Recruitment of Foreigners in the Market for Computer Scientists in the US

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Abstract

This paper presents a dynamic model that characterizes the labor market for computer scientists. Unlike traditional models for scientists and engineers, in our model firms can incur costs to recruit foreigners who are potentially more productive (or relatively less paid) than US workers. We calibrate the model using data from the 1990s (the internet boom) to the early 2000s (a slump in the industry). Using the calibrated model, we conduct counterfactual simulations where firms have limits on foreign recruitment. For a range of labor demand elasticities, our simulations suggest that wages for computer scientists would have been 2.8-3.8% higher, and the number of Americans employed as computer scientists would have been 7.0-13.6% higher in 2004 if firms could not hire more foreigners than in 1994. In contrast, total CS employment would have been 3.8-9.0% lower, and consequently output smaller if firms had these restrictions on foreign recruitment.

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1 Introduction

An increasingly high proportion of the scientists and engineers in the US were born abroad. At a very general level, the issues that come up in the discussion of high skilled immigration mirror the discussion of low skilled immigration. The most basic economic arguments suggest that both high-skill and low-skill immigrants: (1) impart benefits to employers, to owners of other inputs used in production such as capital, and to consumers, and (2) potentially, impose some costs on workers who are close substitutes (Borjas (1999)). On the other hand, the magnitude of these costs may be substantially mitigated if US high skilled workers have good alternatives to working in sectors most impacted by immigrants (Peri and Sparber (2011), Peri et al. (2013)). Additionally, unlike low skilled immigrants, high skilled immigrants contribute to the generation of knowledge and productivity through patenting and innovation. Doing so both serves to shift out the production possibility frontier in the US and may also slow the erosion of the US comparative advantage in high tech (Freeman (2006); Krugman (1979)).

In this paper we study the impact of high skilled immigration on the labor market for computer scientists (CS) in the US, during the Internet boom of the 1990s, and the subsequent slump in the early 2000s. During this period, we observe a substantial increase in the number of temporary non-immigrant visas awarded to high skilled workers, and individuals with computer-related occupations becoming the largest share of H-1B visa holders (US General Accounting Office, 2000). Given these circumstances, it is of considerable interest to investigate how the influx of foreigners affected the labor market outcomes for US computer scientists during this period.

In order to evaluate the impact of immigration on CS domestic workers, we construct a dynamic model that characterizes the labor supply and demand for CS workers during this period. We build into the model the key assumption that labor demand shocks, such as the one created by the dissemination of the Internet, can be accommodated by three sources of CS workers: recent college graduates with CS degrees, US residents in different occupations who switch to CS jobs, and skilled foreigners. Furthermore, firms face a trade-off when deciding to employ immigrants: foreigners are potentially either more productive or less costly than US workers, but there are extra recruitment costs associated with hiring them.

The approach we take in this paper is distinctly partial equilibrium in nature – we focus on the market for computer scientists and ignore any wider impacts that high skilled immigration might
have on the U.S. economy (Nathan (2013)). While we believe this approach can potentially be used to understand the impact that the availability of high skilled foreign labor might have had for this market, this approach precludes any analysis of the overall welfare impact of the H-1B program in particular or high skilled immigration more generally.

The predictions of the model on the impacts of immigration on wages depend on the elasticity of labor demand for computer scientists. As long as the demand curve slopes downwards, the increased availability of foreign computer scientists will put downward pressure on the wages for computer scientists in the US. However, as we discuss further in Section 4.4, there are a number of considerations that might lead us to think otherwise in the case of computer scientists. First, even in a closed economy, the fact that computer scientists contribute to innovation reduces the negative effects foreign computer scientists might have on the labor market opportunities for skilled domestic workers. In addition, in an increasingly global world, we might expect that restrictions on the hiring of foreign skilled workers in the US would lead employers to increase the extent to which they outsource work. Indeed, if computer scientists are a sufficient spur to innovation, or if it is easy for domestic employers to offshore work, any negative effects that an increase in the number of foreign computer scientists working in the US might have on the domestic skilled workforce would be completely offset by increases in the domestic demand for computer scientists. In the end this issue comes down to the slope of the demand curve for computer scientists.  

We use data on wages, domestic and foreign employment, and undergraduate degree completions by major, during the late 1990s and early 2000s to calibrate the parameters of our model such that it reproduces the stylized facts of the CS market during the period. Next, we use the calibrated model to simulate counterfactuals on how the economy would behave if firms had a restriction on the number of foreigners they could hire. Conditional on our assumptions about the slope of the demand curve for computer scientists, our simulation suggests that had US firms not been able to increase their employment of foreign computer scientists above its 1994 level, CS wages would be 2.8-3.8% higher in 2004. Furthermore, the number of Americans working in the CS industry would be 7.0-13.6% higher, the total number of CS workers would be 3.8-9.0% lower and the enrollment levels in computer science would be 19.9-25.5% higher than the observed levels in 2004.

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1 In this discussion we are assuming that foreign trained computer scientists are close substitutes for domestically trained ones. If foreign and domestically trained computer scientists are imperfect substitutes for each other, then the impact that the increased immigration will have on domestically trained computer scientists will also depend on the degree of substitutability between computer scientists trained domestically and abroad.
Within the confines of the model, the predictions of our model do not depend on the specific choice we made for non-calibrated parameters, with one important exception. The exception: crowd out in the market for computer scientists depends crucially on the elasticity of demand for their services. Ideally, we would be able to use exogenous supply shifts to identify the slope of the demand curve for computer scientists, while we use exogenous shifts in demand to identify supply curves. We believe that largely exogenous technological breakthroughs in the 1990s increased the demand for computer scientists, allowing us to identify supply curves. In other contexts, researchers have treated the increase in foreign born workers in the US economy as exogenous. However, in the current context, immigration law in the US implies that most of the foreign born and trained individuals who migrate to the US to work as computer scientists do so because they are sponsored by US based firms. Thus, it seems implausible to treat the number of foreign born computer scientists in the US as an exogenous increase in supply. In the end, without credible sources of identifying information, we resort to parametrically varying the elasticity of the demand for computer scientists through, what we will argue is a plausible range, from -1.3 to -4.0.

This paper constitutes a contribution to two different dimensions of the research literature. First, our study can be seen as an extension of the models of the market for scientists and engineers developed by Freeman (1975, 1976) in the 1970s and refined by Ryoo and Rosen (2004) more recently. In Ryoo and Rosen’s model, employers are restricted to hiring recent graduates from US engineering programs. In our model, employers can also hire both foreigners and US based individuals not trained as computer scientists. As a result, the supply of CS workers implied by our model is substantially more elastic than implied by the Ryoo and Rosen model, especially in the short term. More importantly, the substantial number of skilled foreign workers affects how the labor and education markets adjusts to an increase in the demand for skilled labor. Second, our paper relates to the recent literature on the potential impact that the hiring of high skilled immigrants might have on the wages and employment prospects of US natives.

We review this literature in detail, and describe the market for CS workers in section 2. Section 3 presents the dynamic model we build to characterize the market for CS workers when firms can

\footnote{These include the introduction of the World Wide Web, web browsers, and of search engines. During this time, Microsoft developed popular user-friendly operating systems, and Linux and other free and open-source software packages grew to power much of the Internet’s server infrastructure. Sun Microsystems introduced the Java programming language and various service providers made e-mail available to a wider base of consumers. These types of software innovation, along with steady, rapid improvements to computer hardware and reductions in its cost permanently changed the structure and nature of the industry.}
recruit foreigners. In section 4, we describe how we calibrate the parameters of the model and the counterfactual simulations where firms have restrictions on the number of foreigners they can hire. We conclude with section 5 which presents a discussion based on the results of the paper.

2 The Market for Computer Scientists in the 1990s

2.1 The Information Technology Boom of the Late 1990s

During the mid 1990s, we observe the beginning of the utilization of the Internet for commercial purposes in the United States\(^3\) and a substantial increase in the number of Internet users, as presented in Figure 1. US Internet usage grew 47-fold between 1991 and 2001, from less than 3 million to more than 140 million. One indicator of a contemporaneous change in demand for IT workers is the rise of R&D expenditure of firms in both the computer programming services, and the computer related equipment sector. Specifically, the share of total private R&D of the firms of these two industries increased from 19.5% to 22.1% between 1991 and 1998.\(^4\) The entry and then extraordinary appreciation of tech firms like Yahoo, Amazon and eBay provides a further testament to the “boom” in the IT sector prior to 2001.

These technological innovations had a dramatic effect on the labor market for computer scientists. According to the Census, the number of employed individuals working either as computer scientists or computer software developers (CS) increased by 161% between the years 1990 and 2000. As a comparison, during the same period, the total number of employed workers with at least a bachelor degree increased by 27%, while the number of workers in other STEM occupations increased by 14%.\(^5\) Table 1 shows computer scientists as a share of the college educated workforce and the college educated STEM workforce. In each case, the share was rising before 1990, but rises dramatically during the 1990s. Indeed, by 2000 more than half of all STEM workers are computer scientists. In Figure 2, we use the CPS to show a similar pattern, additionally showing that the growth of CS employment started in the second half of the decade - the same period as the dissemination of the Internet. There is no doubt this was a period of employment expansion of the CS

\(^3\) The decommissioning of the National Science Foundation Network in April of 1995 is considered the milestone for introducing nationwide commercial traffic on the Internet. (Leiner et al. (1997)).

\(^4\) Authors’ calculation using Compustat data.

\(^5\) Here and elsewhere our tabulations restrict the analysis to workers with at least a bachelor degree and use the IPUMS suggested occupational crosswalk. Other STEM occupations are defined as engineers, mathematical and natural scientists.
workforce.

On top of employment decisions, there is evidence that Internet innovation also affected educational choices of students. We show in Figure 3 that the number of bachelor degrees awarded in computer science as a fraction of both the total number of bachelor degrees and the number of STEM major degrees increased dramatically during this period. The CS share of total bachelor degrees increased from about 2% in 1995 to more than 4% in 2002. Even when compared to other STEM majors, it is clear from the figure that for college students, the decision to study computer science also responded to the Internet boom.

In addition to affecting employment and enrollment decisions, there is also empirical evidence that computer scientist wages responded to expanding Internet use. From the Census, we observe a 18% increase in the median real weekly wages of CS workers between 1990 and 2000. The CPS presents similar patterns: starting in the year 1994 we observe in Figure 4 that wages of computer scientists increased considerably when compared to both workers with other STEM occupations and all workers with a bachelor degree. In fact, while during the beginning of the 1990s, the earnings of CS workers were systematically lower than other STEM occupations, the wage differential tends to disappear after 1998.6

2.2 The Immigrant Contribution to the Growth of the High Tech Workforce

Employment adjustments in the market for computer scientists happened disproportionately among foreigners during the Internet boom. Evidence for this claim is found in Table 2 and Figure 5, where we use the Census and CPS to compare the share of foreign computer scientists to the share of foreign workers in other occupations.7 In the second half of 1990s, the foreign fraction of CS workers increased considerably more than both the foreign fraction of all workers with a bachelor degree and the foreign fraction of all workers in a STEM occupation. In particular, foreigners were less represented among individuals working as computer scientists than in other STEM occupations in 1994. However, with the dissemination of the Internet in the later years of the decade, foreigners became a more important part of the pool of CS workers, as foreigners comprised 29.6% of the

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6It seems likely to us that wages increased as well for complementary jobs to computer science, such as marketing and sales staff at software companies. But we leave such spillovers for later research.

