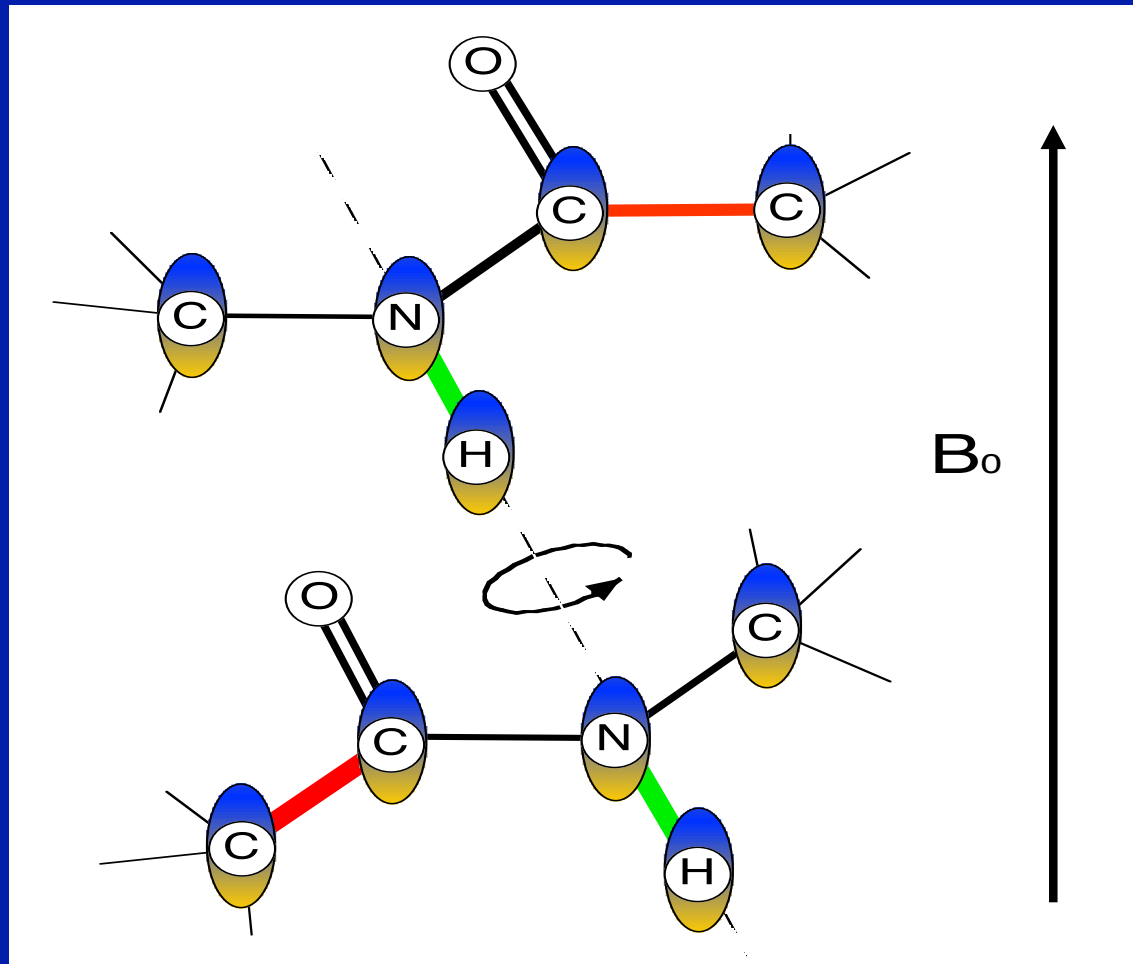
CH<sub>3</sub>



NH

Lee, Kinnear, Wand, Nat. Struct. Biol. 7, 2000:72

# The NH may not see motions the C-C can

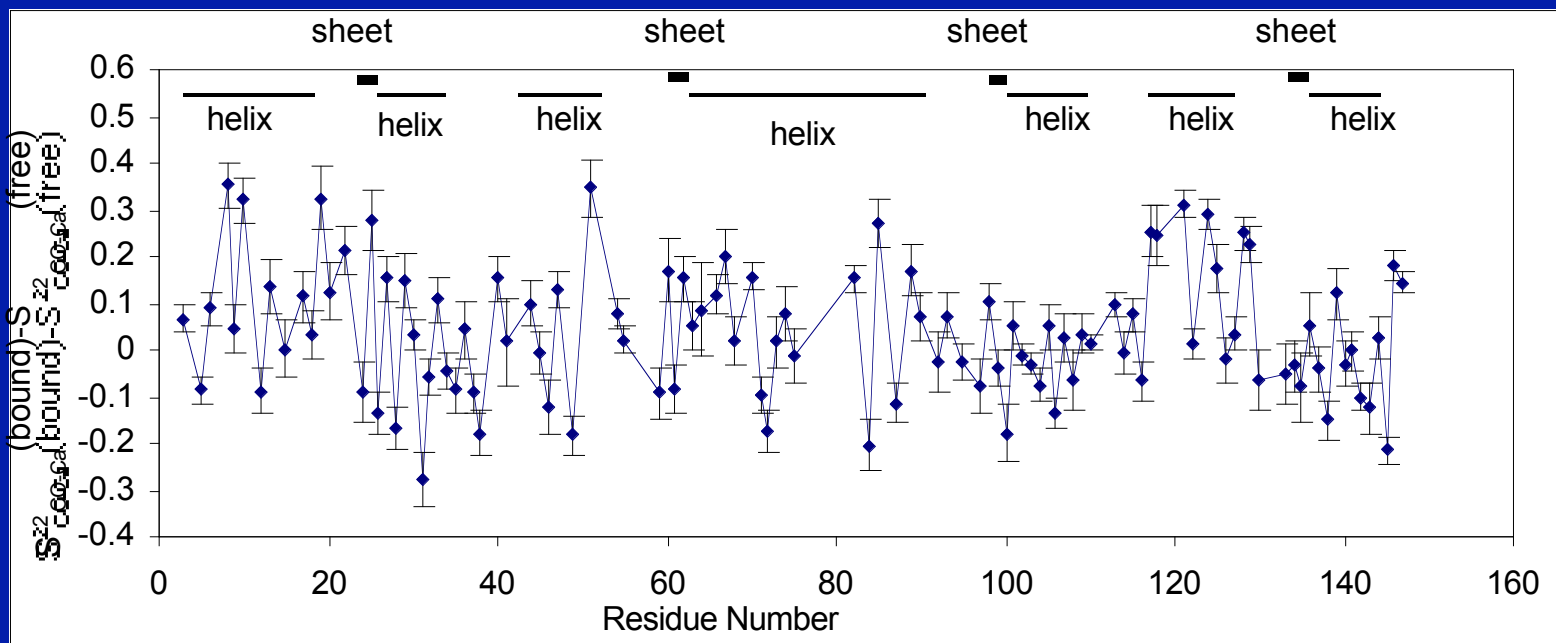


Zeng, L., Fischer, M.W.F. and Zuiderweg, E.R.P. Study of Protein Dynamics in Solution by Measurement of  $^{13}\text{C}\alpha$ - $^{13}\text{C}\text{O}$  NOE and  $^{13}\text{C}\text{O}$  longitudinal relaxation. *J. Biomol. NMR*, 1996; 7, 157-162

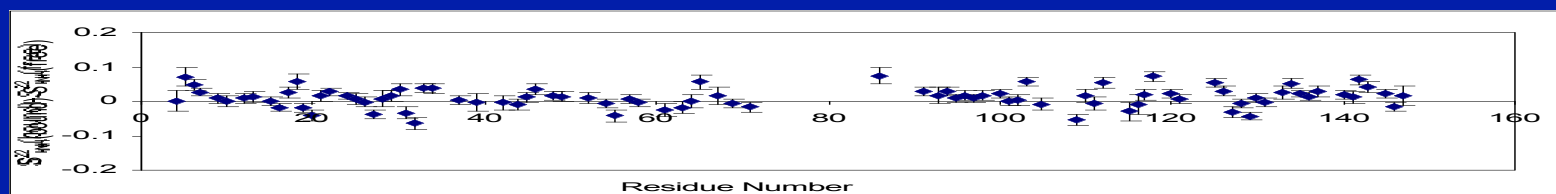
# Dynamics of Calmodulin with and without peptide

Differences in order parameter (bound-minus-free)

