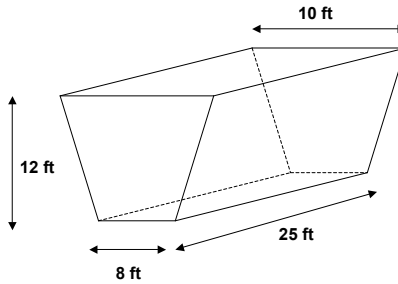


8.5: Applications to Physics

Problems

1. The underground reservoir, pictured below, is filled to a depth of 9 feet with water. The density of water is 62.4 lbs/ft^3 and the tank is buried 5 feet below ground level.



- (a) Write an expression that approximates the work required to lift a horizontal slice of water that is Δy feet thick and is located y_i feet below ground level to a sluice that is 10 feet above ground level. Include units.
- (b) Write an integral for the total amount of work required to pump all the water from the tank to the sluice located 10 feet above ground. Include units.
2. A scale is built by placing a metal plate on top of a spring.
- (a) An object weighing 200 lbs is placed on top of the scale. If the object compresses the spring by 5 in, find the spring constant k such that the force of the spring is $F = -kx$. Include units.
- (b) How much work is done by the object in compressing the spring?
3. A cylindrical tank is buried 15 m below ground and oriented so that the circular ends are vertical. The tank has a radius of 2 m and a length of 20 m and is filled with a gasoline with a density of $\delta = 719.7 \text{ kg/m}^3$. Compute the work required to pump the gasoline to ground level. Include units. [You may use your calculator]

Answers

- 1.** (a) $62.4(25) \left(-\frac{1}{6}y_i + \frac{65}{6} \right) (y_i + 10) \Delta y$ lb ft (b) $\int_8^{17} 62.4(25) \left(-\frac{1}{6}y + \frac{65}{6} \right) (y + 10) dy$ lb ft **2.** (a) $k = 40$ lbs/in (b) 41.66 lb ft **3.** 30,134,622.03 J or 30.1346 MJ