7Here and elsewhere, we define foreigners as who immigrated to the US after the age of 18. We believe that this definition is a proxy for workers who arrived to the US with non-immigrant visa status.
increase in CS workers.

The growth in the representation of the foreign born among the US computer scientist workforce was fueled by two developments. First, there was a truly dramatic increase in the foreign supply of men and women with college educations in science and engineering fields (Freeman (2009)). To take one important example, in India, the number of first degrees conferred in science and engineering rose from 176 thousand in 1990 to 455 thousand in 2000. Second, the Immigration Act of 1990 established the H-1B visa program for temporary workers in “specialty occupations.” The regulations define a “specialty occupation” as requiring theoretical and practical application of a body of highly specialized knowledge in a field of human endeavor including, but not limited to, architecture, engineering, mathematics, physical sciences, social sciences, medicine and health, education, law, accounting, business specialties, theology, and the arts. In addition, applicants are required to have attained a bachelor’s degree or its equivalent as a minimum.

Firms that wish to hire foreigners on H-1B visas must first file a Labor Condition Application (LCA). In LCA’s for H-1B workers, the employer must attest that the firm will pay the non-immigrant the greater of the actual compensation paid to other employees in the same job or the prevailing compensation for that occupation, and the firm will provide working conditions for the non-immigrant that do not cause the working conditions of the other employees to be adversely affected. At that point, prospective H-1B non-immigrants must demonstrate to the US Citizenship and Immigration Services Bureau (USCIS) in the Department of Homeland Security (DHS) that they have the requisite education and work experience for the posted positions. USCIS then may approve the petition for the H-1B non-immigrant for a period up to three years. The visa may be extended for an additional three years, thus a foreigner can stay a maximum of six years on an H-1B visa, though firms can sponsor H-1B visa holders for a permanent resident visa. An important feature of the H-1B visa is that the visa is for work at the specific firm. As a result, workers are effectively tied to their sponsoring firm.

Since 1990 there has been a cap in the number of H-1B visas that can be issued. Initially this cap was set at 65,000 visas per year. In the initial years of the program, the cap was never reached,

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8 The Immigration and Nationality Act of 1952 established the precursor to the H-1B visa, the H-1. The H-1 non-immigrant visa was targeted at aliens of “distinguished merit and ability” who were filling positions that were temporary. Nonimmigrants on H-1 visas had to maintain a foreign residence. The Immigration Act of 1990 established the main features of H-1B visa as it is known today, replacing “distinguished merit and ability” with the “specialty occupation” definition. It also dropped the foreign residence requirement and also added a dual intent provision, allowing workers to potentially transfer from an H-1B visa to immigrant status.
By the mid-1990s, however, the allocation tended to fill each year on a first come, first served basis, resulting in frequent denials or delays on H-1Bs because the annual cap had been reached. After lobbying by the industry, at the end of the decade, Congress acted to raise the cap first to 115,000 for FY1999 and to 195,000 for FY2000-2003. The cap then reverted to 65,000. Figure 6 shows the growth in the number of H-1 visas issued over the last three decades, estimates of the stock of H-1 visas in the economy each year, and the changes in the H-1B visa cap.

Through the decade of the 1990s, H-1B visas became an important source of labor for the technology sector. The National Survey of College Graduates shows that 55% of foreigners working in CS fields in 2003 arrived in the US on a temporary working (H-1B) or a student type visa (F-1, J-1). Furthermore, institutional information indicates a significant increase in the number of visas awarded to computer related occupations during the 1990s. Numbers from the U.S. General Accounting Office (1992) report show that “computers, programming, and related occupations” corresponded only to 11% of the total number of H-1 visas in 1989. However, with concurrent to the Internet boom, computer scientists became a more significant fraction of individuals that received these type of working visas: according to the U.S. Immigration and Naturalization Service (2000), the number of H-1B visas awarded to computer-related occupation in 1999 jumped to close to two-thirds of the visas, and the Department of Commerce (2000) estimated that during the late 1990s, 28% of programmer jobs went to H-1B visa holders.

While H-1B visas holders represent an important source of computer scientists, they do not represent all foreigners in the country working as computer scientists. A significant number of such foreigners are permanent immigrants, some of whom may have come either as children or as students. Other foreigners enter the US to work as computer scientists in the US on L-1B visas, which permit companies with offices both in the US and overseas to move skilled employees from overseas to the US. While we know of no data showing the fraction of computer scientists working in the US on L-1B visas, substantially fewer L-1(A&B) visas are issued than are H-1Bs.

2.3 The Previous Literature on the Impact of Immigrants on the High Tech Workforce in the US

Critiques of the H-1B program (e.g. Matloff (2003)) argue that firms are using cheap foreign labor to undercut and replace skilled US workers. Even the fiercest critiques of the program do not

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9 The 2000 legislation that raised the cap also excluded Universities and non-profit research facilities from it, and a 2004 change added an extra 20,000 visas for foreigners who received a masters degree in the US.
claim that employers are technically evading the law (Kirkegaard (2005)). Rather, these authors argue that the requirement that firms pay visa holders the prevailing wage is close to meaningless. They claim that firms can describe positions using minimal qualifications for the job, thereby establishing a low “prevailing” wage, and then hire overqualified foreigners into the position. These authors conclude that given the excess supply of highly qualified foreigners willing to take the jobs, and given the lack of portability of the H-1B visa, workers on an H-1B visa are not in a position to search for higher wages.

One way to get a handle on the extent to which H-1B visa holders are being under-paid relative to their US counterparts is to compare foreigners on H-1B visas to those with “green cards,” which are portable. Available evidence suggests that computer scientists holding green cards are paid more than observationally equivalent H-1B visa holders. Using difference-in-difference propensity score matching, Mukhopadhyay and Oxborrow (2012) find that green card holders earn 25.4 percent more than observably comparable temporary foreign workers. Additionally, based on an internet survey, Mithas and Lucas (2010), found that IT professionals with green cards earn roughly 5 percent more than observationally equivalent H-1B visa holders using log earnings regressions. Comparisons between green card and H-1B holders are far from perfect. Green cards are not randomly assigned. Many high skilled workers obtain green cards by being sponsored by their employers after they have been working on an H-1B for a number of years. It seems reasonable to assume that those being sponsored are those that both want to stay in the US and are also amongst those the employer wants to hold onto. These kind of considerations lead us to suspect that, conditional on observables, green card holders are positively selected. Given these considerations, it is somewhat surprising that the observed green card premium is not larger than it is.

While there may be no incontrovertible estimate of the productivity (conditional on earnings) advantage of foreign high skilled labor, simple economic reasons suggests this advantage must exist. US employers face both pecuniary and non-pecuniary costs associated with hiring foreigners. A small GAO survey (U.S. General Accounting Office, 2011) estimated the legal and administrative costs associated with each H-1B hire to range from 2.3 to 7.5 thousand dollars. It seems reasonable to assume that employers must expect some cost or productivity advantage when hiring foreigners. This does not mean that foreign hires are always super stars. The productivity advantage could be quite small, and could involve effort, not ability. However, without some productivity advantage, it is hard to see why employers go through the effort and expense to hire foreigners.
H-1B critics are arguing that, for the reasons discussed above, employers find hiring foreign high skilled labor an attractive alternative and that such hiring either “crowds out” natives from jobs or put downward pressure on their wages. However, as far as we know, critics of the H-1B program have not tried to estimate the magnitude of either of these effects. Recent work by economists have started to fill this void. Kerr and Lincoln (2010) and Hunt and Gauthier-Loiselle (2010) provide original empirical evidence on the link between variation in immigrant flows and innovation measured by patenting - finding evidence suggesting that the net impact of immigration is positive rather than simply substituting for native employment. Kerr and Lincoln (2010) also show that variation in immigrant flows at the local level related to changes in H-1B flows do not appear to adversely impact native employment and have a small, statistically insignificant effect on their wages.

A potential issue with Kerr and Lincoln’s analysis is that the observed, reduced-form outcomes may capture concurrent changes in area specific demand for computer scientists. Kerr and Lincoln fully understand this endogeneity issue. To circumvent the problem, they construct a variable that interacts an estimate for the total number of individuals working on H-1B visas in a county with local area dependencies on H-1Bs. Their hope is that the variation in this variable is driven largely by changes in the cap on new H-1B visas that occurred over the last 20 years. That said, it is unclear the extent to which the variation Kerr and Lincoln use is being driven by variation in the visa cap. Because of the dot com bubble bust in 2000 and 2001, the variation in the H-1B cap is only loosely related to actual number of H-1Bs issued. In addition, it is hard to imagine that the cap was exogenous to the demand for IT workers. Finally, if because of local agglomeration effects, the IT boom was concentrated in areas of the country that were already IT intensive (such as Silicon Valley), then the measure of local dependency would be endogenous.

In the context of an economic model, it is difficult to generate a situation in which there is little crowd out unless demand is very elastic. While there are models of the labor market which could rationalize such large elasticities, this paper proposes an alternative interpretation to Kerr and Lincoln’s results, even when the labor demand is not close to perfectly elastic. If employers face costs to hire immigrant labor and are bound to pay the going wage, firms might disproportionately hire immigrants only when the demand for workers is increasing. In this case, immigrants would

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10If computer scientists have large effects on firm productivity, then demand curves for them would be very elastic. Alternatively, one could imagine that, absent the foreign computer scientists, production would shift overseas either because of domestic firms outsourcing production or because of Heckscher-Ohlin effects.
not replace incumbent workers or depress wages, but rather have a negative impact on the growth of wages and employment for natives. Under these circumstances, one might very well see a positive association between an increase in the utilization of foreign computer scientists and the increased utilization of their US counterparts, even though the availability of skilled foreigners is putting downward pressure on the growth in earnings and employment of native computer scientists.

3 A Dynamic Model of Supply and Demand of Computer Scientists

To gauge the impact that the availability of foreign high skilled labor has had on US workers, we construct a simple model of the labor market for computer scientists. While our model is quite stylized, we intend to capture the most salient features of the market.

In our model there are three potential sources for computer scientists. First, there are those who earn computer science bachelor’s degrees from US institutions. These individuals must complete college before they are ready to work. Second, there are US residents working in other occupations who can switch into computer science, but must pay costs to switch occupations. Third, there are foreigners who are being recruited on temporary work visas. Here we are aggregating foreign students getting degrees in the US with their domestic counterparts. During the 1990s, foreigners represented a small share of new CS graduates each year (around 10%).

There is also the group who immigrated with their parents as children, but these individuals are typically either citizens or green card holders and we assume employers do not distinguish between these individuals and the US born. We also ignore the fact that some immigrants are coming in on permanent visas. As the GAO and Department of Commerce reports cited earlier suggest, at least in the 1990s, the majority of foreigners working as computer scientists within the US who have finished their undergraduate degrees abroad, arrived on temporary work visas. In addition, the data we will use does not allow us to distinguish visa types.