CO-Ca

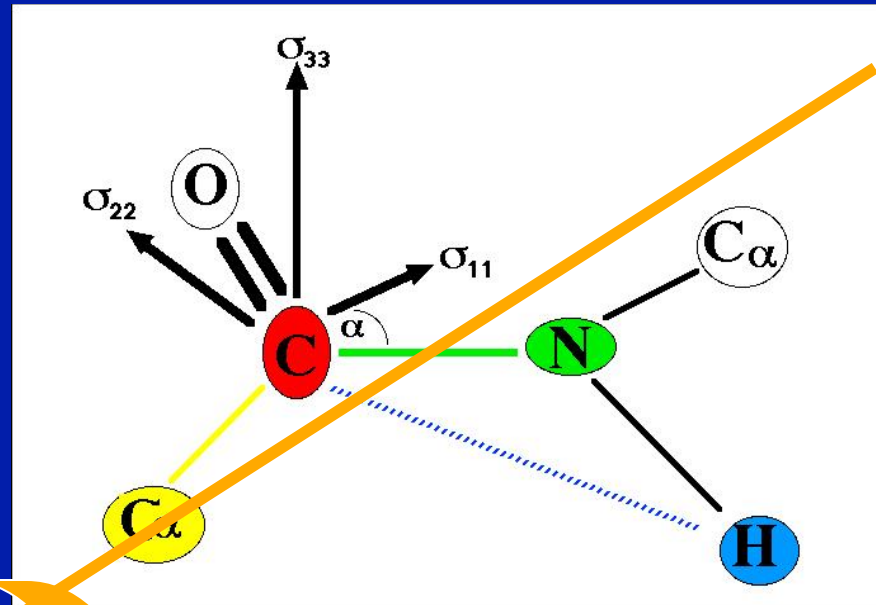


NH



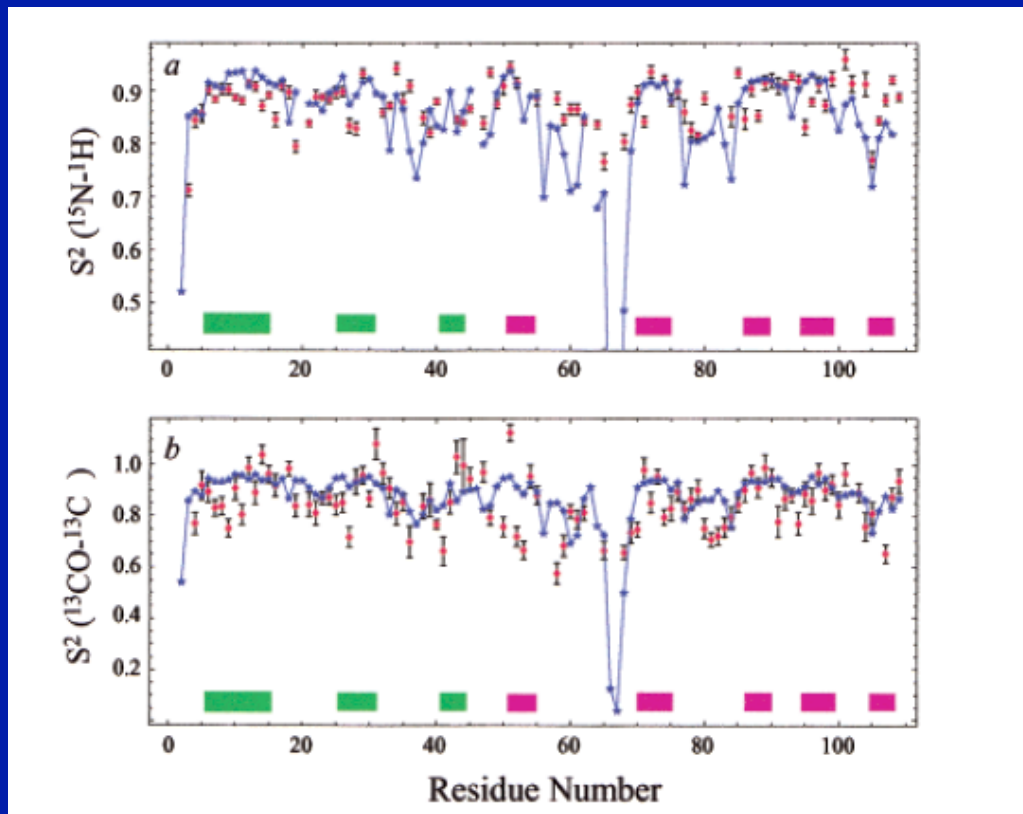
Wang, T, King Frederick, K., Igumenova, T.I., Wand, A.J. and Zuiderweg, E.R.P.  
Changes in Calmodulin backbone dynamics upon ligand binding revealed by cross-correlated NMR relaxation measurements, *J. Am.Chem.Soc.* 127, 828-829 (2005)

MD: peptide-plane Dynamics is dominated by “crank-shaft” motions around the CA-CA direction. This would imply that CO-CA order parameter should be larger than N-H order parameters



Y. Pang, EZ, Biochemistry, 41, 2655 (2002)

However we generally find the average CO-Ca order parameter to be smaller than the NH order parameter



Data points are experimental  
Blue line is a 1.6 ns MD simulation using the CHARMM-param22 forcefield, binase in water.

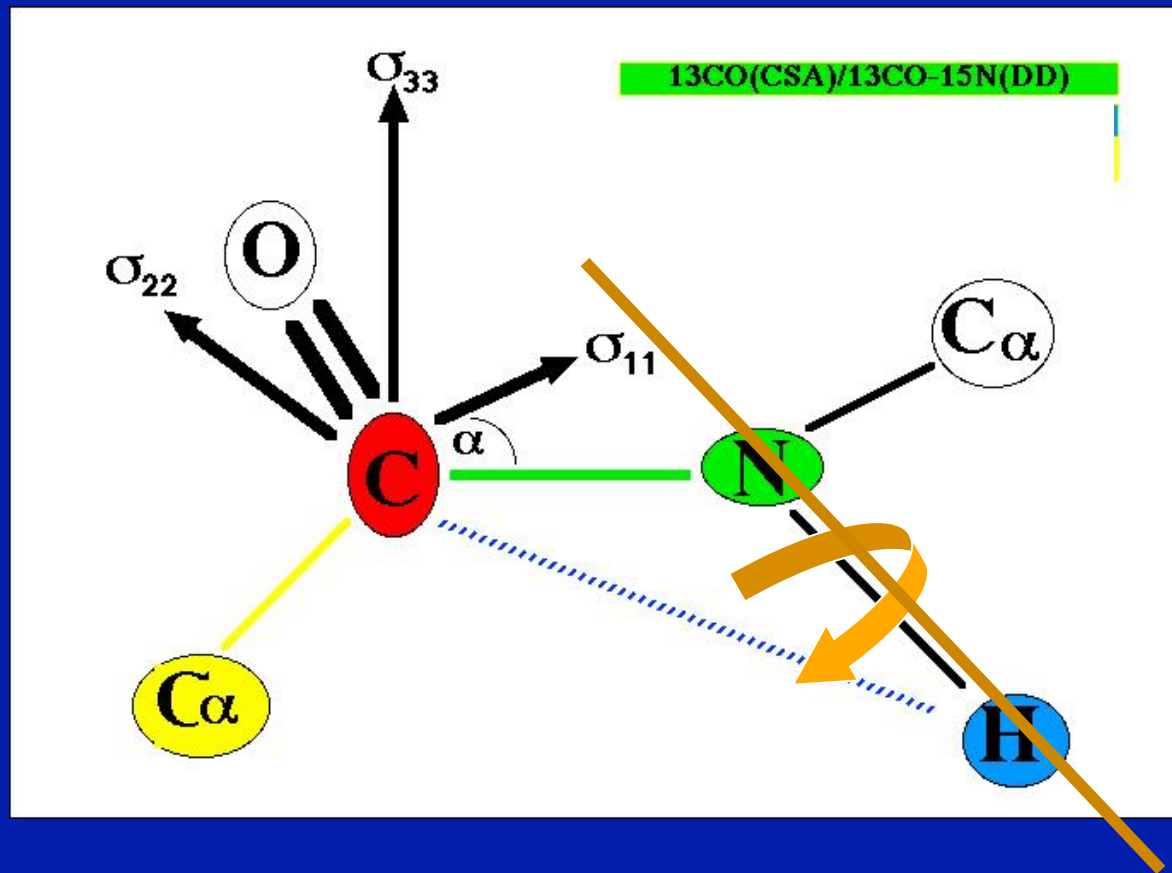
Pang, A, Buck, M., and Zuiderweg, E.R.P. Backbone Dynamics of the Ribonuclease Binase Active Site Area using Multinuclear ( $^{15}\text{N}$  and  $^{13}\text{CO}$ ) NMR Relaxation and Computational Molecular Dynamics, *Biochemistry*, 41, 2655-2666 (2002)

and the COCA order parameter decreases faster than the NH order parameter upon increase in temperature

	Ratio $S^2_{\text{NH}}(303) / S^2_{\text{NH}}(278)$	Ratio $S^2_{\text{COCa}}(303) / S^2_{\text{COCa}}(278)$
Binase	0.98	0.90
Ubiquitin	0.97	0.87
Cyt-b5	0.99	0.89

Wang, T., Cai, S. and Zuiderweg, E.R.P. Temperature dependence of anisotropic protein backbone dynamics J. Am. Chem. Soc. 125, 8639-8643 (2003).