In terms of the demand side of the model, we assume that firms observe the technological progress level and make decisions about whether to hire foreigners or workers already permanently in the US. We assume that foreigners are somewhat more productive than US workers but are paid the same wage due to institutional restrictions. Alternatively, we could have equally well assumed employers experience a cost advantage associated with hiring foreigners. Furthermore,

\footnote{IPEDS Completions Survey.}
firms face increasing costs for recruiting foreigners, making it non-optimal for firms to only hire foreign workers.

3.1 Labor Supply of American Computer Scientists

We model U.S computer scientists as making two types of decisions along their career in order to maximize the expected present value of their lifetime utility. At age 20, individuals in college choose the field of study that influences their initial occupation after graduation, and from age 22 to 65, workers choose between working as a computer scientist or in another occupation. Individuals have rational, forward looking behavior and make studying and working decisions based on the information available at each period.

3.1.1 Studying decision

We assume that students make their major decisions when they are juniors in college. At age 20, an individual draws idiosyncratic taste shocks for studying computer science or another field: $\eta_i^c$ and $\eta_i^o$, respectively. This student also has expectations about the prospects of starting a career in each occupation after graduation (age 22), which have a values $V_{22}^c$ and $V_{22}^o$ respectively. With this information, an individual chooses between pursuing computer science or a different choice of major at the undergraduate level.\footnote{Essentially, we are assuming that students decide their major after the end of their second year in school. This presumes that the relative pool of potential applicants would have sufficient background to potentially major in computer science. A four year time horizon is more standard. We experimented with such a horizon and doing so made little qualitative difference to our conclusions.}

We model the utility of a student as a linear function of the taste shocks and career prospects in each sector. There is also a taste attractiveness parameter $\alpha_o$ for studying a different field from computer science and individuals discount their future with an annual discount factor $\beta$. With these assumptions, the field of study decision is represented by:

$$\max\{\beta E_t V_{22}^c + \eta_i^c, \beta E_t V_{22}^o + \alpha_o + \eta_i^o\}$$

We assume that $\eta_i^c$ and $\eta_i^o$ are independently and identically distributed and for $s = \{c, o\}$, can be defined as $\eta_i^s = \sigma_0 v_i^s$, where $\sigma_0$ is a scale parameter and $v_i^s$ is distributed as a standard Type I Extreme Value distribution. This distributional assumption is common to dynamic discrete choice models (Rust (1987), Kline (2008)) and it is convenient because it allows the decisions of agents to
be smoothed out, a desired property that will be used in the characterization of the equilibrium of the model.

Given the distributional assumption of idiosyncratic taste shocks, it follows that the probability of a worker graduating with a computer science degree can be written in logistic form:

\[ p_c^t = \left[ 1 + \exp\left(-\left(\beta^2 E_t - 2[V_{22}^c - V_{22}^o] - \alpha_o / \sigma_o \right)\right) \right]^{-1} \]

Note that the important parameter for how studying choices of workers are sensitive to different career prospects is the standard deviation of taste shocks. Small values of \( \sigma_0 \) imply that small changes in career prospects can produce big variations in the number of students graduating with a computer science degree.

The next step to characterize the supply of young computer scientists is to map the graduating probability described above to employment. Defining \( M^a_t \) as the exogenous number of college graduates with age \( a \) in time period \( t \),13 the number of recent graduates with a computer science degree in year \( t \) is represented by \( C_t = p_c^t M^a_t \).

### 3.1.2 Working Decision

The field of study determines if an individual enters the labor market as either a computer scientist or with a different occupation. However, individuals can choose to switch occupations along their careers. Specifically, at the beginning of each period, individuals between ages 22 and 65 choose to work in CS or another type of job in order to maximize the expected present value of their lifetime utility.

A feature of the model is that switching occupations is costly for the worker. A justification for this assumption is that workers have occupational-specific human capital that cannot be transferred (Kambourov and Manovskii (2009)). We assume the cost to switch occupations is a quadratic function of a worker’s age. Note that this assumption implies that it becomes increasingly harder for workers to switch occupations as they get older. Additionally, there is no general human capital accumulation and wages do not vary with the age of a worker.14

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13We are implicitly assuming that anyone who majors in computer science would have completed college even had they not majored in computer science and that computer science majors are infra marginal college finishers. A similar assumption was made by Ryoo and Rosen (2004) in their work on Engineers

14The implications of the model will still hold if there is general human capital accumulation and individuals expect similar wage growth profiles working as computer scientists or in the alternative occupation. As we do not distinguish workers by age in the calibration of the model, for simplicity we assume that workers at different ages within the same occupation are paid the same wage level.
Finally, we assume that workers have linear utility from wages, taste shocks and career prospects. Furthermore, wages must be totally consumed in that same year and workers cannot save or borrow. The Bellman equations of worker $i$ at age $a$ between 22 and 64 at time $t$ if he starts the period as a computer scientist or other occupation are respectively:

$$V^c_{t,a} = \max\{w^c_t + \beta \mathbb{E}_t V^c_{t+1,a+1} + \varepsilon^c_{it}, w^o_t - c(a) + \beta \mathbb{E}_t V^o_{t+1,a+1} + \varepsilon^o_{it} + \alpha_1\}$$

$$V^o_{t,a} = \max\{w^c_t - c(a) + \beta \mathbb{E}_t V^c_{t+1,a+1} + \varepsilon^c_{it}, w^o_t + \beta \mathbb{E}_t V^o_{t+1,a+1} + \varepsilon^o_{it} + \alpha_1\}$$

where $c(a) = \lambda_0 + \lambda_1 a + \lambda_2 a^2$, is the monetary cost of switching occupation for an age $a$ worker, and $\alpha_1$ is the taste attractiveness parameter for not working as a computer scientist. For simplicity, we assume that the current wage in the other occupation $w^o_t$ is exogenous and perfectly anticipated by the workers.\(^{15}\) In the model, all workers retire at age 65 and their retirement benefits do not depend on their career choices. As a consequence, workers at age 65 face the same decision problem but, without consideration for the future.

As in the college-major decision problem, idiosyncratic taste shocks play an important role in working decisions of an individual. Once more, we will assume that taste shocks are independently\(^{16}\) and identically distributed and for $s = \{c, o\}$ can be defined as $\varepsilon^s_{it} = \sigma_1 v^s_{it}$ where $\sigma_1$ is a scale parameter and $v^s_{it}$ is distributed as a standard Type I Extreme Value distribution.

Defining $p^{cS}_{t,a}$ as the probability that a worker at age $a$ between 22 and 64 moves from occupation $s$ to occupation $S$, it follows from the error distribution assumption that the migration probabilities can be represented as:

$$p^{cS}_{t,a} = [1 + \exp(-(w^c_t - w^o_t - c(a)) - \alpha_1 + \beta \mathbb{E}_t[V^c_{t+1,a+1} - V^o_{t+1,a+1}]) / \sigma_1]^{-1}$$

$$p^{oS}_{t,a} = [1 + \exp(-(w^o_t - w^c_t - c(a) + \alpha_1 + \beta \mathbb{E}_t[V^o_{t+1,a+1} - V^c_{t+1,a+1}]) / \sigma_1]^{-1}$$

and the migration probabilities of workers at age 65 are the same without discounting future career prospects. Note that the switching probabilities depend upon both the current wage differential and expected future career prospects at each occupation. The standard deviation of the taste shocks,\(^{15}\) As a matter of fact, in the simulations of the paper we will set $w^o_t = 1$ and measure wages of computer scientists as an occupational premium.

\(^{16}\) In the working decision problem, the independence assumption might be less plausible because taste shocks could be serially correlated. However, identifying parameters of the model with serially correlated errors is infeasible without longitudinal data (Kline (2008)).
the sector attractiveness constant and the cost of switching occupations will effect the extent to which changes in relative career prospects affect the movement of US residents across fields.

A feature of dynamic models with forward looking individuals is that working decisions depend upon the equilibrium distribution of career prospects. As in the dynamic choice literature with extreme value errors (Rust (1987) and Kline (2008)), we use the properties of the idiosyncratic taste shocks distribution to simplify the expressions for the expected values of career prospects. As a result, the expected value function for an individual at age \( a \) between 22 and 64 working as a computer scientist or in another occupation are respectively:

\[
E_t V_{t+1,a+1}^c = \sigma_1 \mathbb{E}_t \left[ \gamma + \ln \left\{ \exp \left( (w_{t+1}^c + \beta \mathbb{E}_{t+1} V_{t+2,a+2}^c) / \sigma_1 \right) + \exp \left( (w_{t+1}^c - c(a) + \alpha_1 + \beta \mathbb{E}_{t+1} V_{t+2,a+2}^o) / \sigma_1 \right) \right\} \right]
\]

\[
E_t V_{t+1,a+1}^o = \sigma_1 \mathbb{E}_t \left[ \gamma + \ln \left\{ \exp \left( (w_{t+1}^o + \alpha_1 + \beta \mathbb{E}_{t+1} V_{t+2,a+2}^o) / \sigma_1 \right) + \exp \left( (w_{t+1}^o - c(a) + \beta \mathbb{E}_{t+1} V_{t+2,a+2}^c) / \sigma_1 \right) \right\} \right]
\]

(1)

where gamma \( \gamma \approx 0.577 \) is the Euler’s constant and the expectations are taken with respect to future taste shocks. Workers at age 65 face the same expected values but don’t discount the future.

Now we turn to transforming migration probabilities to employment. The first step is to determine the CS supply of recent college graduates. After leaving college, individuals can start their careers in the occupation correspondent to their field of study with no cost. However, we also allow workers at age 22 to pay the switching costs and get their first job in an occupation different from their field of study. As a consequence, the number of computer scientists at age 22 is a function of the number of recent graduates with a computer science degree and the migration probabilities:

\[
L_{22}^c = (1 - p_{22}^co)C_t + p_{22}^co [M_{22}^c - C_t]
\]

where \( M_{22}^c \) is the number of recent college graduates, \( C_t \) is the number of recent graduates with a computer science degree, and \( M_{22}^c - C_t \) is the number of college graduates with any other degree.

In the same way, the supply of computer scientists at age \( a \) from 23-65 is a function of past employment in each occupation and the migration probabilities:

\[
L_{a}^c = (1 - p_{a-1}^co) L_{a-1} + p_{a-1}^co [M_{a-1}^c - L_{a-1}^c]
\]
where $M^a_t$ is the exogenous total number of workers in the economy at age $a$ in time period $t$. $M^a_t - L^a_t$ is the number of workers at age $a$ working in the residual sector. For simplicity, we assume that the number of workers in the economy at age $M^a_t$ is exogenous and constant over time.$^{17}$

The aggregate domestic labor supply of computer scientists is the sum of labor supply at all ages:

$$L_t = \sum_{a=22}^{a=65} L^a_t \quad (2)$$

Note that the labor supply of computer scientists depends on past employment, new college graduates with a computer science degree and on wages through the migration probabilities.

### 3.2 Labor Supply of Foreign Computer Scientists

An important characteristic of our model is that firms can recruit foreigners to work as computer scientists. As it will become clear throughout the section, this possibility has implications on how the market for CS workers responds to technological shocks, such as Internet innovation, in terms of enrollment decisions, wages and employment.