Thus, there must be significant motion affecting the CO-CA order more than the NH order parameter – in a rigid peptide plane, only a motion around the NH vector would do this



However, such a correlated motion is unlikely.

We currently favor the idea that there is sufficient flexibility in the peptide plane that re-orientational motions affecting the Ca atom would not necessarily affect the N-H bond vector.

There is QM and IR evidence that such may indeed be the case

(Mannfors, B. E.; Mirkin, N. G.; Palomäki, K.; Krimm, S. *J. Phys. Chem.* **2003**, *A107*, 1825-1832.)

*Better QM-based forcefields for MD simulations are needed to settle this issue*



In subsequent research, we have taken a more practical approach: how to get proper order parameters for the motions that affect the CO?

Effective Lipari–Szabo order parameters and local correlation times for relaxation vectors of protein  $^{13}\text{C}$ O nuclei are extracted from a  $^{13}\text{C}$ O- $R_1$  experiment, a transverse  $^{13}\text{C}$ O CSA/ $^{13}\text{C}$ O- $^{13}\text{C}$ a CSA/dipolar cross correlation and a transverse  $^{13}\text{C}$ O CSA/ $^{13}\text{C}$ O- $^{15}\text{N}$  CSA/dipolar cross correlation experiment.

Given the global rotational correlation time from  $^{15}\text{N}$  relaxation experiments, the program COMFORD fits the  $^{13}\text{C}$ O data to an effective order parameter  $S^2_{\text{CO}}$ , an effective local correlation time and the orientation of the CSA tensor with respect to the molecular frame.

Wang, T., Weaver, D.S., Cai, S., Zuiderweg, E.R.P.

Quantifying Lipari-Szabo model-free parameters from  $^{13}\text{C}$ O NMR relaxation experiments. *J Biomol NMR*. 36, 79-102. (2006)

We are trying to formulate a NMR relaxation paradigm that works for larger proteins.

The standard  $^{15}\text{N}$ -based paradigm does not work very well for proteins with  $t_c > 15$  ns.

The most problematic is the  $^1\text{H} \rightarrow ^{15}\text{N}$  NOE experiment, which when properly performed, may take a month of instrument time.

There also problems with the  $R_2$  experiments – for the larger proteins one uses higher-field instruments which exacerbate  $R_{ex}$  and the variations in  $^{15}\text{N}$  CSA relaxation.

A  $^{15}\text{N}$  paradigm suitable for larger proteins we try to develop uses

$^{15}\text{N}$   $R_1$

$R_2$   $^{15}\text{N}$ -CSA/  $^{15}\text{N}$ - $^1\text{H}$  DD cross correlation

$R_1$   $^{15}\text{N}$ -CSA/  $^{15}\text{N}$ - $^1\text{H}$  DD cross correlation

Model computations suggest that we can reliably fit for  $\tau_c$ ,  $S^2$ ,  $\tau_{\text{loc}}$  and the  $^{15}\text{N}$  CSA out of of these upto  $\tau_c$  30 ns.

What is holding us back?

Lousy funding climate.

## Experimental

$^{15}\text{N}$   $R_1$ : easy to run, easy on the probe, easy to interpret

$R_2$   $^{15}\text{N}$ -CSA/  $^{15}\text{N}$ - $^1\text{H}$  DD cross correlation:  
easy to run, easy on the probe, easy to interpret

$R_1$   $^{15}\text{N}$ -CSA/  $^{15}\text{N}$ - $^1\text{H}$  DD cross correlation:  
easy to run, easy on the probe, difficult to interpret

$R_1$   $^{15}\text{N}$ -CSA/  $^{15}\text{N}$ - $^1\text{H}$  DD cross correlation:

Is difficult to interpret because  $^1\text{H}$ - $^1\text{H}$  NOE effects enter into the cross-relaxation matrix.

Earlier, we have tried to measure the NOEs and back-fit these in the relaxation matrix

Wang, L. Kurochkin, A.V. and Zuiderweg, E.R.P. An iterative fitting procedure for the determination of longitudinal NMR cross-correlation rates. *J. Magn. Reson.*, 144, 175-185 (2000)

More recently, we have been able to separate the effects using symmetric reconversion

Weaver, D.S. and Zuiderweg, E.R.P. a TROSY NMR experiment measuring longitudinal relaxation interference. *J Chem Phys*, 128 155103 (14 pg) (2008)

We thus now have available the  $R_1$   $^{15}\text{N}$ -CSA/  $^{15}\text{N}$ - $^1\text{H}$  DD cross correlation rates, and are able to carry out the  $^{15}\text{N}$  relaxation on larger proteins.

What started as a nasty interference, the  $^1\text{H}$ - $^1\text{H}$  relaxation rates extracted from the  $R_1$   $^{15}\text{N}$ -CSA/  $^{15}\text{N}$ - $^1\text{H}$  DD can be interpreted in terms of dynamics themselves:

Weaver DS, Zuiderweg ER. Protein proton-proton dynamics from amide proton spin flip rates. *J Biomol NMR*. 45, 99-119. (2009)

The general applicability of this still needs to be further validated with MD runs.

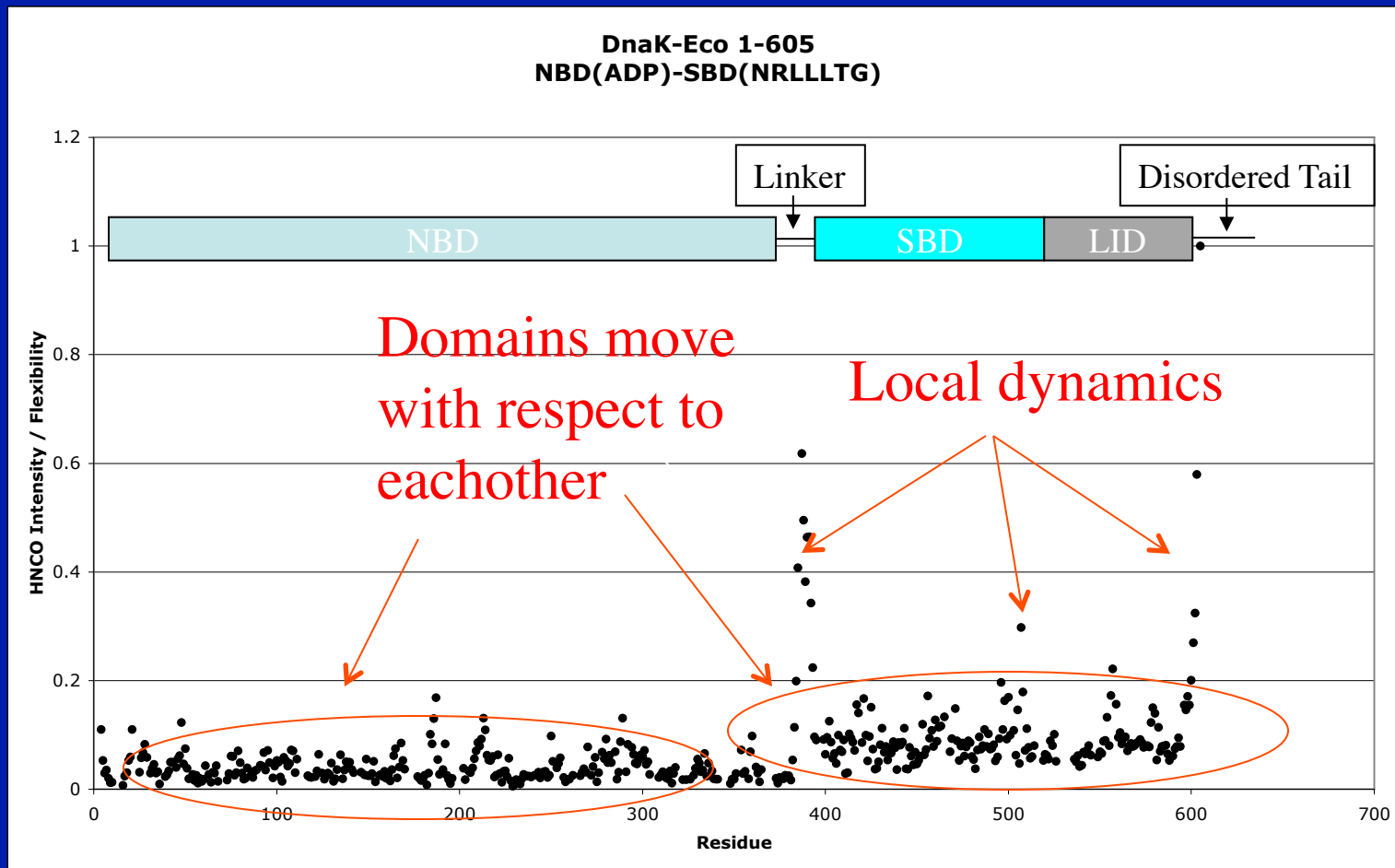
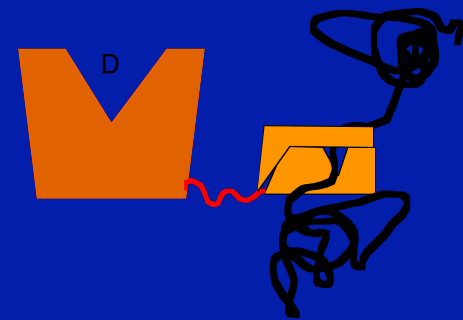
Another approach to measure dynamics in proteins in a semi-quantitative way, is to just measure the intensity of cross peaks in HSQC, TROSY or HNCOC.

Areas with low order parameters stand out with high peak intensities, areas with  $R_{ex}$ , stand out with low peak intensities.

This is almost exclusively due to variations in amide proton  $R_2$  rates. Simulations show that dynamical effects on these rates have a much larger effect than variations in the local environment, provided one chooses an appropriate perdeuteration level.

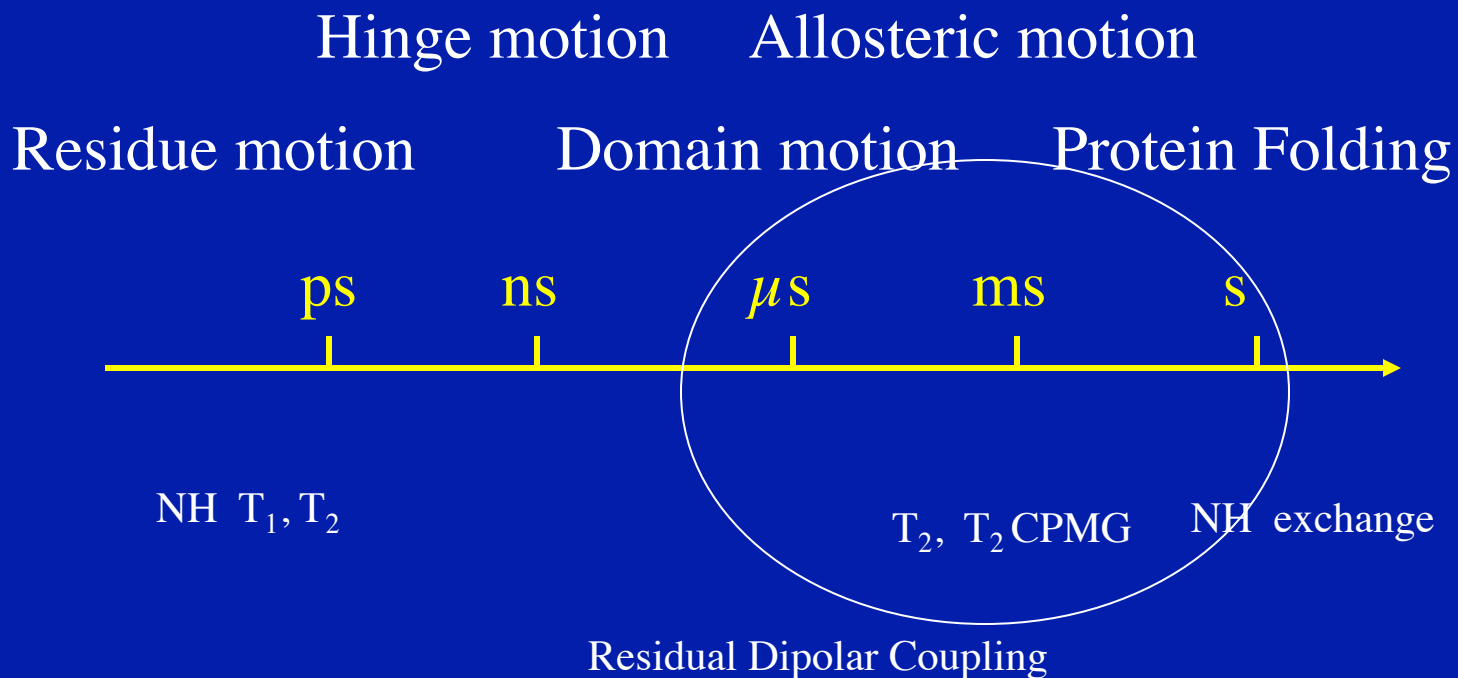
An example is shown for the dynamical properties of a large protein  
(to be submitted)