We model foreign computer scientists as having a perfectly elastic labor supply. The wage that a computer scientist could obtain in India, for example, is so much lower than it is in the US that the wage premium creates a large queue of individuals ready to take jobs in the US ($^{18}$Clemens (2013) provides direct evidence on this point). Additionally, we assume that foreigners cannot switch their occupation once hired to work as computer scientists and they continue to work in the US until their visa expires.$^{19}$

A simplified way to model the framework described above is to define $R_t$ as the number of foreigners recruited as CS in period $t$. Next, we assume that all CS foreigners stay in the US for 6 years, that is the maximum length of a H-1B visa contract.$^{20}$ In this framework, the number of

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$^{17}$In the simulation of the paper we set $M^a_t$ to be constant for all ages and $\sum_{a=22}^{a=65} M^a_t = 100$. We measure employment of computer scientists as percentage points of the employed population of interest.

$^{18}$As it will become clear later, the reason why in our model foreigners do not swamp the U.S. labor markets is because firms must pay, in addition to prevailing wages, increasing recruitment costs to employ foreigners.

$^{19}$In fact, during the period we are studying roughly half of those on H-1B visas eventually became permanent residences. In our appendix, we present a modification of the model that allows a constant fraction of H-1B visa holders to become permanent residents. Our results are consistent across modeling specifications.

$^{20}$The initial duration of the H-1B contract is 3 years, but it is extendable for an additional 3 years. Extensions do not count toward the H-1B cap, and are generally granted. As it will become clear in the labor demand side, in our model firms have incentive to keep foreigners for the maximum length of their contract. In our model, employers cannot lay foreign workers off, under the assumption that this was an unlikely practice during the Internet boom.
foreigners currently working as CS in the US is defined as the sum of current and the recruitment in the past 5 years:

\[ F_t = \sum_{j=0}^{5} R_{t-j} \]  

(3)

### 3.3 Labor Demand for Computer Scientists

We model the labor demand as resulting from the decisions made by a standard representative firm in a perfectly competitive framework. In the model, firms observe both the wage and technological progress levels and choose US and foreign employment in order to maximize their intertemporal profits. While firms do not assume that their US employees will necessarily stay with them from one period to the next, given the institutional setting, firms do assume that foreign workers will continue with the firm until the workers’ visa expires six years after he or she is hired.

We assume there is only one type of firm that hires computer scientists. CS labor is the only input used in the production function and we ignore the firm’s decision about capital or other types of labor adjustments.\(^{21}\) We further assume that computer scientists at different ages are perfect substitutes in the production function. As a consequence, firms do not distinguish workers by age when making their hiring decision, precluding analyzing the kind of issues addressed by Kerr et al. (2013).\(^{22}\) In addition, we assume that foreigners and US workers are close substitutes in the production function, but foreigners have higher marginal productivity than US workers.

A restriction we impose in the model is that all computer scientists in the market are paid the same wage independently of their age or citizenship. This assumption is in accordance with the H-1B visa regulation that requires that wages paid to foreigners must be at least the prevailing wage rate for the occupational classification in their area of employment. Finally, there are no adjustment costs for American workers but firms incur extra costs to recruit foreigners.\(^{23}\) This expenditure is justified by the fees and expenses directly related to the visa application process, and also the extra cost that a firm typically has for searching for workers overseas.

As it will become clear throughout the section, this framework implies that firms face a trade-

\(^{21}\)The assumption that labor adjustment decisions are independent of capital is standard in the dynamic labor demand literature when data on capital stock is not available (Hamermesh (1989)). Including capital in the production function generally does not qualitatively change the results (Kline (2008)).

\(^{22}\)While we suspect is would make sense to allow workers of different ages to be imperfect substitutes in production for each other, CPS sample sized are too small to support this kind of analysis.

\(^{23}\)In our appendix we set-up and calibrate a model where the quadratic cost term for hiring foreigners also applies to Americans. Our results are not sensitive to this modeling change.
off when making the decision of hiring foreigners. On one hand, foreigners have a higher marginal productivity than US workers and are paid the same wage. As a consequence, firms are willing to substitute foreign workers for their US workers. On the other hand, there are extra recruitment costs to bring foreigners to the US. This restriction implies that firms never completely substitute foreign for US workers.

3.3.1 Firm’s Decision

The forward looking firm makes decisions about the recruitment of US and foreign workers in order to maximize intertemporal profits, as represented by the Bellman equation:

$$\pi_t = \max_{L_t, R_t, \theta} A_t Y(L_t + \theta F_t) - w_t (L_t + F_t) - C_R(R_t) + \beta E_t[\pi_{t+1}]$$

subject to foreign labor supply:

$$F_t = \sum_{j=0}^{5} R_{t-j}$$

where $A_t Y(.)$ is the production function, $\theta$ is a constant greater than 1 that represents marginal productivity differences between foreigners and US workers, and $C_R(.)$ is the recruitment cost function of foreigners.

We represent the production function as Cobb-Douglas, such that $Y(L_t + \theta F_t) = (L_t + \theta F_t)^\gamma$, for some $\gamma$ between zero and one, implying a downward sloping labor demand curve for computer scientists. This set-up can be made consistent with the Romer (1986) model of knowledge accumulation as a by-product of capital accumulation; or the Arrow (1962) learning-by-doing model, where we allow increases in employment to lead to increases in productivity. To see this, we can reformulate the production function to be $Y_t = [B_t(L_t + \theta F_t)]^{\delta}$. If we let the technology parameter exhibit learning-by-doing, then $B_t = \psi_t(L_t + \theta F_t)^{\alpha}$. If we define, $A_t = \psi_t^{\delta}$ and $\gamma = \alpha \delta$, then we recover the simple Cobb-Douglas production function: $A_t(L_t + \theta F_t)^\gamma$. The parameter, $\gamma$, should then be thought of as a reduced-form parameter that captures not just the effective labor share in output, but also the productivity gains from hiring more effective workers. As long as $\gamma$ lies between 0 and 1, this parametrization guarantees a decreasing marginal return to labor and thus an interior solution for the employment

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24For simplicity, we assume that firms and individuals have the same annual discount factor $\beta$. For expositional purposes, we now omit the the superscript $c$ for wages and employment of computer scientists.
decision of the firm. Furthermore, the parameter $\gamma$ has a direct mapping to the long-run elasticity of labor demand with respect to effective labor ($L_e = L + \theta F$):

$$\epsilon_{L_e,w} = \frac{1}{1-\gamma}$$

Additionally, we assume that recruitment costs of foreigners include both linear and quadratic components $C_R(R_t) = c_1 R_t + c_2 R_t^2$. The linear term in the foreign recruitment cost represents expenditures that are required for hiring each foreign worker, such as application fees. The quadratic term has been widely used in dynamic labor demand literature (Sargent (1978) and Shapiro (1986)). As will become clear from the first order condition of the firm, convex hiring costs, because increasing marginal recruitment costs of foreigners, prevents firms from completely substituting foreigners for domestic workers.\(^{25}\)

As in a typical dynamic labor demand problem the solution to the firm’s decision can be characterized by both the first order and envelope conditions with respect to the employment level. The first order condition of the firm’s maximization problem with respect to US employment is represented by the following equation:

$$A_t \gamma (L_t + \theta F_t)^{\gamma-1} = w_t \quad (4)$$

Note that because there is no adjustment costs for US workers, the first order condition with respect to US employment is the same as in a static maximization problem. It is simply characterized by firms equalizing the marginal product of US workers to their wage level.

In addition to choosing US worker employment, the firm also decides the number of foreign workers recruited at each period. The first order condition of the firm’s problem with respect to $R_t$ is given by:

$$\theta A_t \gamma (L_t + \theta F_t)^{\gamma-1} - w_t - c_1 - 2c_2 R_t + \sum_{j=1}^{5} \beta_j \mathbb{E}_t [\frac{\partial \pi_{t+j}}{\partial R_t}] = 0$$

where $\frac{\partial \pi_{t+j}}{\partial R_t}$ is defined as how profits in $t+j$ are affected by changes in the recruitment in $t$. Finally, we use envelope condition to derive the shadow price of past foreign recruitment on current profits, such that:

\(^{25}\)Our formulation implies the foreign share of new hires will rise as demand increases. There are alternative models that would imply something similar. If firms had some local monopsony power, they would accommodate demand increases by shifting recruitment toward foreign labor. In our modeling efforts, we have experimented with such models, but we do not include their detailed results. In qualitative terms such models give similar counterfactual predictions to the model we emphasize here. Surely, there are important differences between the model we present here and the alternative monopsony model we developed. However, if the focus is on trying to understand the impact of immigration on wages and employment, the different models give similar predictions.
Rearranging the first order and envelope conditions of foreigner recruitment leads us to the useful alternative representation to the demand for foreign workers:

\[
\sum_{j=0}^{5} \beta^{j} \mathbb{E}_{t}[\theta A_{t+j} \gamma (L_{t+j} + \theta F_{t+j})^{\gamma-1} - w_{t+j}] = c_{1} + 2c_{2}R_{t} \tag{5}
\]

Equation (5) shows the trade-off faced by firms when hiring foreigners. The left hand side can be interpreted as the present value of the expected marginal benefit of recruiting a foreigner, defined as the difference between the marginal productivity of a foreigner and wage level during the 6 years duration of his contract. Note that firms benefit from hiring foreigners because they are more productive than US workers by a constant \( \theta \) but are paid the same wage. The right hand side represents the marginal cost of recruiting a foreigner. Since the marginal cost of recruiting a foreigner is increasing with \( R_{t} \), firms will never completely substitute foreigners for US workers in the model.

### 3.4 Equilibrium

A dynamic general equilibrium can be characterized by the system of equations that represent those choice functions and the stochastic process of technological progress \( A_{t} \). In particular, equation (1) characterizes the expectations of workers with respect to future career prospects, equations (2) and (3) are the dynamic labor supply of American and foreigner computer scientists respectively, and equations (4) and (5) describe the dynamic labor demand for American and foreign CS.