# Dynamical Properties of a 70 kDa protein

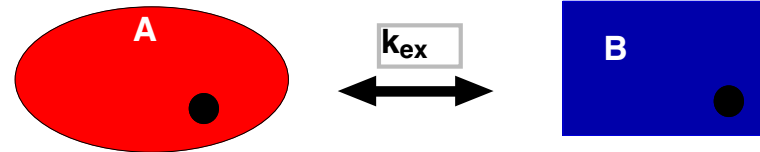




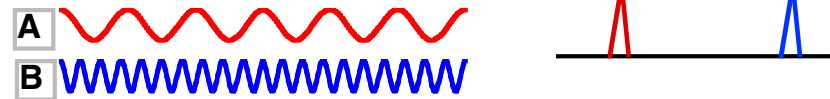
# Common NMR relaxation



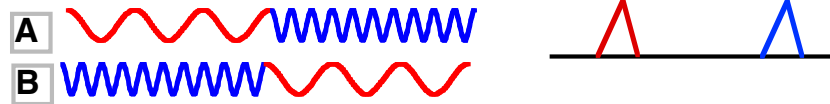
# Exchange Broadening and dynamics



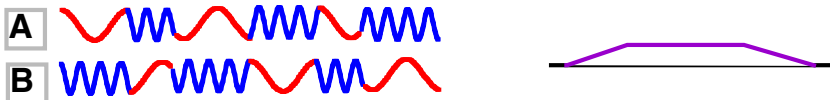
$k_{ex} = 0$



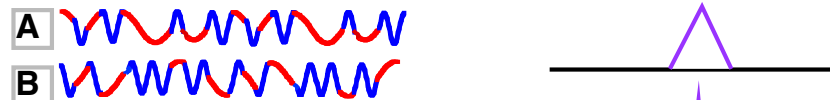
$k_{ex} \ll |\omega_a - \omega_b|$



$k_{ex} \sim |\omega_a - \omega_b|$



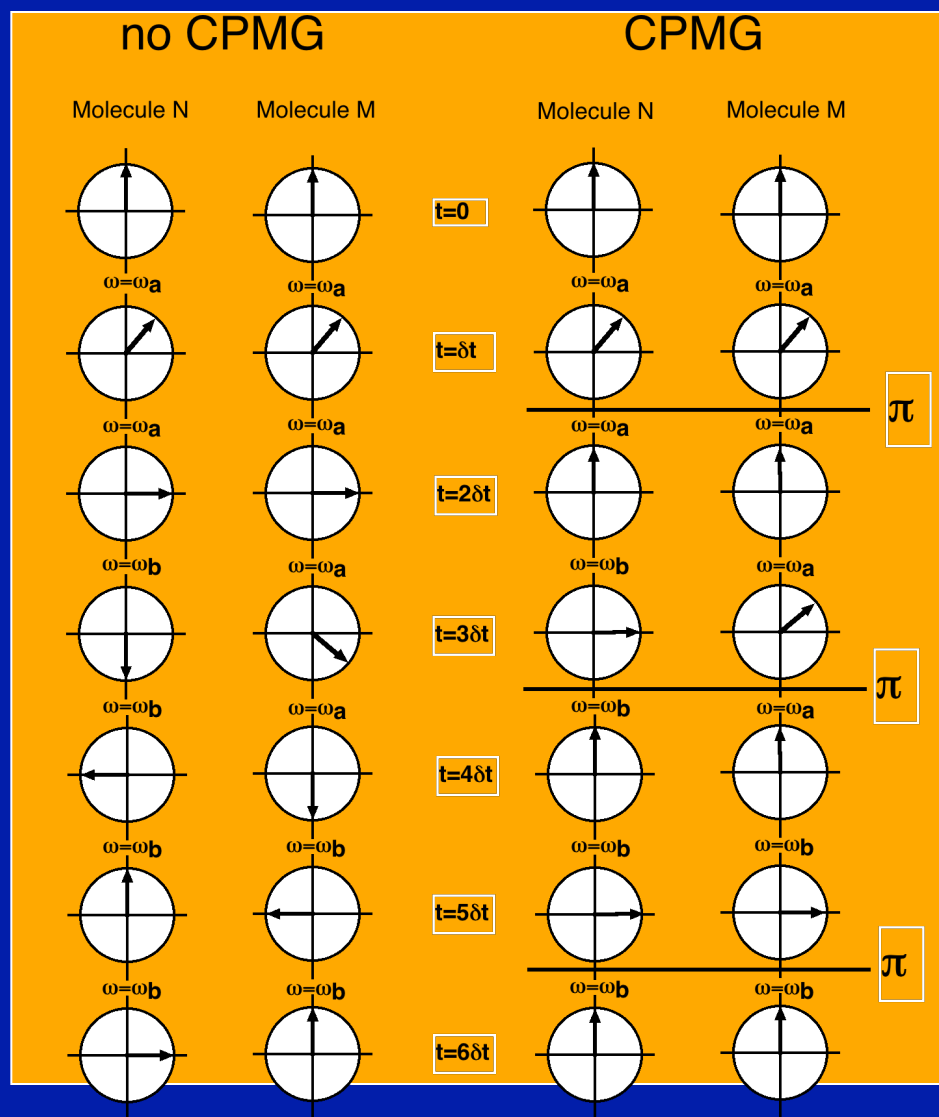
$k_{ex} \sim |\omega_a - \omega_b|$



$k_{ex} \gg |\omega_a - \omega_b|$



# How to detect milli/micro second dynamics

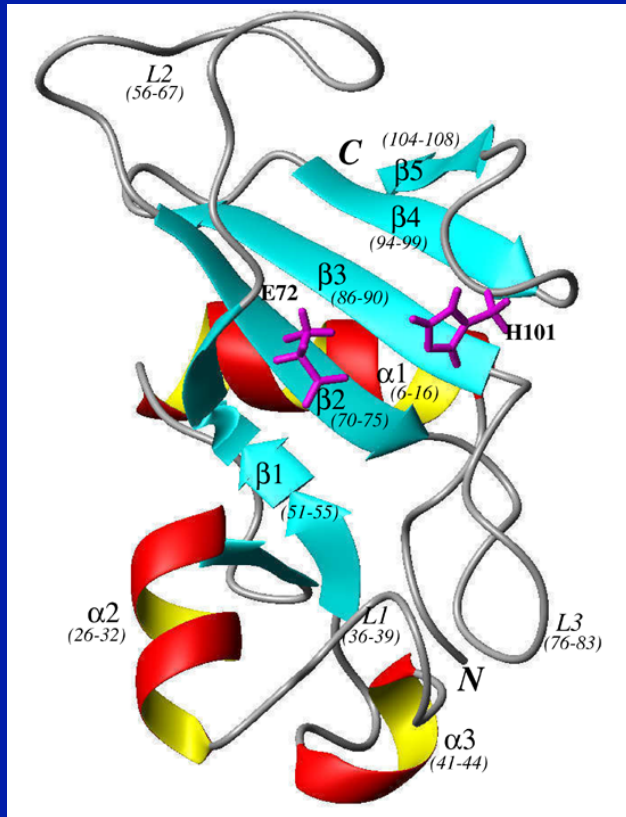


# Functional dynamics in the active site of the ribonuclease Binase

Wang, L., Pang, Y., Holder, T., Brender,  
J.R., Kurochkin, A, Zuiderweg, E.R.P.

Proc. Natl. Acad. Sci. USA, 98, 7684-7689  
(2001)

# Binase = Barnase

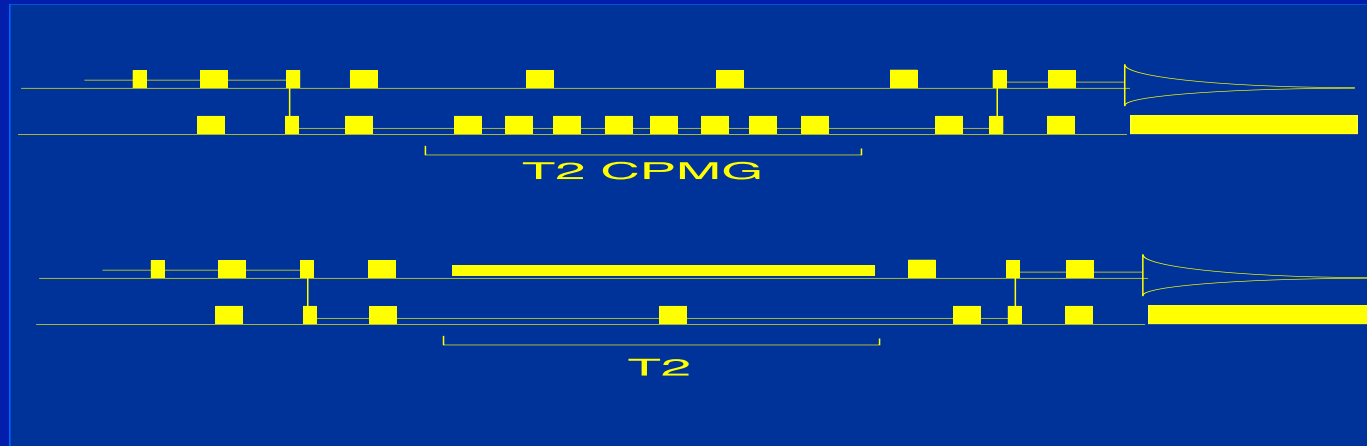
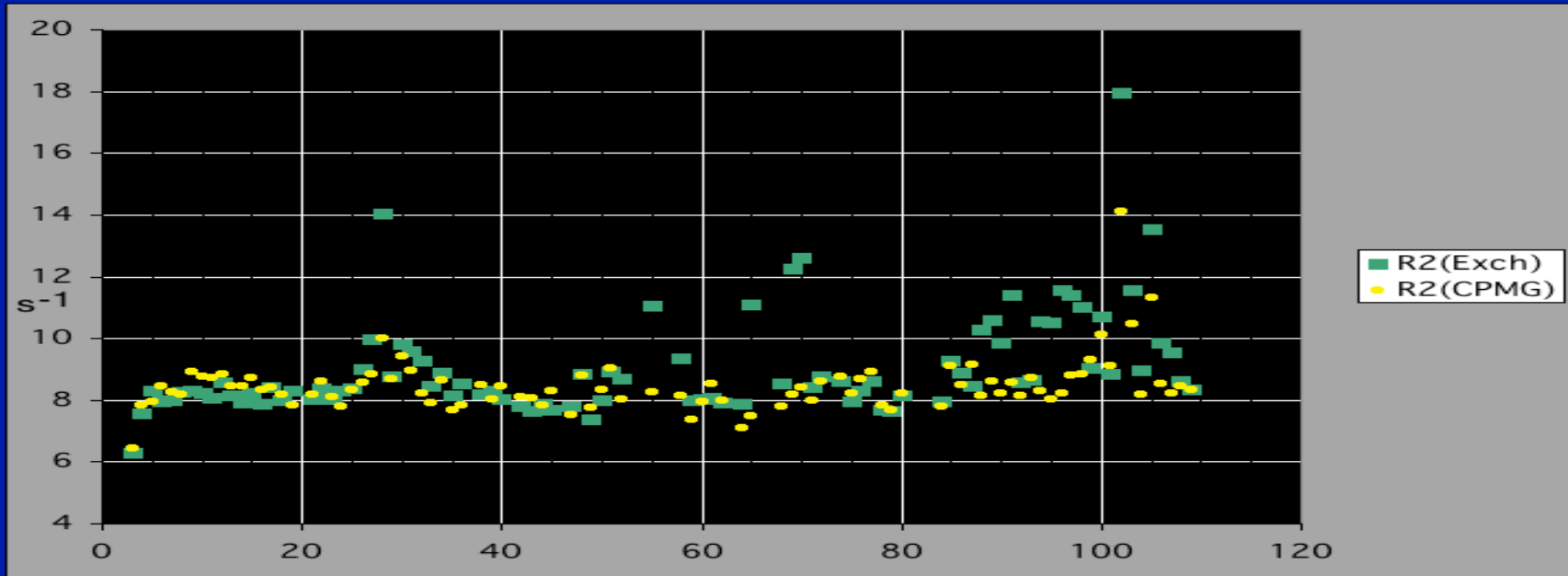