The last piece to characterize the equilibrium of the model is to define a stochastic process of technological progress. Note that \( A_{t} \) is the only source of exogenous variation to the system. We choose to specify \( A_{t} \) as a close to random walk process,\(^{26}\) such that:

\(^{26}\)We model the technology progress as a close to random walk since we will interpret the Internet boom as a series of very persistent technological shocks that hit the information technology sector during the late 1990s. We also interpret the 2000 to 2004 to be a dot com bust (our out-of-sample predictions are 2005 to 2009). We found little evidence that workers, students or employers expected the increase in the demand for computer scientists during the 1990s to be temporary (and subject to a post-Y2K bug slump). First, the BLS projected a steady increase in CS employment after the year 2000, and claimed that it expected the top two fastest growing occupations to be computer scientists, and computer engineers respectively. Furthermore, there is a substantial increase in CS degrees started during the dot-com boom, indicating that students perceived the demand for computer scientists to be increasing permanently during the period. We therefore believe that a more realistic assumption is that agents perceived the increase in demand during the late 1990s to be permanent - and that the World Wide Web generated opportunities for new businesses that demanded computer scientists. However, at some period in the beginning of the year 2000, presumably for a variety of reasons, the boom turned around and NASDAQ crashed.
\[ A_t = 0.999A_{t-1} + 0.001\bar{A} + \xi_t \] (6)

where \(\bar{A}\) is the steady state level of progress, and \(\xi_t\) is the i.i.d. random idiosyncratic productivity shock with mean zero that is assumed to be independent of other variables of the model.\(^{27}\)

The equilibrium of the model can be expressed by a mapping from the state variables: \(s = \{C_t, L_{t-1}, ..., L_{t-64}, R_{t-1}, ..., R_{t-5}, A_{t-1}\}\) and exogenous productivity shock \(\xi_t\) to the values of \(L_t, w_t, R_t,\) and \(V_t\), the vector of career prospects at different occupations for different ages, that satisfies the system of equations (1) to (6). We solve the system by numerically simulating the model in Dynare via perturbation methods.\(^{28}\) The policy functions are calculated using a second order polynomial approximation to the decision rules implied by the equations of the model.\(^{29}\)

### 4 Calibration and Simulation

#### 4.1 Identification and Calibration Method

There are twelve parameters in the model \(\{\sigma_0, \alpha_0, \sigma_1, \alpha_1, \lambda_0, \lambda_1, \lambda_2, \beta, \gamma, \theta, c_{R1}, c_{R2}\}\). We set the foreign worker productivity parameter \(\theta = 1.12\)\(^{30}\) based on estimations from the 2003 National Survey of College Graduates data.\(^{31}\) This value of the wage premium earned by foreign green card holders is broadly consistent with other estimates in the literature (Mithas and Lucas (2010), Mukhopadhyay and Oxborrow (2012)). Furthermore, we set the annual discount rate of workers and firms \(\beta = 0.9\). Our results are not sensitive to plausible variations of this parameter.

In our modeling we are treating the wage, employment and enrollment shifts as a response to an exogenous shift in the demand for computer scientists due to the technological developments that occurred during the period of analysis. We use this demand shift to identify the enrollment and labor supply response of natives, and the parameters affecting the hiring decision of foreigners:

\(^{27}\)Note that both workers and firms are risk neutral in our model. For this reason, the certainty equivalence property holds and the solution of the model does not depend on higher moments of the idiosyncratic productivity shock.

\(^{28}\)Dynare is a widely used software for solving Dynamic Stochastic General Equilibrium models. See Juillard (1996) for details.

\(^{29}\)Collard and Juillard (2001a,b) describe in detail the perturbation and higher order approximation of policy function methods we use in this paper.

\(^{30}\)In an additional Appendix we re-do all our results for different values of this parameter, and find that our results are not sensitive to the choice of this parameter.

\(^{31}\)Specifically, we estimate the wage premium for foreign born computer scientists who are naturalized or permanent residents, compared to US born CS workers. This estimation comes from a logarithmic of annual earnings regression controlling for gender and a cubic age polynomial. We interpret this wage premium as the average marginal productivity difference between foreign and US computer scientists.
\{\sigma_0, \alpha_0, \lambda_0, \lambda_1, \lambda_2, \alpha_1, c_{R1}, c_{R2}\}. At the same time, demand shifts will not identify the slope of the labor demand curve. As a result, we present the results of the paper using different assumptions about the values of \(\gamma\).

To calibrate \(\{\sigma_0, \alpha_0, \lambda_0, \lambda_1, \lambda_2, \sigma_1, \alpha_1, c_{R1}, c_{R2}\}\), we use observations of US and foreign employment, wages, and enrollment between 1994 and 2004. We define other STEM occupations as the career alternative to CS jobs. The data we are using on employment and earnings is derived from the March Current Population Survey. This survey contains no indication as to the visa status of the foreign born. To approximate the population of interest, we identify the foreign born who immigrated to the US after they turned 18 as our foreign workers. We also normalize employment variables to use units of American STEM workers, and wages to use units of wages of other STEM jobs, and thus define our key data series as:  

1. \(L_t = \frac{\text{US computer scientists}}{\text{US workers with STEM occupations}}\)
2. \(F_t = \frac{\text{Foreign computer scientists}}{\text{US workers with STEM occupations}}\)
3. \(w_t = \frac{\text{Median weekly wages for computer scientists}}{\text{Median weekly wages for other STEM jobs}}\)
4. \(p_{t+2}^c = \frac{\text{US computer science BA degrees awarded (lagged 2 years)}}{\text{US STEM BA degrees awarded (lagged 2 years)}}\)
5. \(s_{a_1, a_2} = \frac{\text{US computer scientists with age between } a_1 \text{ and } a_2}{\text{US computer scientists}}\)

For \(a_1\) and \(a_2\) defined as the age ranges \{22 to 34; 35 to 44; 45 to 65\}.

Conditional on \(\gamma\) and \(\theta\) and observations of \(\{w_t, L_t, F_t\}\) we are able to recover values of \(A_t\) implied by our model during the period of 1994 to 2004:

\[
A_t = \frac{w_t}{\gamma(L_t + \theta F_t)^{\gamma - 1}}
\]

We assume that the economy is in steady state in 1994, such that \(\bar{A} = A_{1994}\), and that it is hit by the series of shocks. In terms of expectations, we assume that both firms and individuals are

\[^{32}\text{We use March CPS observations and define foreigners as those born abroad and immigrated after the age of 18. See the data appendix for more information on occupational classifications. We smooth the raw data as follows: } X_{t,\text{smooth}} = \frac{1}{3}(X_{t-1,\text{raw}} + X_{t,\text{raw}} + X_{t+1,\text{raw}}), \text{ except for the American and foreigner employment data in 1994, which citizen} \]

\[^{33}\text{We exclude imputed values of wages, and multiply top-coded values by a factor of 1.4. Bollinger and Hirsch (2007) show that not excluding imputations can lead to biased results. Whereas the top-coding adjustment is standard in the literature (Lemieux (2006)).} \]

\[^{34}\text{Uses data from 1996 to 2006, representing enrollment decisions from 1994 to 2004.} \]
surprised by changes in $A_t$.\footnote{We also considered the alternative assumption that all agents fully or partially anticipated the future path of technological process. This assumption yields time paths for wages and employment that are quite similar to the ones we observe under our static expectations assumption. In contrast, with this alternative assumption, enrollment jumps almost immediately, which is inconsistent with the time path of enrollment we observe. At the same time, our counterfactual simulations presented later with the alternative anticipation assumption are similar to the ones we present with static expectations. Presumably a model that allowed expectations to evolve would be more realistic. However, given the robustness of our central results to the static versus foresight assumption, we did not explore such an alternative.} Note that following equation (6), firms and workers have essentially static expectations about future technology progress, such that $E_t[A_{t+j}] \equiv A_t$ for any $j$.

The remaining parameters $\{\sigma_0, \alpha_0, \lambda_0, \lambda_1, \lambda_2, \sigma_1, \alpha_1, c_{R1}, c_{R2}\}$ are calibrated such that the model matches the observations of $L_t$, $F_t$, $w_t$, in two periods of time: 1994 and 2004, and the changes in the age structure $s_{t_1}^{a_1}, a_2$ in 2004.\footnote{The decision to match changes in the age structure of CS rather then levels is to assure that our calibrated model reflects movements that occurred in the market for CS during the period rather than the age structure of the entire population. In fact, we obtain more reasonable calibrated parameters when matching the changes in the age structure of CS.} We use a Nelder-Mead simplex method to find parameter values which yield solutions to the model under these data restrictions.\footnote{Note that we have a perfectly identified system: we find the values of 9 independent parameters and 2 implied values of $A_t$ such that the model matches 11 data observations: $L_t$, $F_t$, $w_t$ and $p_{c}^{-2}$ in two years and the observation of changes in $s_{t}^{21,34}$, $s_{t}^{35,64}$, and $s_{t}^{45,65}$ in 2004.} The intuition for the identification of the parameters comes straight from the data. For the given series of exogenous technological shocks and wages, variations of enrollment between 1994 and 2004 identify the parameters $\sigma_0$ and $\alpha_0$, changes in native employment identify the parameters $\sigma_1$ and $\alpha_1$, variations in foreign employment identify the recruitment cost parameters $c_{R1}$ and $c_{R2}$, and changes in the age structure of computer scientists identify the quadratic costs of switching occupations: parameters $\lambda_0$, $\lambda_1$, and $\lambda_2$.

4.2 Calibration results

We use the procedure described above to calibrate the model using three different values of $\gamma$: $\{0.25, 0.5, 0.75\}$.\footnote{$\gamma$ in the 0.25 to 0.75 range imply labor demand elasticities between -1.33 and -4.0. Ryoo and Rosen (2004), estimate demand elasticities for engineers that lie between -1.2 and -2.2, while Borjas (2009), studying the effect the immigration of foreign born PhD scientists on the wages of competing workers, estimates demand elasticities of approximately -3.0. While some may take issue with the external validity of these estimates for us, they do suggest that we have varied $\gamma$ through a sensible range.} We present the calibrated parameters for these different values of $\gamma$ in Table 3 and a comparison of the data with the model’s output in Figures 7 - 8. We also report the long and short run effective occupation-wage, and enrollment elasticities, along with the long-run demand-wage elasticity, implied by each $\gamma$, where the occupation-wage elasticity is an elasticity of labor supply to the CS sector. We consider the demand elasticities derived from our $\gamma$’s to span a reasonable range of plausible values of this parameter, which as we describe in Section 4.4, is challenging to identify.
The calibrated model allows us to calculate several additional economically meaningful statistics, which we also include in the bottom segment of Table 3. We calculate the long-run occupation and enrollment elasticities with respect to wages, by replacing the demand side of the model with an exogenous wage, which we set to be permanently 1% higher than its 1994 value, and in each case, we allow the supply side to come to a new equilibrium based on the calibrated parameters. We similarly calculate the short-run occupation and enrollment elasticities, but instead of allowing the supply side to come to a new steady-state, we calculate the elasticities based off of changes in occupation and enrollment after 1 year.

In the bottom section of Table 3, we show how each of these long-run elasticities varies with $\gamma$. The long-run occupational labor supply elasticity for Americans is around 5.4. The enrollment in CS is even more elastic, with a long-run elasticity that lies around 11.6.\(^{39}\) This result reflects the large enrollment response we witness in the data. The short-run occupation elasticity is much lower than the corresponding long-run elasticity. We expect this result, due to the supply frictions and lags in our model. In contrast, the short-run and long-run enrollment elasticities are almost exactly the same. Pre-enrollment students respond immediately to a wage shock. A fuller model which includes capacity constraints on the supply side of the higher education market, would work to slow such adjustments. Finally, the average cost of recruiting a foreign worker is about 0.53 times the average annual earnings of a non-CS STEM job.

In Figures 7-8, we report both the path predicted by our calibrated model (Full model) and the path observed in the data (Smooth data) during 1994-2009. Note that by the construction of our calibration procedure, the full model fits the data perfectly in 1994 and 2004. We use the transition period between 1995 to 2003 to evaluate how well the model fits the data, and the years 2005-2009 for out of sample prediction. These years include observed changes to relevant immigration laws, and potentially unobserved structural changes which would map to changes in our parameters, so our model has trouble fitting the data in this period for some series. Figure 7 shows that for different $\gamma$’s, the model is a fairly close fit for CS wages and American employment during the evaluation period, although CS wages in the model grow faster at first and American employment in CS grows more slowly in the model than the data. The fit of these two series is still relatively good in the out of sample prediction period, with wages slightly higher and American employment slightly lower in

\(^{39}\)Ryoo and Rosen estimate substantially smaller enrollment elasticities of between 2.5 and 4.5, but are modeling the decision to enroll in a broader field than we are.
the model compared to the data.

Figure 8 shows that the enrollment output of the model is particularly sensitive to the choice of $\gamma$, where lower values somewhat under-predict the enrollment boom surrounding 2001. At odds with the predictions of our model, enrollment does not increase starting in 2006. Given the rising wages of computer scientists at the time, this pattern seems a bit surprising and we confess to not having a good understanding as to why enrollments do not seem to be responding to market signals. The figure also shows that foreign employment grows more slowly at first in the model than the data. In the out of sample period, foreign employment shrinks in the model instead of growing slightly, as in the data. This could be because our model assumes that after a 6-year period, foreigners return to their home country. In the Appendix, we calibrate a model that allows a certain fraction of H-1B workers to become permanent residents. This extension of the model does a better job of fitting the share of foreign employment in the last few years (and overall does a good job of fitting the different calibrated series).

4.3 Simulation of Fixed Foreign Worker Population Counterfactual

We use our calibrated model to simulate a counterfactual Internet boom from 1994-2004, as if firms had restrictions on the number of foreigners that they can hire. The exercise consists of hitting the calibrated model with the same technological shocks we derived before but imposing that firms cannot increase $F_t$ above its 1994 level. The results of this simulation are also presented in Figures 7-8 (Restricted Model). There we can compare the counterfactual for different values of $\gamma$ with the smoothed data.

Overall, our calibrated model implies an increase in the demand for domestic workers when firms cannot increase foreign employment above its 1994 level. As a result, we observe higher wages, US employment and computer science enrollment in the counterfactual economy. We simulate significant differences in the labor market for computer scientists during the Internet boom if firms had restrictions on the number of foreigners they could hire. While the data shows that the relative wages for CS workers increased by 3.2% between 1994 and 2004, in the simulated economy wages would have increased between 5.9% to 6.9% (decreasing with $\gamma$) during the same period. In terms of employment, we observe an increase of 41% of total CS employment during the Internet boom, while in the economy where we restrict foreign workers we find an increase of only 29.1% to 36.1% (decreasing with $\gamma$) during the same period. This change in employment results from the more
inelastic labor supply curve that firms face when extra foreigners are not available.

In Table 4 we compare the 2004 levels of the variables of interest between the data and the simulated economy where firms could not increase foreign employment above its 1994 levels. We find that in 2004, CS workers wages would be 2.8% to 3.8% higher if firms had restrictions in the number of foreigners they could hire. Furthermore, the number of Americans working in the CS sector would be 7.0% to 13.6% higher in 2004, but the total employment level would be lower by 3.8% to 9.0%. Finally we find a significant difference in the number of students enrolling in computer science in the simulated counterfactual economy. Relative to other STEM fields, enrollment in CS would be 19.9% - 25.5% higher in 2004 if firms could not increase foreign employment during the Internet boom. These numbers reflect the fact that, according to our calibrations, students’ major choices are very sensitive to changes in wages.

To sum up, even when assuming a very elastic labor demand curve (high $\gamma$ values) we find significant effects of foreign recruitment on wages and employment of domestic CS workers during the Internet boom. Additionally, firms would not replace all foreigners with domestic workers during this period if they were restricted to keeping the same foreign employment level of 1994, implying that industry output would be reduced.

4.4 Identification of Labor Demand

As shown previously, the labor market outcomes of the counterfactual simulations holding $F_t$ fixed can vary with values of $\gamma$. In particular, we observe that when using a more elastic labor demand (higher $\gamma$), our simulated counterfactual economy (where we restrict foreigner workers) from section 4.3 has smaller increases in wages and US employment. The natural question is which, if any, of the 3 different $\gamma$'s yields results that are closest to what we would observe if firms had not been able to recruit foreigners during the Internet boom?

In a closed, constant returns to scale economy, the elasticity of demand for computer scientists would depend on both the substitutability between consumption of goods produced in sectors of the economy intensive in computer scientists and other goods, and on the substitutability between production of computers scientists and other factors of production. Given the fact that the share of computer scientists working in any one sector is not that large, the demand elasticity will be

\[\text{According to the Census, roughly 30% of computer scientists worked in either the computer manufacturing or the computer services three-digit industries during 1990 and 2000.}\]
determined largely by the elasticity of substitution between computer scientists and other factors of production. In the relatively small window of time we are talking about, it is hard to believe these elasticities are that large.

There are two factors that mitigate this basic conclusion. First, to the extent that computer scientists contribute to innovation in the sectors of the economy intensive in computer scientist labor, the derived elasticity of demand for computer scientists in those sectors is likely to be higher than it would otherwise have been. In addition, the potential for off-shoring would drive up the derived elasticity of demand for computer scientists. However, even if, for these reasons, the derived demand for computer sciences in computer manufacturing and computer services was quite high, a small enough share of computer scientists work in these industries, that it is hard to believe either agglomeration effects or off-shoring can drive up the derived demand elasticity for computer scientists that much. Additionally, if it would have been easy for employers to outsource, CEOs like Microsoft’s Bill Gates would not have been lobbying to increase the H-1B visa cap. It is hard to reconcile the fact that the computer industry is lobbying so hard for easier access to foreigners, if it did not matter where their workforce was located.

Traditionally, exogenous shifts in supply are used to identify demand curves. In our case, while there is a plausibly exogenous component to the increased representation of the foreign born amongst the US Science and Engineering workforce, our visa system ensures that there is a large endogenous component. In theory, it might be possible to get some leverage on identifying the labor demand curve for CS workers by comparing the results of the counterfactual simulation for the different $\gamma'$s to the observations of what happened in the Information Technology (IT) sector in the mid 1970s. Specifically, as described in Bound et al. (2013), during this earlier period, the IT sector experienced a significant transformation due to the introduction of the microprocessor, which generated an increase in the demand for IT workers. However, firms had substantially less access to foreign labor during that earlier boom than they did during the 1990s. This happened because there was a sharp increase in the supply of college graduates from overseas in the past decades, but also due to the change in the US visa system in the early 1990s that facilitated a greater inflow of high skilled foreigners via employer-sponsored visas.

Our strategy would be to use our calibrated model to simulate what would happen if firms had

\footnote{We have also shown that the production function is consistent with one type of model that incorporates the effect that computer scientists have on firm innovation.}
less access to foreign high-skilled labor in the 1990s boom and compare these simulations to the earlier boom. Comparisons between simulation results with different values of $\gamma$ and what actually happened earlier would help narrow plausible values for $\gamma$. Intuitively, if demand is relatively elastic, the loss of access to foreigners would have relatively little impact on wages, but a large impact on total CS employment. Whereas a less elastic demand curve would have a large effect on wages and less of an effect on total CS employment. This kind of exercise is valid only under the strong assumptions that our economic model accurately reflects that labor market for IT workers, and that the demand and supply elasticities were the same during the two periods and that the two shocks generated shifts in the labor demand of roughly the same magnitude. However heroic such assumptions might be, the strategy fails for a simpler reason. The strategy requires comparing wage and employment changes for a small segment of the workforce across periods. Our estimates were simply not reliable enough for such exercises to be meaningful.

Given the data limitations and other complications discussed in this section, we cannot provide an estimate for the value of $\gamma$, but our discussion suggests that the elasticity of demand for computer scientists should not be too large and that the values presented in this paper cover a plausible range.

5 Discussion

The model we have developed in this paper suggests an intermediate position as the most reasonable one in the debate over the effects of high-skilled immigration, on US workers. Focusing on the tech boom of the 1990s, we develop a model that allows us to answer the counterfactual question: what would have happened to overall employment, to the employment of US residents, and to wages in the IT sector had the immigration of computer scientists been restricted to its level as of the early 1990s before the tech boom? Our results suggest a middle ground between the two sides of this debate.

First, our estimates suggest that even without foreign trained computer scientists, the supply of computer scientists to the US market is quite elastic, especially in the medium run, as the students induced to study computer science by the increased opportunities in the field begin to enter the market. For elasticities of demand that lie between -1.3 and -4.0, we show that had firms not been able to hire immigrants through the late 1990s, the wages of US trained computer scientists would have been 2.8% to 3.8% higher than they were, and there would have been 7% to 13.6% more
Americans working in the CS sector.

At the same time our estimates suggest that were it not for the immigrant computer scientists that firms were able to hire, the growth in the number of computer scientists in the economy would have been significantly slowed. Our estimates suggest that total employment in the CS sector would have been 3.8-9% lower if firms were not able to hire additional immigrants during the late 1990s, thus implying that the fact that firms could hire immigrants during the 1990s increased output and lowered both input and output prices in the computer scientist intensive sectors of the economy. How much these developments benefited stock holders and consumers depends on the nature of the output market, which we have not tried to model. The increased employment of computer scientists would also have increased the demand for complementary production inputs, such as software marketing and sales workers. Furthermore, the availability of foreign CS workers made the CS labor supply curve more elastic, further enhancing this demand increase for complements.

Under the assumption that the tech boom of the 1990s exogenously increased the demand for computer scientists, we have been able to reliably estimate supply curves. Estimating the slope of the labor demand curve was substantially more difficult. In other contexts, labor economists have been willing to assume some degree of exogeneity to immigrant supplies. In the current framework, the institutional context implies that immigrant CS labor is completely endogenous to labor demand.

While we cannot reliably estimate the slope of the demand curve for computer scientists, we believe that we can reject any notion that the demand curve for computer scientists is close to perfectly elastic. Perfectly elastic demand curves are inconsistent with the rising wages for computer scientists that we observe during the 1990s. As long as the demand curve for computer scientists is downward sloping, the increased access employers had to foreign-trained, skilled immigrants during the 1990s works to lower both the wages and employment opportunities for US trained computer scientists.

Our paper should be viewed as a first-step towards modeling the US labor market for computer-scientists. In the model we incorporate features that were ignored in earlier models developed by Freeman and Ryoo and Rosen. Specifically we model both the possibility that individuals might switch occupations, and the possibility that firms might hire immigrants from abroad. In the context of computer scientists both are clearly important. We focused on the market for computer
scientists. In the context of other scientific fields where a masters or PhD are essential, it would also be important to model foreign participation in US graduate programs as well.\footnote{Such degrees are becoming increasingly important in computer science, as well.}
References


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Juillard, M., 1996. Dynare: A program for the resolution and simulation of dynamic models with forward variables through the use of a relaxation algorithm. CEPREMAP 9602.


Peri, G., Shih, K., Sparber, C., 2013. Stem workers, h1b visas and productivity in us cities.