109 residues

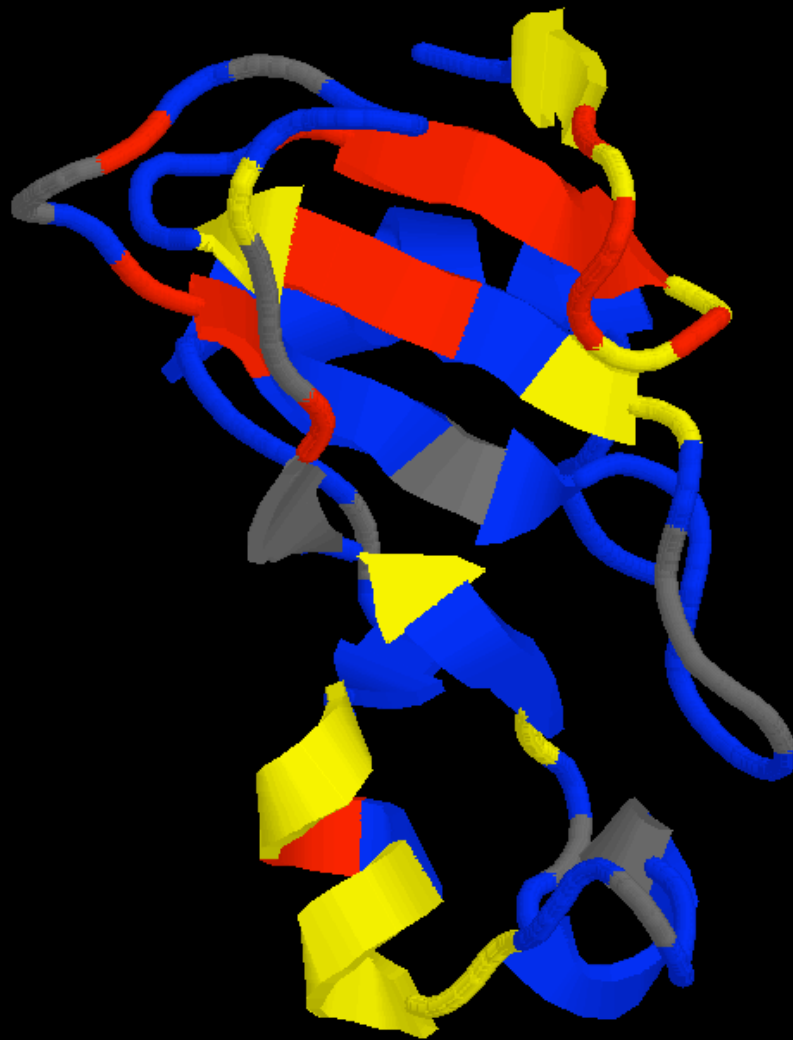
Guanyl-specific  
ribonuclease

17 a.a. difference  
with barnase

# Conformational exchange broadening in Binase



# Binase MD av NMR



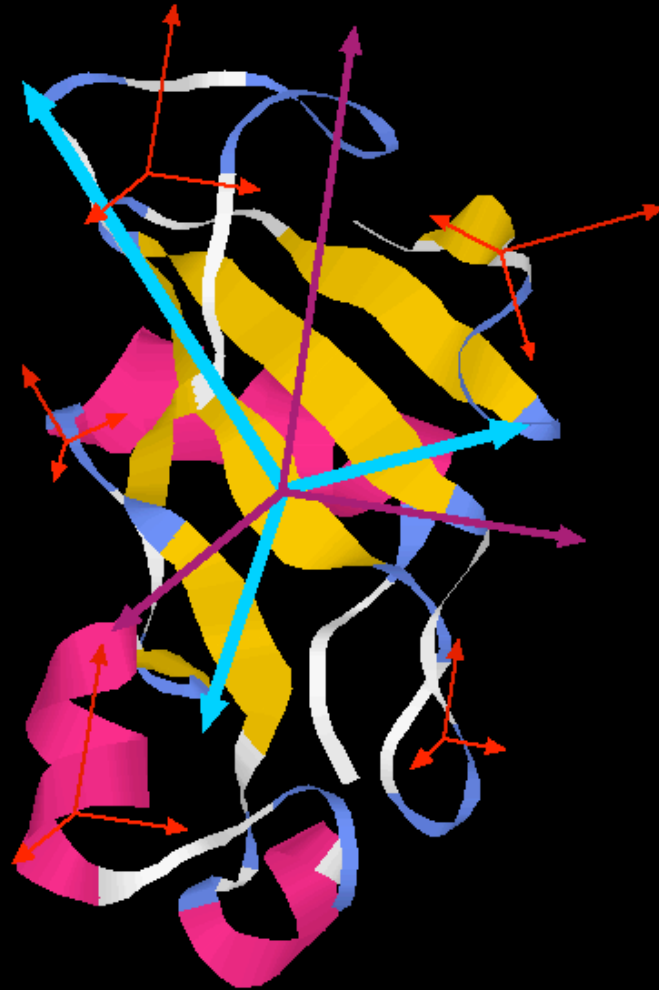
$R_{ex} < 0.5$

$0.5 < R_{ex} < 1.5$

$R_{ex} > 1.5$

no data

Binase MD averaged NMR structure



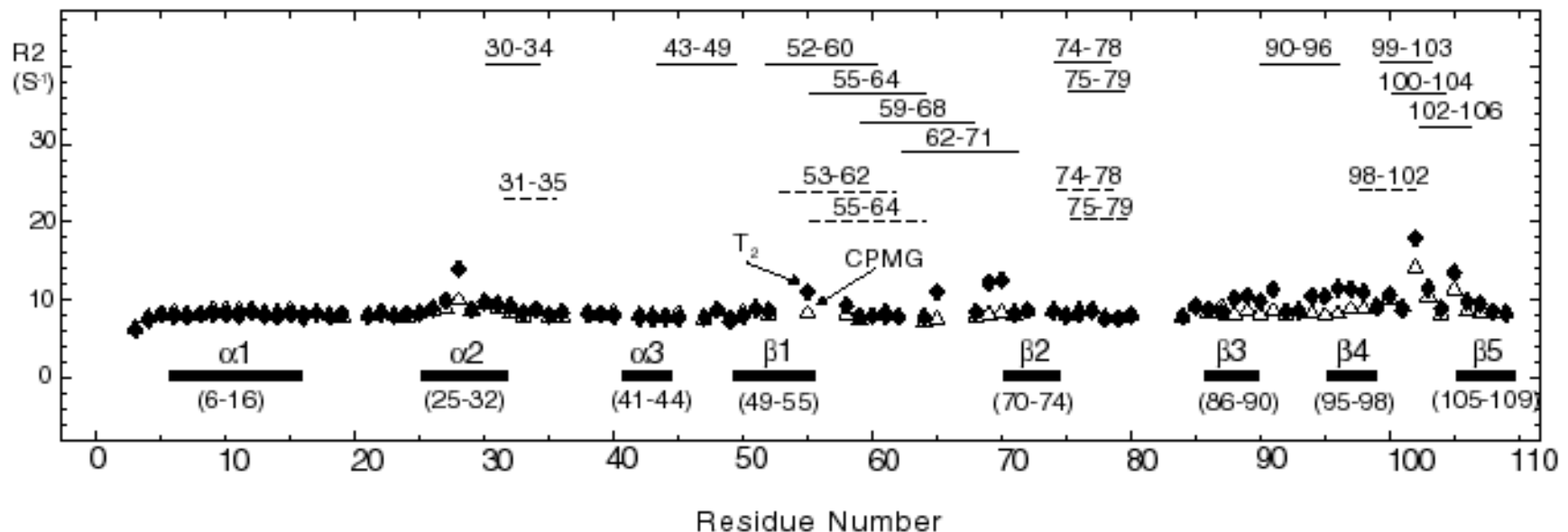
PDB Frame

Global Allign Frame

Local Allign Frames

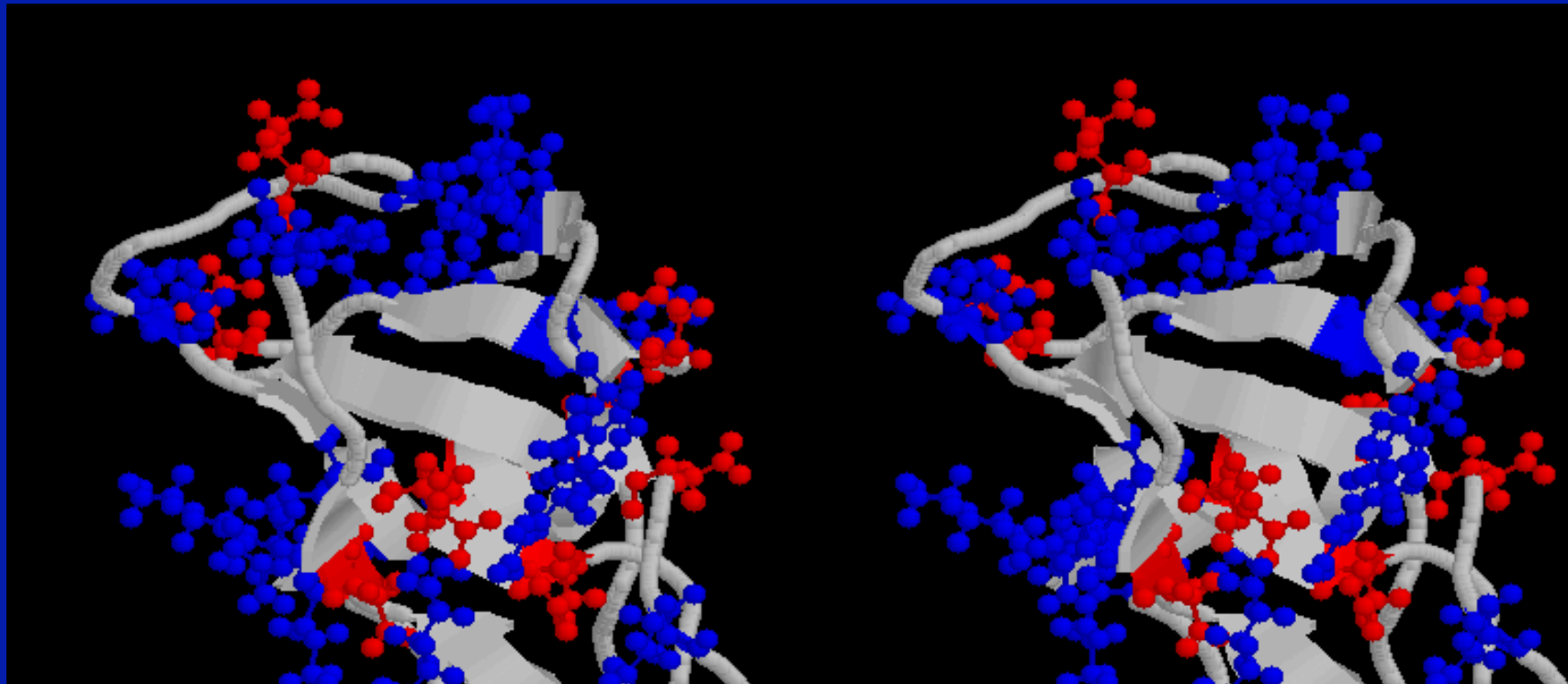


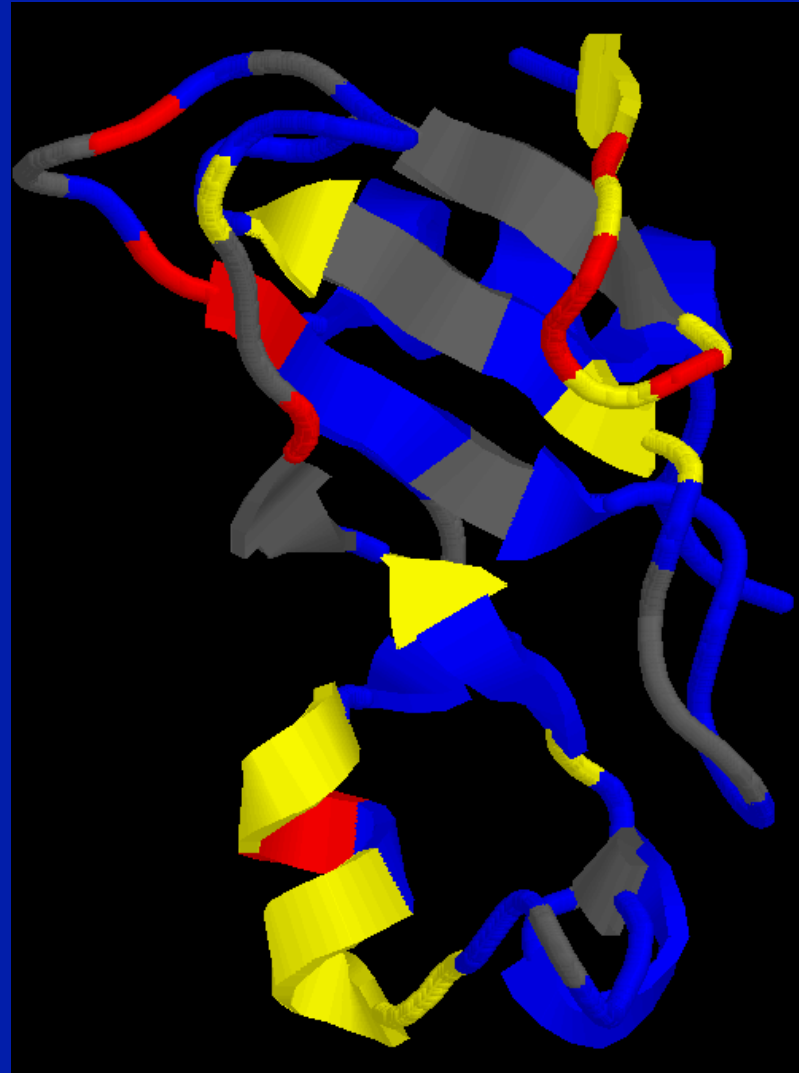