Table 1: Fraction of Computer Scientists in the US Workforce by Occupation

<table>
<thead>
<tr>
<th>Year</th>
<th>All workers with a BA/MA</th>
<th>STEM college graduate workers</th>
</tr>
</thead>
<tbody>
<tr>
<td>1970</td>
<td>1.68%</td>
<td>16.86%</td>
</tr>
<tr>
<td>1980</td>
<td>1.83%</td>
<td>23.60%</td>
</tr>
<tr>
<td>1990</td>
<td>3.30%</td>
<td>35.99%</td>
</tr>
<tr>
<td>2000</td>
<td>5.66%</td>
<td>53.31%</td>
</tr>
<tr>
<td>2010</td>
<td>5.28%</td>
<td>54.90%</td>
</tr>
</tbody>
</table>

Note: Sample restricted to employed workers with a Bachelors or a Masters degree. Definition of Computer Scientists and STEM workers determined by occupational coding (for details see Data Appendix).
Source: US Census (years 1970 to 2000); ACS (2010)
Table 2: Foreign Born and Immigrated at Age 18 or Older Fraction of Employed Population by Occupation

<table>
<thead>
<tr>
<th>Year</th>
<th>Immigrants as a fraction of BA/MAs</th>
<th>Immigrants as a fraction of Computer Scientists</th>
<th>Immigrants as a fraction of Other STEM workers</th>
</tr>
</thead>
<tbody>
<tr>
<td>1970</td>
<td>2.10%</td>
<td>2.37%</td>
<td>3.63%</td>
</tr>
<tr>
<td>1980</td>
<td>5.43%</td>
<td>7.09%</td>
<td>9.72%</td>
</tr>
<tr>
<td>1990</td>
<td>6.86%</td>
<td>11.06%</td>
<td>10.71%</td>
</tr>
<tr>
<td>2000</td>
<td>8.41%</td>
<td>18.59%</td>
<td>12.69%</td>
</tr>
<tr>
<td>2010</td>
<td>12.77%</td>
<td>27.82%</td>
<td>18.21%</td>
</tr>
</tbody>
</table>

Note: Sample restricted to employed workers with a Bachelors or a Masters degree. Definition of Computer Scientists and STEM workers determined by occupational coding (for details see Data Appendix). Immigrant defined as one born abroad, and migrated to the US after the age of 18.

Source: US Census (years 1970 to 2000); ACS (2010)
Table 3: Calibrated Parameters

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
<th>$\gamma$</th>
<th>Calibrated Value</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>0.25</td>
<td>0.50</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\alpha_0$</td>
<td>Mean taste for not studying CS</td>
<td>0.0940</td>
<td>0.0943</td>
</tr>
<tr>
<td>$\sigma_0$</td>
<td>Std. dev. of study area taste shocks</td>
<td>0.0001</td>
<td>0.0001</td>
</tr>
<tr>
<td>$\alpha_1$</td>
<td>Mean taste for not working in CS</td>
<td>0.3715</td>
<td>0.3486</td>
</tr>
<tr>
<td>$\sigma_1$</td>
<td>Std. dev. of occupation taste shocks</td>
<td>0.1385</td>
<td>0.1364</td>
</tr>
<tr>
<td>$c_{R1}$</td>
<td>Foreign linear recruitment cost</td>
<td>0.5247</td>
<td>0.5228</td>
</tr>
<tr>
<td>$c_{R2}$</td>
<td>Foreign quadratic recruitment cost</td>
<td>0.0102</td>
<td>0.0109</td>
</tr>
<tr>
<td>$\lambda_0$</td>
<td>Sector switching constant cost</td>
<td>0.1159</td>
<td>0.1164</td>
</tr>
<tr>
<td>$\lambda_1$</td>
<td>Sector switching linear cost</td>
<td>0.0138</td>
<td>0.0119</td>
</tr>
<tr>
<td>$\lambda_2$</td>
<td>Sector switching quadratic cost</td>
<td>0.0006</td>
<td>0.0004</td>
</tr>
<tr>
<td>$\epsilon_{L,d,w}$</td>
<td>Long run effective labor demand elasticity</td>
<td>1.33</td>
<td>2.00</td>
</tr>
<tr>
<td>$\epsilon_{L,s,w}$</td>
<td>Long run US occupational labor supply elasticity</td>
<td>5.4612</td>
<td>5.5743</td>
</tr>
<tr>
<td>$\epsilon_{p,w}$</td>
<td>Long run US CS enrollment elasticity</td>
<td>11.6954</td>
<td>11.2624</td>
</tr>
<tr>
<td>$\epsilon_{d,w}$</td>
<td>Short run US occupational labor supply elasticity</td>
<td>0.5591</td>
<td>0.6745</td>
</tr>
<tr>
<td>$\epsilon_{p,w}$</td>
<td>Short run US CS enrollment elasticity</td>
<td>10.2834</td>
<td>11.3758</td>
</tr>
<tr>
<td>$AC_F$</td>
<td>Average cost of recruiting foreign worker</td>
<td>0.5312</td>
<td>0.5299</td>
</tr>
</tbody>
</table>

Note: The average cost of recruiting a foreign worker is measured in units of average annual US non-CS STEM worker wages. The parameter $\gamma$ determines the labor demand elasticity to wages.
Table 4: Summary of Results from Counterfactual Simulation

<table>
<thead>
<tr>
<th>Variable</th>
<th>γ = 0.25</th>
<th>γ = 0.5</th>
<th>γ = 0.75</th>
</tr>
</thead>
<tbody>
<tr>
<td>CS Wages</td>
<td>3.8%</td>
<td>3.2%</td>
<td>2.8%</td>
</tr>
<tr>
<td>CS US Native Employment</td>
<td>13.6%</td>
<td>12.5%</td>
<td>7.0%</td>
</tr>
<tr>
<td>CS Enrollment</td>
<td>25.5%</td>
<td>20.2%</td>
<td>19.9%</td>
</tr>
<tr>
<td>Total Employment</td>
<td>-3.8%</td>
<td>-4.6%</td>
<td>-9.0%</td>
</tr>
</tbody>
</table>

Note: The counterfactual simulates an economy from 1994-2009 in which the level of foreign CS workers is not allowed to increase from its 1994 value. The parameter \( \gamma \) determines the labor demand elasticity to wages. See section 4 for details.
Figure 1: Internet Users in the US

Internet Users (per 100 people)

Source: World Development Indicators - World Bank
Note: Sample restricted to employed workers with a Bachelors or a Masters degree. Definition of Computer Scientists and STEM workers determined by occupational coding (for details see Data Appendix).
Source: March CPS
Figure 3: Computer Science Fraction of Bachelor Degrees Awarded in US

Note: STEM majors are defined as engineering, computer and math sciences and natural science.
Source: IPEDS Completions Survey.
Figure 4: Relative Earnings of Computer Scientists

Note: Earnings are median weekly earnings. Imputed values excluded (see Data Appendix for details). Sample restricted to employed workers with a Bachelor's or a Master's degree. Definition of Computer Scientists and STEM workers determined by occupational coding (for details see Data Appendix).

Source: March CPS, lagged by 1 year.
Figure 5: Foreign Born and Immigrated at Age 18 or Older Fraction of Employed Population by Occupation

Note: Sample restricted to employed workers with a Bachelors or a Masters degree. Definition of Computer Scientists and STEM workers determined by occupational coding (for details see Data Appendix). Immigrant defined as one born abroad, and migrated to the US after the age of 18. Immigration status is not available in the CPS before 1994.
Source: March CPS
Figure 6: H-1 and H-1B Visa Population


Note: Population stock is constructed using estimations of inflow (visas granted) and outflow (deaths, permanent residency, or emigration) of H-1 workers. In later years, the number of visas granted could exceed the visa cap due to exemptions for foreigners who work at universities and non-profit research facilities. Beginning in 2004, an additional 20,000 H-1B visas were except from the cap for foreign workers with a master's or higher degree from a US university.
Note: The full model is the simulation of the economy using the calibrated parameters. The restricted model simulates the same calibrated model, but restricting firms to keep their foreign temporary worker CS employment to its 1994 value. Wages are relative to other STEM occupations. Employment and enrollment are shares of STEM workers and undergrad STEM enrollment, respectively, and are multiplied by 100. The parameter gamma determines the labor demand elasticity to wages. See Section 4 for details.
Figure 8: Model and Counterfactual (2/2)

Note: The full model is the simulation of the economy using the calibrated parameters. The restricted model simulates the same calibrated model, but restricting firms to keep their foreign temporary worker CS employment to its 1994 value. Wages are relative to other STEM occupations. Employment and enrollment are shares of STEM workers and undergrad STEM enrollment, respectively, and are multiplied by 100. The parameter gamma determines the labor demand elasticity to wages. See Section 4 for details.
Appendix

A Data Appendix

This study draws on a variety of datasets. The sample used in Tables 1 and 2 are based on the IPUMS Census from 1970 to 2000. We restrict the sample to employed workers. We use the IPUMS suggested occupation crosswalk and define computer scientists as computer systems analysts, computer scientists and computer software developers with at least a BA degree. STEM occupations are defined as engineers, computer systems analysts and computer scientists, computer software developers, operations and systems researchers and analysts, actuaries, statisticians, mathematicians and mathematical scientists, physicists and astronomers, chemists, atmospheric and space scientists, geologists, physical scientists n.e.c., agricultural and food scientists, biological scientists, foresters and conservation scientists, and medical scientists.

In Table 2 we define foreigners as either naturalized citizens or non-citizens who immigrated after the age of 22. For early Census years the year of immigration is only available in ranges. In order to construct a precise year of immigration value for workers in those samples we choose to select a random value within the year range for each individual.

Data on earnings, domestic employment and foreign employment used in the calibration procedure and in Figures 2, 4, 5, 7 and 8 come from the March CPS, obtained from the IPUMS and NBER websites. The sample consists of employed persons with at least a BA degree. A person is defined as ‘foreign’ if he/she was born outside the United States and immigrated after the age of 18. Earnings are deflated to 1999 dollars, and top-coded values are multiplied by 1.4.

In our analysis we drop imputed earnings. In order to identify these imputed values, we use a methodology similar to Bollinger and Hirsch (2007). From the IPUMS database we use the qinclongj and qincwage variables, and from the NBER database we use the FL665 flag to identify imputations. The database also contains ten Census Bureau flags that identify a small fraction (less than 1%) of earnings as allocated. Over the period under study around 26% of earnings were allocated. This fraction of imputations varies over time - between 19.14% (in 1994) and 29.47% (in 2003). These numbers are consistent with Bollinger and Hirsch (2007) who find that between 1998 and 2006, the non-response rate was about 20%. The small difference in our numbers arises both

\[43\text{We thank Thomas Lemiux and Chris Bollinger for their guidance on this issue}\]
from using a different sample (restricted to those with BA/MA degree) and because non-response is not the only reason the CPS imputes earnings.

In order to define workers as STEM or working in Computer Science we use the occupational codes in the CPS Outgoing Rotation Group (CPS-ORG) data set. Occupational coding in the CPS-ORG changed between 2002 (using the 1990 definition) and 2003 (using the 2000 definition). Between 2000 and 2002, both occupational codes are available in the data allowing us to create a crosswalk by: (a) first identifying STEM and Computer Science workers using the year 2000 occupational codes, and then (b) assigning weights to each 1990 occupational code to be consistent with the new definitions. The reason we start with the year 2000 occupational codes is because it captures a more exhaustive list of modern occupations that are especially relevant to this analysis.

Figure 3 and the enrollment series in Figures 7 and 8 are based on Integrated Post-secondary Education Data System (IPEDS) Completions Survey. It consists of bachelor’s degrees awarded by the NSF population of institutions. STEM majors fields are defined as engineering, astronomy, chemistry, physics, other physical sciences, atmospheric sciences, earth sciences, oceanography, mathematics and statistics, computer science, agricultural sciences, biological sciences, medical sciences, and other life sciences. Enrollment in computer science (Figures 7 and 8) is defined as number of degrees awarded in this field lagged by 2 years.

B Model Extension: Permanent Residents

Here we propose an extension of our main model which replaces certain assumptions about labor supply and demand in this model by allowing some foreign workers who migrate using a temporary visa to stay in the US as permanent residents. We calibrate this model as well and present some of its results.

B.1 Labor Supply

Labor supply of Americans computer scientists is defined as in the main model. In contrast, there are two types of foreigners in the new model: temporary residents $T_t$ and permanent residents $P_t$. Temporary residents behave like foreigners in the previous model. They are hired for a 6 years contract and cannot switch their occupation once hired to work as computer scientists:
\[ T_t = \sum_{j=0}^{n} R_{t-j} \]  

(1)

The innovation of this version of the model is that we allow half the temporary residents to become permanent residents and stay in the US after the end of their contract.\(^{44}\) When becoming permanent residents, these workers are not attached to a firm and can switch occupations. We assume that permanent residents behave like Americans, meaning that they have the same taste parameters. Furthermore, we assume that they are 30 years old when they become permanent residents.\(^{45}\)

Within this framework, the supply of permanent resident computer scientists at age of 30 is defined as follows:

\[ P_{t}^{30} = (1 - p_{t,30}^{s,30})0.5.R_{t-6} + p_{t,30}^{poc,30}[H_{t}^{30} - 0.5R_{t-6}] \]

where \( p_{t,30}^{s,30} \) is the probability that a 30 years old worker moves from occupation \( s \) to occupation \( S \), and \( H_{t}^{30} \) is the total number of recent permanent residents with an STEM occupation, and in consequence, \( H_{t}^{30} - R_{t-6} \) is the number of recent permanent residents that were working in other STEM jobs in \( t - 1 \).

Two comments are needed regarding the supply of recent permanent residents. First, as we assume that permanent residents behave like Americans, the switching probability \( p_{t,30}^{s,30} \) is the same one identified for 30 year old Americans. It depends on taste parameters and the wage differential between CS and non-CS jobs. Second, we assume that \( H_{t}^{30} \) is exogenous to labor demand shocks or other variables of the model. One can think of this assumptions as the fact that the US only allows a fixed number of workers to become permanent residents every year and this number is independent of other variables presented in this model. Nevertheless, the fraction of recent permanent residents that are computer scientists changes over time and is affected by previous demand for temporary residents.

Following the same steps we used to define the labor supply of Americans, we can define the supply of permanent resident computer scientists at age \( a \) from 31-65 as a function of past employment

\(^{44}\)This share is inline with evidence presented by Lowell (2001) that four-tenths of temporary specialty workers in a H visa contract adjust to permanent residency.

\(^{45}\)The underlying assumption is that foreigners complete a 4 year college and a 2 years Masters program before they are hired as temporary workers (age 24). In fact, U.S. General Accounting Office (2011) shows that more than half of H-1B workers have an advanced degree (master, professional or PhD.) in 2010.
of these types of workers in each occupation, and the migration probabilities:

\[ P^a_t = (1 - p^c_{t,a}) P^a_{t-1} + p^c_{t,a} [H^a_t - P^a_{t-1}] \]

The aggregate permanent resident labor supply of computer scientists is the sum of labor supply of these workers at all ages:

\[ P_t = \sum_{a=30}^{a=65} P^a_t \] (2)

Finally, the foreigners labor supply is defined as the sum of permanent residents and temporary residents at each period of time.

\[ F_t = P_t + T_t \] (3)

B.2 Labor Demand

Firms are indifferent between Americans and permanent residents. These workers have the same productivity and are paid the same wage. Let’s define the domestic labor demand as the sum of American computer scientists \( L_t \) and permanent residents computer scientists as \( P_t \)

\[ D_t = L_t + P_t \] (4)

As before, firms decide how many temporary residents to recruit in each period. Furthermore, firms will also decide how many domestic computer scientists they will hire. The Bellman equation problem of the firm is defined as:

\[ \pi_t = \max_{D_t, R_t} A_t (D_t + T_t)^\gamma - w_t (D_t) - \frac{w_t}{\gamma} T_t - C_R(R_t) + \beta E_t [\pi_{t+1}] \]

subject to the supply of temporary residents:

\[ T_t = \sum_{j=0}^{5} R_{t-j} \]

It is important to note a small difference in the way we are setting up the firm’s problem now. Before, we assumed that temporary workers were more productive than Americans. Now we assume
that they are as productive as domestics, but are paid a lower wage by a fraction \( \theta \).

As before we assume that the recruitment costs of temporary residents include both linear and quadratic components

\[
C_R(R_t) = c_1 R_t + c_2 R_t^2.
\]

As in a previous labor demand problem, the solution to the firm’s decision can be characterized by both the first order and envelope conditions with respect to the employment level. The first order condition of the firm’s maximization problem with respect to \( D_t \) is represented by the following equation:

\[
A_t \gamma (D_t + T_t)^{\gamma - 1} = w_t
\]

(5)

In addition to choosing US worker employment, the firm also decides the number of foreign recruited at each period. The first order condition of the firm’s problem with respect to \( R_t \) is given by:

\[
A_t \gamma (D_t + T_t)^{\gamma - 1} - \frac{w_t}{\theta} - c_1 - 2c_2 R_t + \sum_{j=1}^{5} \beta^j E_t \left[ \frac{\partial \pi_{t+j}}{\partial R_t} \right] = 0
\]

(6)

where \( \frac{\partial \pi_{t+j}}{\partial R_t} \) is defined as how profits in \( t+j \) are affected by changes in the recruitment in \( t \).

Finally, we use the envelope condition to derive the shadow price of past foreign recruitment on current profits, such that:

\[
\frac{\partial \pi}{\partial R_{t-j}} = A_t \gamma (D_t + T_t)^{\gamma - 1} - \frac{w_t}{\theta} \text{ for } j = 1, ..., 5
\]

B.3 Discussion of Permanent Residents Extension

In figures A.1 and A.2, we show the results of calibrating the model including the permanent resident extension in this appendix. They are directly analogous to figures 7 and 8. In setting up the counterfactual with this model extension, we fix \( T_t \), the number of temporary workers, to its 1994 value, to match the policy experiment envisioned in Section 4.3, a reduction in the number of temporary work visas allowed each year.

Overall, there are no drastic changes between the results of the main model and this extension model. Both models predict essentially the same CS wages and American employment. However,

\[\text{Note that if permanent residents were more productive than Americans, firms would just substitute their American workers for permanent residents. This new assumption is with accordance with the evidence presented in section 4.1 that there is a wage premium associated with obtaining a green card.}\]
in the extension model, the counterfactual level of American employment is slightly lower. The extension model predicts slightly higher enrollment, although the counterfactuals are very similar. The foreign employment prediction is similar in both models, until 2004, but is a better fit post-2004 in the permanent residents model. In the counterfactual in the main model, we directly fix foreign employment to its 1994 value, whereas in the extension model, we fix the level of temporary residents, which allows total foreign employment to increase slightly via an increase in the number of permanent residents.
Figure A.1: Extension Model and Counterfactual (1/2)

Note: The full model is the simulation of the economy using the calibrated parameters and the modeling changes to allow for permanent residents in Appendix B. The restricted model simulates the same calibrated model, but restricting firms to keep their foreign temporary worker CS employment to its 1994 value. Wages are relative to other STEM occupations. Employment and enrollment are shares of STEM workers and undergrad STEM enrollment, respectively, and are multiplied by 100. The parameter gamma determines the labor demand elasticity to wages. See Section 4 for further details.
Note: The full model is the simulation of the economy using the calibrated parameters and the modeling changes to allow for permanent residents in Appendix B. The restricted model simulates the same calibrated model, but restricting firms to keep their foreign temporary worker CS employment to its 1994 value. Wages are relative to other STEM occupations. Employment and enrollment are shares of STEM workers and undergrad STEM enrollment, respectively, and are multiplied by 100. The parameter $\gamma$ determines the labor demand elasticity to wages. See Section 4 for further details.
C Additional Model Specifications

C.1 Sensitivity to Foreigner Productivity Premium

In this appendix we try various values of the foreigner productivity premium $\theta$ to see how sensitive our results are to the number used in the text (a 12% premium). We experiment with various values, and have presented a sensitivity analysis for a 9% premium and a 15% premium (for $\gamma = 0.75$). The table below shows how our parameters are not sensitive to the value used. The only parameter that does change is the recruitment costs of foreign workers (as expected). From the figures below, we can see that the model fits well regardless of which parameter value we pick, and the counterfactual exercise where we restrict foreigners is also unaffected by our value of $\theta$.

<table>
<thead>
<tr>
<th>Calibrated Parameters</th>
<th>Productivity Premium</th>
<th>9%</th>
<th>12%</th>
<th>15%</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\alpha_0$</td>
<td>Mean taste for not studying CS</td>
<td>0.1044</td>
<td>0.0836</td>
<td>0.0774</td>
</tr>
<tr>
<td>$\sigma_0$</td>
<td>Std. dev. of study area taste shocks</td>
<td>0.0002</td>
<td>0.0002</td>
<td>0.0002</td>
</tr>
<tr>
<td>$\alpha_1$</td>
<td>Mean taste for not working in CS</td>
<td>0.3529</td>
<td>0.3673</td>
<td>0.3356</td>
</tr>
<tr>
<td>$\sigma_1$</td>
<td>Std. dev. of occupation taste shocks</td>
<td>0.1444</td>
<td>0.1439</td>
<td>0.1477</td>
</tr>
<tr>
<td>$c_{R_1}$</td>
<td>Foreign linear recruitment cost</td>
<td>0.3920</td>
<td>0.5221</td>
<td>0.6510</td>
</tr>
<tr>
<td>$c_{R_2}$</td>
<td>Foreign quadratic recruitment cost</td>
<td>0.0089</td>
<td>0.0124</td>
<td>0.0151</td>
</tr>
<tr>
<td>$\lambda_0$</td>
<td>Sector switching constant cost</td>
<td>0.1289</td>
<td>0.1031</td>
<td>0.0955</td>
</tr>
<tr>
<td>$\lambda_1$</td>
<td>Sector switching linear cost</td>
<td>0.0131</td>
<td>0.0151</td>
<td>0.0083</td>
</tr>
<tr>
<td>$\lambda_2$</td>
<td>Sector switching quadratic cost</td>
<td>0.0002</td>
<td>0.0003</td>
<td>0.0004</td>
</tr>
</tbody>
</table>
Figure 3: Sensitivity Analysis - Different Values of $\theta$ (Full Model)
Figure 4: Sensitivity Analysis - Different Values of $\theta$ (Model that Restricts Foreign Workers to 1994 levels)
C.2 Model with Quadratic Hiring Costs for Americans

We also set-up and calibrate a model that includes a quadratic-term in the hiring costs for Americans. This cost parameter is identical to the quadratic-cost parameter in the hiring of foreigners. This changes the first order conditions for hiring Americans to the following:

\[ A_t \gamma (L_t + \theta F_t)^{\gamma - 1} - 2c_2 L_t = w_t \]

As we can see from the figure below, this does not drastically change the model’s fit.
Figure 5: Quadratic Hiring Costs for Americans