# Exchange Broadening and RDC Tensor Deviations



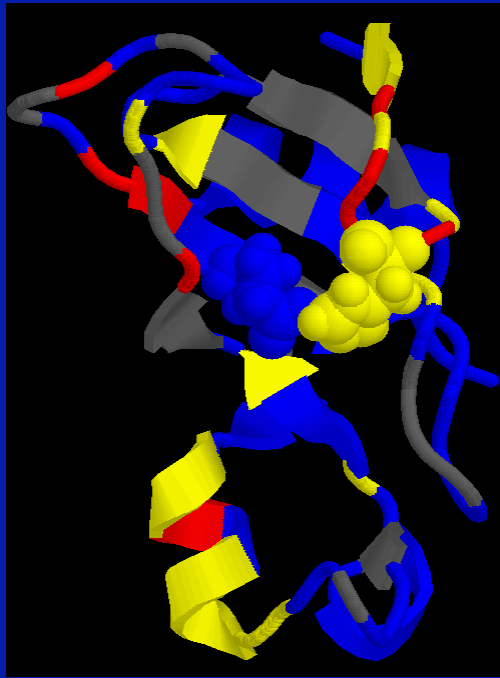
RDC tensors deviate in all areas where we see exchange broadening, except for beta 3. This indicates that  $\beta_3$  is not moving.

Exchange broadening on the beta sheet is an induced effect

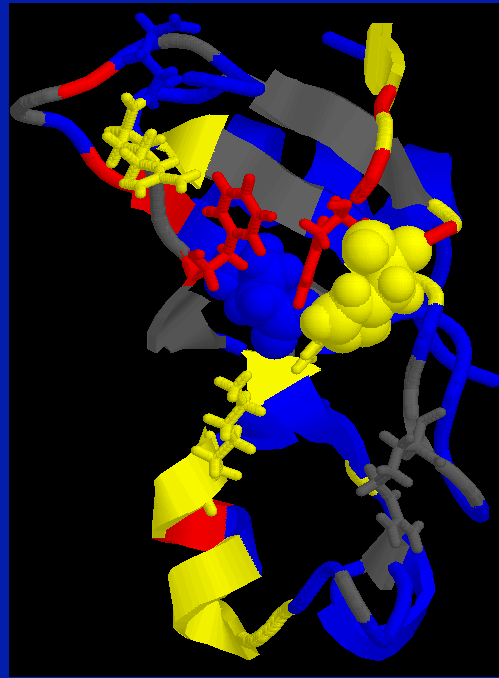




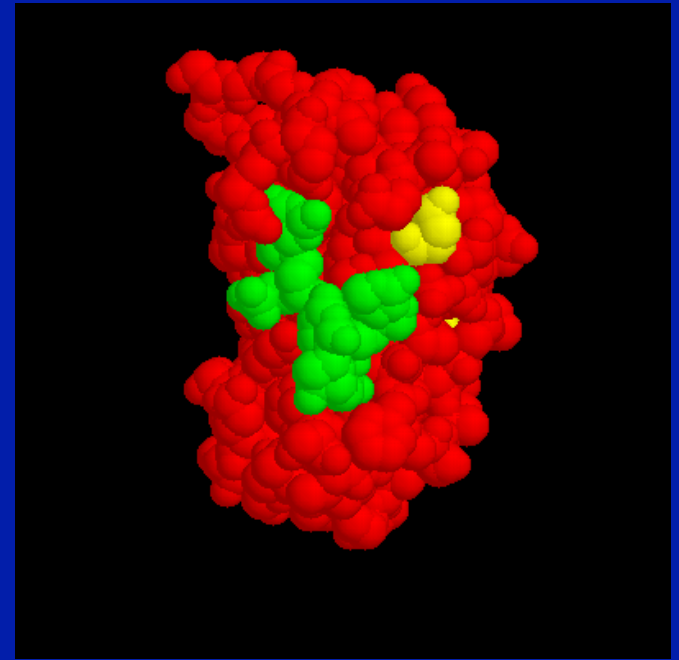
Eliminating the induced broadening from the picture



Catalytic  
residues



Residues that interact with substrate



i.e. residues important to the protein function move

Where it matters it moves!

Maximum turn over rate for these enzymes is  $1400 \text{ s}^{-1}$

	substrate	$k_{\text{cat}}$	$K_M$	$k_{\text{cat}}/K_M$
		$\text{s}^{-1}$	$\mu\text{M}$	$\text{M}^{-1}\text{s}^{-1}$
Binase	GpU	0.4	230	$1.7\text{e}3$
Barnase	GpU	4.3	150	$2.9\text{e}4$
Binase	Poly-I	141	80	$1.8\text{e}6$
Barnase	Poly-I	1413	130	$1.1\text{e}7$

from Schulga et al, Prot. Engin. 11, 775, 1998

## NMR-detected dynamics is at roughly the same time scale

- **Conformational exchange rates in Binase (s<sup>-1</sup>).**
- Gln 28     $3.8 \times 10^3 \pm 600$
- Phe 55     $2.4 \times 10^3 \pm 120$
- Trp 70     $2.7 \times 10^3 \pm 200$
- Leu 97     $2.7 \times 10^3 \pm 700$
- Tyr 102    $4.7 \times 10^3 \pm 800$
- Ala 103    $6.1 \times 10^3 \pm 1200$

# Functional Dynamics?

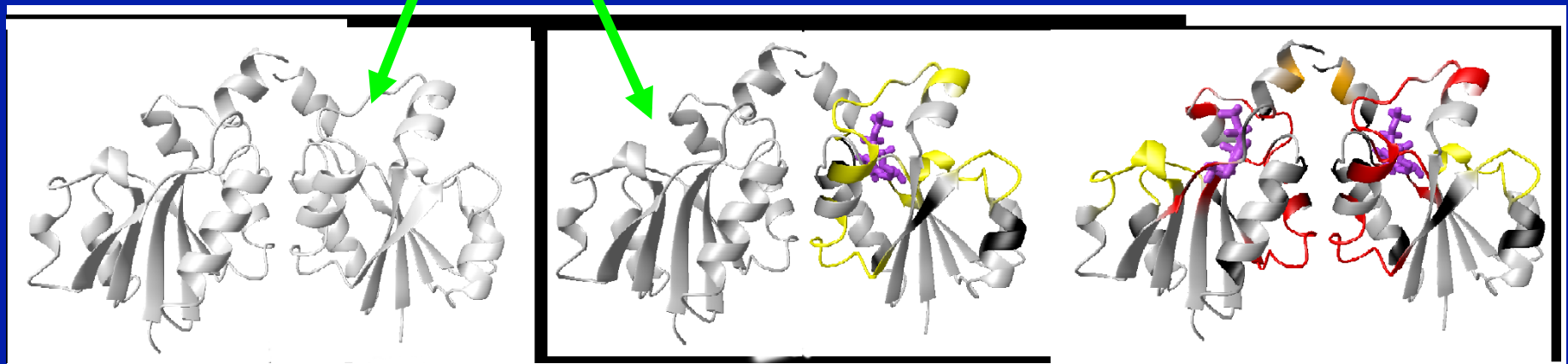
- Apparently,  $k_{\text{cat}} \text{ max}$  corresponds to the flap dynamics rate
- Apparently,  $k_{\text{cat}} \text{ max}$  reflects product release rate (exit rate)

# GCTase, a negatively cooperative enzyme

Binding sites identical,  
Expect identical local  
binding free energies

Thus:

2.7 Kcal/M of binding  
free energy lost on  
interface



First CTP

$\Delta G = -7.3$  Kcal/M

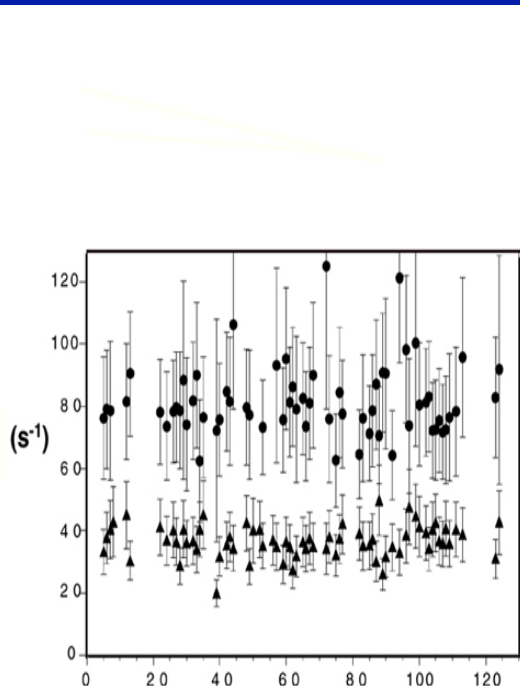
Second CTP

$\Delta G = -4.6$  Kcal/M

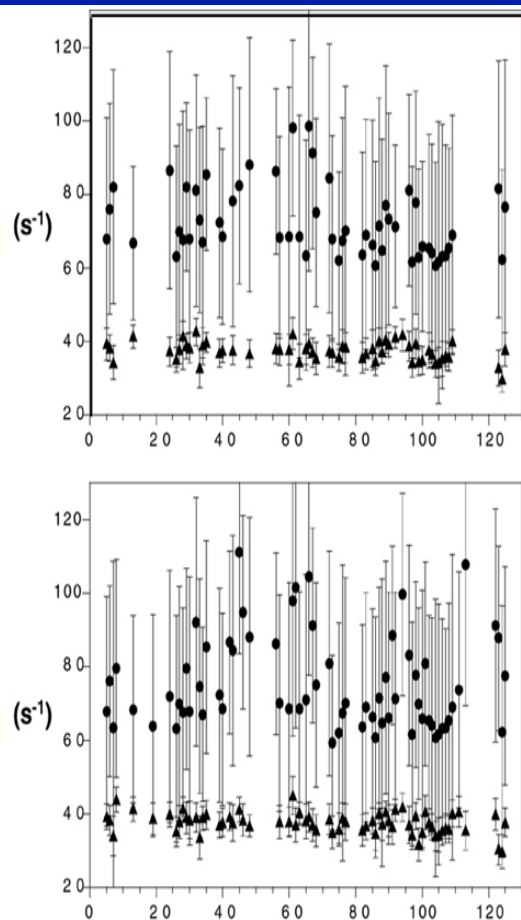
Stevens, S.Y., Sanker, S., Kent, C. and Zuiderweg, E.R.P. Delineation of the allosteric mechanism for a cytidyltransferase exhibiting negative cooperativity, *Nature Structural Biology* 8, 947-952 (2001)



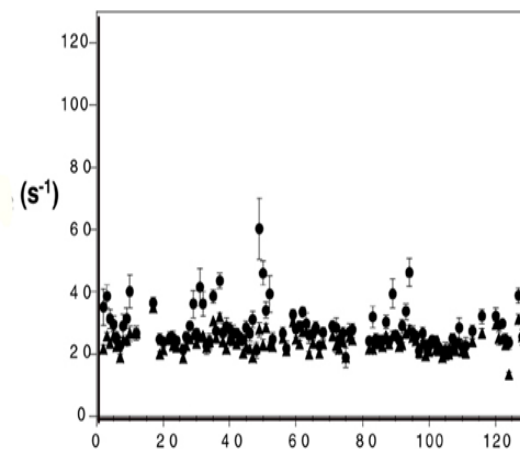
# $^{15}\text{N}$ $R_2$ relaxation with and without exchange broadening suppression



*GCT*



*GCT(CTP)*



*GCT(CTP)<sub>2</sub>*

*GCT*       $\longrightarrow$       *GCT(CTP)*       $\longrightarrow$       *GCT(CTP)<sub>2</sub>*

*Dynamic*       $\longrightarrow$       *Dynamic*       $\longrightarrow$       *Rigid*

$\Delta S = 0$

$\Delta S = \text{neg}$

Therefore, the allosteric free energy  
of negative cooperativity  
has an **entropic** component.

## Compare dynamic NMR studies of Calbindin

Mäler, L., Blankenship, J., Rance, M. & Chazin, W. J. *Nature Struct. Biol.* **7**, 245 – 250 (2000).

*Calb*       $\longrightarrow$       *Calb*( $Ca^{2+}$ )       $\longrightarrow$       *Calb*( $Ca^{2+}$ )<sub>2</sub>

*Dynamic*       $\longrightarrow$       *Rigid*       $\longrightarrow$       *Rigid*

$\Delta S = \text{neg}$

$\Delta S = 0$

The allosteric free energy of  
*positive cooperativity*  
has an **entropic** component.

# Students associated with dynamics research in the Zuiderweg lab:

Mark Fischer (1992-1998 Ph.D.)

Yuxi Pang (1997-2001 Ph.D.)

Daniel Weaver (2004-2009 Ph.D.)

Weidong Hu, Ph.D. (1994-1997)

Lei Zheng, Ph.D. (1995-1997)

Ananya Majumdar, Ph.D. (1997)

Maurizio Pellecchia, Ph.D. (1998-1999)

Shawn Stevens, Ph.D. (1997-2003)

Lincong Wang, Ph.D. (1998-2001)

Sheng Cai, Ph.D. (2001-2004)

Tianzi Wang, Ph.D. (2001-2005)

# Supported by

NSF MCB 9513355 2/1/96-1/31/99

Study of Isotropic and Anisotropic motions in proteins  
involving  $^{13}\text{C}$  and  $^{15}\text{N}$  NMR relaxation

NSF MCB 0135330 2/1/99-1/31/07

Motional modelling by NMR